## CBSE Class 10th Mathematics

## Standard Sample Paper- 06

## Maximum Marks:

Time Allowed: 3 hours

## General Instructions:

i. All the questions are compulsory.
ii. The question paper consists of 40 questions divided into 4 sections $\mathrm{A}, \mathrm{B}, \mathrm{C}$, and D .
iii. Section A comprises of 20 questions of 1 mark each. Section $B$ comprises of 6 questions of 2 marks each. Section C comprises of 8 questions of 3 marks each. Section D comprises of 6 questions of 4 marks each.
iv. There is no overall choice. However, an internal choice has been provided in two questions of 1 mark each, two questions of 2 marks each, three questions of 3 marks each, and three questions of 4 marks each. You have to attempt only one of the alternatives in all such questions.
v. Use of calculators is not permitted.

## Section A

1. Which of the following numbers have the non-terminating repeating decimal expansion?
a. $\frac{117}{6^{2} \times 5^{3}}$
b. $\frac{6}{15}$
c. $\frac{21}{280}$
d. $\frac{77}{210}$
2. The LCM of 24,60 and 150 is
a. 2400
b. 1800
c. 600
d. 1200
3. The percentage of marks obtained by 100 students in an examination are as follows:

| Marks | $130-135$ | $135-140$ | $140-145$ | $145-150$ | $150-155$ | $155-160$ | $160-165$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 10 | 15 | 18 | 22 | 23 | 8 | 4 |

The cumulative frequency of the class interval 150-155 is
a. 90
b. 80
c. 100
d. 88
4. In a cricket match Kumble took three wickets less than twice the number of wickets taken by Srinath. The product of the number of wickets taken by these two is 20 , then the number of wickets taken by Kumble is
a. 4
b. 5
c. 10
d. 2
5. If a $\sin \theta+b \cos \theta=c$, then the value of a $\cos \theta-b \sin \theta$ is
a. $\sqrt{a^{2}+b^{2}-c^{2}}$
b. $\sqrt{a^{2}+b^{2}+c^{2}}$
c. $\sqrt{a^{2}-b^{2}+c^{2}}$
d. None of these
6. Choose the correct option and justify your choice: $\frac{2 \tan 30^{\circ}}{1-\tan ^{2} 30^{0}}$
a. $\cos 60^{\circ}$
b. $\sin 30^{0}$
c. $\sin 60^{0}$
d. $\tan 60^{\circ}$
7. A kite is flying at a height of 200 m above the ground. The string attached to the kite is temporarily tied to a point on the ground. The inclination of the string with the ground is $45^{\circ}$. The length of the string, assuming that there is no slack in the string is
a. 100 m
b. 200 m
c. $200 \sqrt{2} \mathrm{~m}$
d. $100 \sqrt{2} \mathrm{~m}$
8. The co - ordinates of the mid - point of the line joining the points (3p, 4) and ( $-2,4$ ) are ( $5, \mathrm{p}$ ). The value of ' p ' is
a. 1
b. 4
c. 2
d. 3
9. If the co - ordinates of a point are $(-5,11)$, then its abscissa is
a. -5
b. 11
c. 5
d. -11
10. Two dice are thrown simultaneously. The probability of getting a doublet is
a. $\frac{1}{6}$
b. $\frac{1}{2}$
c. $\frac{2}{3}$
d. $\frac{1}{36}$
11. Fill in the blanks:

The TSA of a solid hemisphere of diameter 2 cm is $\qquad$ .
12. Fill in the blanks:

The product of the zeroes of $-2 x^{2}+k x+6$ is $\qquad$ .

OR

Fill in the blanks:

The product of the zeroes of $-2 x^{2}+k x+6$ is $\qquad$ .
13. Fill in the blanks:
$\triangle A B C$ and $\triangle D E F$ are similar. Area of $\triangle A B C$ is $9 \mathrm{~cm}^{2}$ and Area of $\triangle D E F$ is $64 \mathrm{~cm}^{2}$. If $D E=5.1 \mathrm{~cm}$, then the value of AB is $\qquad$ .
14. Fill in the blanks:

1, 4, 9 form a sequence in which next two terms are $\qquad$ .
15. Fill in the blanks:

If the vertices of a triangle have integral coordinates, then the triangle cannot be
$\qquad$ triangle.
16. Can we have any $\mathrm{n} \in \mathrm{N}$, where $4^{\mathrm{n}}$ ends digit zero?
17. In Fig. if $\angle A=\angle \mathrm{C}$, then prove that $\triangle \mathrm{AOB} \sim \Delta \mathrm{COD}$.

18. If the sum of first k terms of an A.P. is $3 \mathrm{k}^{2}-\mathrm{k}$ and its common difference is 6 . What is the first term?

## OR

What is 18 th term of the sequence defined by $\mathrm{a}_{\mathrm{n}}=\frac{n(n-3)}{n+4}$.
19. Two tangents making an angle of $60^{\circ}$ between them are drawn to a circle of radius $\sqrt{3} \mathrm{~cm}$ then find the length of each tangent.

20. Determine whether the given quadratic equation has real roots or not.
$x^{2}-2 x+1=0$

## Section B

21. A box contains 12 balls out of which $x$ are black. If one ball is drawn at random from the box, what is the probability that it will be a black ball? If 6 more black balls are put in the box, the probability of drawing a black ball is now double of what it was
before. Find x.
22. Find the value of k for which the roots are real and equal of equation:
$4 x^{2}-2(k+1) x+(k+4)=0$
23. In fig. if $A B \| D C$ and $A C$ and $P Q$ intersect each other at the point $O$, prove that $O A \times C Q$ $=O C \times A P$.


Corresponding sides of two similar triangles are in the ratio of $2: 3$. If the area of the smaller triangle is $48 \mathrm{~cm}^{2}$, find the area of the larger triangle.
24. Vijay lives in a flat in a multi-story building. His driving was rough so his father keeps eye on his driving. Once he drives from his house to Faridabad. His father was standing on the top of the building at point A as shown in the figure. At point C , the angle of depression of a car from the building was $60^{\circ}$. After accelerating 20 m from point C, Vijay stops at point $D$ to buy ice-cream and the angle of depression changed to $30^{\circ}$.


By analysing the above given situation answer the following questions:
i. Find the value of x .
ii. Find the height of the building AB .
25. A quadrilateral ABCD is drawn to circumscribe a circle. Prove that $\mathrm{AB}+\mathrm{CD}=\mathrm{AD}+\mathrm{BC}$

> OR

If PA and PB are tangents drawn from external point P such that $\mathrm{PA}=10 \mathrm{~cm}$ and $\angle \mathrm{APB}$ $=60^{\circ}$, find the length of chord $A B$.
26. A farmer used to irrigate his land during summer on a regular basis to grow his crops and save them from dry weather. To irrigate his land he built a tube well in his field. The tube well has a rectangular tank and a pipe that is used to fill this tank. The dimensions of this tube well system are:
Water is flowing at the rate of $5 \mathrm{~km} / \mathrm{hr}$ through a pipe of diameter 14 cm into a rectangular tank which is 50 m long and 44 m wide.


After reading the above given information, answer the following questions:
i. The volume of the water flowing through the cylindrical pipe in $x$ hours.
ii. Determine the time in which the level of the water in the tank will rise by 7 cm .

## Section C

27. Prove that $\sqrt{5}+\sqrt{3}$ is irrational number.

## OR

Write the HCF and LCM of smallest odd composite number and the smallest odd prime number. If an odd number $p$ divides $q^{2}$, then will it divide $q^{3}$ also? Explain.
28. In an A.P., if the $5^{\text {th }}$ and $12^{\text {th }}$ terms are 30 and 65 respectively, what is the sum of first

20 terms?
29. Find the values of $a$ and $b$ for which the following system of equations has infinitely many solutions:
$2 x+3 y=7$
$2 a x+a y=28-b y$

## OR

Solve $2 x+3 y=11$ and $2 x-4 y=-24$ and hence find the value of ' $m$ ' for which $y=m x+$ 3.
30. Divide the polynomial $f(x)=30 x^{4}+11 x^{3}-82 x^{2}-12 x+48$ by $3 x^{2}+2 x-4$. Also, find the quotient and remainder
31. Name the type of quadrilateral formed, if any, by the following points, and give reasons for your answer: $(-3,5),(3,1),(0,3),(-1,-4)$
32. Prove the trigonometric identity:
$\sec ^{6} \theta=\tan ^{6} \theta+3 \tan ^{2} \theta \sec ^{2} \theta+1$

## OR

If $\sec \theta+\tan \theta=\mathrm{p}$, find the value of $\operatorname{cosec} \theta$.
33. The radius of a circle with centre $O$ is 5 cm (fig.). Two radii OA and OB are drawn at right angles to each other. Find the areas of the segments made by the chord AB (Take $\pi=3.14)$

34. The agewise participation of students in the Annual Function of a school is shown in the following distribution.

| Age(in years) | $5-7$ | $7-9$ | $9-11$ | $11-13$ | $13-15$ | $15-17$ | $17-19$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of students | x | 15 | 18 | 30 | 50 | 48 | x |

Find the missing frequencies when the sum of frequencies is 181 . Also, find the mode of the data.

## Section D

35. Construct an isoceles triangle ABC with base $\mathrm{BC}=6 \mathrm{~cm}, \mathrm{AB}=\mathrm{AC}$ and $\angle A=90^{\circ}$. Draw another similar triangle whose sides are $\frac{4}{5}$ times of the sides of $\triangle A B C$. Justify your construction.

## OR

Draw a circle of radius 2 cm with centre O and take a point P outside the circle such that $\mathrm{OP}=6.5 \mathrm{~cm}$. From P, draw two tangents to the circle.
36. Sides AB and AC and median AD of a triangle ABC are respectively proportional to sides PQ and PR and median PM of another triangle PQR. Prove that $\triangle A B C \sim \triangle P Q R$.

37. Solve the following system of equations graphically:
$x+2 y-7=0$
$2 x-y-4=0$
OR

One says, "Give me a hundred rupee, friend! I shall then become twice as rich as you are." The other replies, "If you give me ten rupees, I shall be six times as rich as you are." Tell me how much money both have initially?
38. A friction clutch is in the form of a frustum of a cone, the diameter of the ends being 32 cm and 20 cm and length 8 cm . Find its bearing surface and volume.

## OR

The difference between the sides at right angles in a right-angled triangle is 14 cm . The area of the triangle is $120 \mathrm{~cm}^{2}$. Calculate the perimeter of the triangle.
39. A vertical tower stands on a horizontal plane and is surmounted by a flag-staff of height 7 m . From a point on the plane, the angle of elevation of the bottom of the flagstaff is $30^{\circ}$ and that of the top of the flag-staff is $45^{\circ}$. Find the height of the tower.
40. In annual day of a school, age-wise participation of students is shown in the following frequency distribution:

| Age of <br> student (in <br> years) | $5-7$ | $7-9$ | $9-11$ | $11-13$ | $13-15$ | $15-17$ | $17-19$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of <br> students | 20 | 18 | 22 | 25 | 20 | 15 | 10 |

Draw a less than type' ogive for the above data and from it find the median age.

## CBSE Class 10th Mathematics Standard

## Sample Paper - 01

## Solution

## Section A

1. (d)
$\frac{77}{210}$
Explanation:
$\frac{77}{210}=\frac{11}{30}=\frac{11}{2 \times 3 \times 5}$
Because non-terminating repeating decimal expansion should have the denominator other than 2 or 5 .
2. (c)

600

Explanation:
$24=2^{3} \times 3$
$60=2^{2} \times 3 \times 5$
$150=2 \times 3 \times 5^{2}$
$\therefore \operatorname{LCM}(24,60,150)=2^{3} \times 3 \times 5^{2}=600$
3. (d) 88

Explanation:

| Marks | $130-$ <br> 135 | $135-$ <br> 140 | $140-$ <br> 145 | $145-$ <br> 150 | $150-$ <br> 155 | $155-$ <br> 160 | $160-$ <br> 165 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 10 | 15 | 18 | 22 | 23 | 8 | 4 |
| Cumulative <br> Frequency | 10 | 25 | 43 | 65 | 88 | 96 | 100 |

Therefore, cumulative frequency of the class interval $150-155$ is 88.
4. (b) 5

Explanation:

Let the number of wickets taken by Srinath be $x$ then the number of wickets taken by Kumble will be $2 x-3$
According to question, $x(2 x-3)=20$
$\Rightarrow 2 x^{2}-3 x-20=0$
$\Rightarrow 2 x^{2}-8 x+5 x-20=0$
$\Rightarrow 2 x(x-4)+5(x-4)=0$
$\Rightarrow(x-4)(2 x+5)=0$
$\Rightarrow x-4=0$ and $2 x+5=0$
$\Rightarrow x=4$ and $x=\frac{-5}{2}$ [ $x=\frac{-5}{2}$ is not possible]
Therefore, number of wickets taken by Srinath is 4 .
Then number of wickets taken by Kumble $=2 \times 4-3=5$
5. (a)

$$
\sqrt{a^{2}+b^{2}-c^{2}}
$$

Explanation:
Given: $a \sin \theta+b \cos \theta=c$
Squaring both sides, we get
$\Rightarrow a^{2} \sin ^{2} \theta+b^{2} \cos ^{2} \theta+2 a b \sin \theta \cos \theta=c^{2}$
$\Rightarrow a^{2}\left(1-\cos ^{2} \theta\right)+b^{2}\left(1-\sin ^{2} \theta\right)+2 a b \sin \theta \cos \theta=c^{2}$
$\Rightarrow a^{2}-a^{2} \cos ^{2} \theta+b^{2}-b^{2} \sin ^{2} \theta+2 a b \sin \theta \cos \theta=c^{2}$
$\Rightarrow a^{2} \cos ^{2} \theta-b^{2} \sin ^{2} \theta-2 a b \sin \theta \cos \theta=a^{2}+b^{2}-c^{2}$
$\Rightarrow(a \cos \theta-b \sin \theta)^{2}=a^{2}+b^{2}-c^{2}$
$\Rightarrow a \cos \theta-b \sin \theta=\sqrt{a^{2}+b^{2}-c^{2}}$
6. (d) $\tan 60^{0}$

Explanation:

$$
\begin{aligned}
& \frac{2 \tan 30^{0}}{1-\tan ^{2} 30^{0}} \\
& =\frac{2 \times \frac{1}{\sqrt{3}}}{1-\left(\frac{1}{\sqrt{3}}\right)^{2}}=\frac{\frac{2}{\sqrt{3}}}{1-\frac{1}{3}} \\
& =\frac{\frac{2}{\sqrt{3}}}{\frac{2}{3}}=\frac{2}{\sqrt{3}} \times \frac{3}{2}=\sqrt{3}=\tan 60^{\circ}
\end{aligned}
$$

7. (c) $200 \sqrt{2} \mathrm{~m}$

Explanation:


Here, in triangle $A B C$, Height of the slide $=A B=200 \mathrm{~m}$
Angle of elevation $=\theta=45^{\circ}$ To find: Length of the string $=\mathrm{AC}$
$\therefore \sin 45^{\circ}=\frac{\mathrm{AB}}{\mathrm{AC}}$
$\Rightarrow \frac{1}{\sqrt{2}}=\frac{200}{\mathrm{AC}}$
$\Rightarrow \mathrm{AC}=200 \sqrt{2} \mathrm{~m}$
8. (b) 4

Explanation:

Let the coordinates of midpoint $\mathrm{O}(5, p)$ is equidistance from the points $\mathrm{A}(3 p, 4)$ and $\mathrm{B}(-2,4)$. (because O is the mid-point of AB )
$\therefore 5=\frac{3 p-2}{2} \Rightarrow 3 p-2=10$
$\Rightarrow 3 p=12 \Rightarrow p=4$
Also $p=\frac{4+4}{2} \Rightarrow p=4$
9. (a) -5

Explanation:
Since $x$-coordinate of a point is called abscissa.

Therefore, abscissa is -5 .
10. (a) $\frac{1}{6}$

Explanation:
Doublet means getting same number on both dice simultaneously
Doublets $=(1,1),(2,2),(3,3),(4,4),(5,5),(6,6)$
Number of possible outcomes $=6$
Total number of ways to throw a dice $=36$
Probability of getting a doublet $=\frac{6}{36}=\frac{1}{6}$
11. $3 \pi \mathrm{~cm}^{2}$
12. -3 OR -3
13. $\mathrm{AB}=1.91 \mathrm{~cm}$
14. 16,25
15. equilateral triangle
16. If a number ends with zero then it is divisible by 5 .

For unit's digit to be 0 , then $4^{\mathrm{n}}$ should have 2 and 5 as its prime factors, but $4^{\mathrm{n}}=\left(2^{2}\right)^{\mathrm{n}}=$ $2^{2 n}$.

As $n \in N$ we take $n=1,2,3,4 \ldots$..etc

So above becomes $4^{1}, 4^{2}$...etc
As it does not contain 5 as one of its prime factors.
Therefore, $4^{\mathrm{n}}$ will not end with digit 0 for $\mathrm{n} \in \mathrm{N}$.
17. In triangles $A O B$ and COD, we obtain
$\angle \mathrm{A}=\angle \mathrm{C}$ (Given)
and, $\angle 1=\angle 2$ [Vertically opposite angles]

Therefore, by AA- criterion of similarity, we obtain
$\Delta A O B \sim \Delta C O D$
18. Let the sum of $k$ terms of A.P. is $S_{n}=3 k^{2}-k$

Now $\mathrm{k}^{\text {th }}$ term of A.P $=\mathrm{S}_{\mathrm{n}}-\mathrm{S}_{\mathrm{n}-1}$
$a_{k}=\left(3 k^{2}-k\right)-\left[3(k-1)^{2}-(k-1)\right]$
$=\left(3 \mathrm{k}^{2}-\mathrm{k}\right)-\left[3\left(\mathrm{k}^{2}-2 \mathrm{k}+1\right)-(\mathrm{k}-1)\right]$
$=3 \mathrm{k}^{2}-\mathrm{k}-\left[3 \mathrm{k}^{2}-6 \mathrm{k}+3-\mathrm{k}+1\right]$
$=3 \mathrm{k}^{2}-\mathrm{k}-\left[3 \mathrm{k}^{2}-7 \mathrm{k}+4\right]$
$=3 \mathrm{k}^{2}-\mathrm{k}-3 \mathrm{k}^{2}+7 \mathrm{k}-4$
$=6 \mathrm{k}-4$
first term $=\mathrm{a}=6 \times 1-4=6-4=2$

## OR

We have to find the 18 th term of the sequence defined by $\mathrm{a}_{\mathrm{n}}=\frac{n(n-3)}{n+4}$.
We have, $\mathrm{a}_{\mathrm{n}}=\frac{n(n-3)}{n+4}$
Putting $\mathrm{n}=18$, we get
$\mathrm{a}_{18}=\frac{18 \times(18-3)}{18+4}=\frac{18 \times 15}{22}=\frac{135}{11}$
19. $\tan 30^{\circ}=\frac{O A}{A P}$
$\Rightarrow \frac{1}{\sqrt{3}}=\frac{\sqrt{3}}{A P}$
$\Rightarrow A P=3$
$\therefore A P=B P=3 \mathrm{~cm}$
20. $x^{2}-2 x+1=0$

Now, Discriminant D $=(-2)^{2}-4 \times 1 \times 1=4-4=0$
For real roots, discriminant should be greater than or equal to zero, so the given equation has real roots.

## Section B

21. There are 12 balls in the box.

Therefore, the total number of favourbale outcomes $=12$
The number of favourable outcomes $=x$
Proabibilty of the event $=\frac{\text { Number of favourble outcomes }}{\text { Total number of possible outcomes }}$
Therefore P1 $=P($ Getting a black ball $)=\frac{x}{12}$
If 6 more balls put in the box, then
Total number of favourable outcomes $=12+6=18$
And Number of favourable outcomes $=x+6$
$\therefore \mathrm{P}_{2}=P($ Getting a black ball $)=\frac{x+6}{12}$
According to question, $\mathrm{P}_{2}=2 \mathrm{P}_{1}$
$\frac{x+6}{18}=2 \times \frac{x}{12}$
$\frac{x+6}{18} \times \frac{12}{x}=2$
$x=3$
22. The given equation is $4 \mathrm{x}^{2}-2(\mathrm{k}+1) \mathrm{x}+(\mathrm{k}+4)=0$

It has real and equal roots, so $\mathrm{D}=0$
$b^{2}-4 a c=0$
$[-2(k+1)]^{2}-4 \times 4(k+4)=0$
$4(k+1)^{2}-16(k+4)=0$
$4 k^{2}+8 k+4-16 k-64=0$
$4 k^{2}-8 k-60=0$
$k^{2}-2 k-15=0$
$\mathrm{k}^{2}-5 \mathrm{k}+3 \mathrm{k}-15=0$
$k(k-5)+3(k-5)=0$
$(k-5)(k+3)=0$
$k=5,-3$
23. According to the question, we are given that,
$\mathrm{AB} \| \mathrm{DC}$


In $\triangle \mathrm{APO}$ and $\triangle \mathrm{CQO}$, we have,
$\angle \mathrm{A}=\angle \mathrm{C}$
$\angle \mathrm{P}=\angle \mathrm{Q}$ (Alternate interior angles)
$\triangle \mathrm{APO} \sim \triangle \mathrm{CQO}$ (AA siimilarity)
$\frac{\mathrm{OA}}{\mathrm{OC}}=\frac{\mathrm{AP}}{\mathrm{CQ}} \Rightarrow \mathrm{OA} \times \mathrm{CQ}=\mathrm{OC} \times \mathrm{AP}$
OR

We know that ,if two triangles are similar,then, the ratio of the areas is the square of the ratio of their corresponding sides.

Since $\triangle \mathrm{ABC} \sim \triangle \mathrm{DEF}$, therfore by above theorem, we have,

$$
\frac{\operatorname{ar}(\triangle A B C)}{\operatorname{ar}(\triangle D E F)}=\left(\frac{A B}{D E}\right)^{2}
$$

But, $\mathrm{AB}: \mathrm{DE}=2: 3$ (Given)
and $\operatorname{ar}(\triangle \mathrm{ABC})($ smaller $)=48 \mathrm{~cm}^{2}$
$\therefore \frac{48}{\operatorname{ar}(\triangle D E F)}=\left(\frac{2}{3}\right)^{2}$
$\Rightarrow \operatorname{ar}(\Delta \mathrm{DEF})=\frac{48 \times 9}{4}=108 \mathrm{~cm}^{2}$
24. The above figure can be redrawn as shown below:

i. From the figure,
let $A B=h$ and $B C=x$
In $\triangle \mathrm{ABC}$,
$\tan 60=\frac{\mathrm{AB}}{\mathrm{BC}}=\frac{\mathrm{h}}{x}$
$\sqrt{3}=\frac{\mathrm{h}}{x}$
$h=\sqrt{3} \mathrm{x}$
In $\triangle \mathrm{ABD}$,
$\tan 30=\frac{\mathrm{AB}}{\mathrm{BD}}=\frac{\mathrm{h}}{x+20}$
$\frac{1}{\sqrt{3}}=\frac{\sqrt{3} x}{x+20}[$ using (i)]
$\mathrm{x}+20=3 \mathrm{x}$
$x=10 m$
ii. Height of the building, $h=\sqrt{3} x=10 \sqrt{3}=17.32 \mathrm{~m}$
25. We know that the tangent segments from an external point to a circle are equal

$\therefore \mathrm{AP}=\mathrm{AS}$
$B P=B Q$
$C R=C Q$
DR = DS

Adding (1), (2), (3) and (4), we get
$(\mathrm{AP}+\mathrm{BP})+(\mathrm{CR}+\mathrm{DR})=(\mathrm{AS}+\mathrm{BQ}+\mathrm{CQ}+\mathrm{DS})$
$\Rightarrow \mathrm{AB}+\mathrm{CD}=(\mathrm{AS}+\mathrm{DS})+(\mathrm{BQ}+\mathrm{CQ})$
$\Rightarrow \mathrm{AB}+\mathrm{CD}=\mathrm{AD}+\mathrm{BC}$

OR

$\because \angle \mathrm{APB}=60^{\circ}$
$\angle \mathrm{AOB}=120^{\circ}$ [O is centre of circle]
$\angle \mathrm{OAB}=\angle \mathrm{OBA}=30^{\circ}$
$\therefore \angle \mathrm{PAB}=60^{\circ}, \angle \mathrm{PBA}=60^{\circ}$
$\therefore \triangle \mathrm{PAB}$ is equilateral triangle
$\therefore \mathrm{AB}=\mathrm{PA}=10 \mathrm{~cm}$
26. According to question,

Diameter of the pipe $=14 \mathrm{~cm}$
Thus, Radius of the pipe $=7 \mathrm{~cm}$
Now, the volume of the water flowing through the cylindrical pipe in 1 hour $=\pi r^{2} h$ Clearly, the water column forms a cylinder whose radius $\mathrm{r}=\frac{14}{2} \mathrm{~cm}=\frac{7}{100} \mathrm{~m}$ and Length $=\mathrm{h}=5000 \mathrm{x}$ m
i. Volume of the water flowing through the cylindrical pipe in $x$ hours

$$
\begin{aligned}
& =\pi r^{2} h=\frac{22}{7} \times\left(\frac{7}{100}\right)^{2} \times 5000 x m^{3}=\frac{22}{7} \times \frac{7}{100} \times \frac{7}{100} \times 5000 x \\
& =77 x \mathrm{~m}^{3}
\end{aligned}
$$

ii. Volume of the water that falls into the tank in x hours $=50 \times 44 \times \frac{7}{100}=154 \mathrm{~m}^{3}$ Volume of the water flowing through the cylindrical pipe in x hours $=$ Volume of
the water that falls in the tank in $x$ hours
$\Rightarrow 77 \mathrm{x}=154$
$\Rightarrow \quad x=\frac{154}{77}=2$
Hence, the level of water in the tank will rise by 7 cm in 2 hours.

## Section C

27. Let $\sqrt{5}+\sqrt{3}$ be rational number equal to $\frac{a}{b}$. there exist co-prime integers a and b such that
$\sqrt{5}+\sqrt{3}=\frac{a}{b}$
$\Rightarrow \quad \sqrt{5}=\frac{a}{b}-\sqrt{3}$
$\Rightarrow \quad(\sqrt{5})^{2}=\left(\frac{a}{b}-\sqrt{3}\right)^{2}$ [Squaring both sides] we get,
$\Rightarrow \quad 5=\frac{a^{2}}{b^{2}}-\frac{2 a \sqrt{3}}{b}+3$
$\Rightarrow \quad 2=\frac{a^{2}}{b^{2}}-\frac{2 \sqrt{3} a}{b}$
$\sqrt{3}=\left(a^{2}-2 b^{2}\right) \frac{b}{2 a b}$
Since a,b are integers, therefore $\left(a^{2}-2 b^{2}\right) \frac{b}{2 a b}$ is a rational number which is a contradiction as $\sqrt{3}$ is an irrational number.
Hence, $\sqrt{5}+\sqrt{3}$ is irrational.

Smallest odd composite number $=9$
and smallest odd prime number $=3$

HCF of 9 and $3=3$ and LCM of 9 and $3=9$

Now, if an odd number $p$ divides $q^{2}$, then $p$ is one of the factors of $q^{2}$,
i.e. $q^{2}=p m$, for some integer $m$.....(i)

Now, $q^{3}=q^{2} \times q$
$\Rightarrow q^{3}=p m \times q$
$\Rightarrow q^{3}=p(\mathrm{mq})[$ from $E q(\mathrm{i})]$
$\Rightarrow p$ is a factor of $q^{3}$ also $\Rightarrow p$ divides $q^{3}$.
28. Let first term be a and common difference be d

Given $5^{\text {th }}$ term $=30$
$\Rightarrow \mathrm{a}+(5-1) \mathrm{d}=30$
$\Rightarrow \mathrm{a}+4 \mathrm{~d}=30$
and, $12^{\text {th }}$ term $=65$
$\Rightarrow \mathrm{a}+(12-1) \mathrm{d}=65$
$\Rightarrow \mathrm{a}+11 \mathrm{~d}=65$
Subtracting equation (i) from equation (ii)
$a+11 d-a-4 d=65-30$
$\Rightarrow 7 \mathrm{~d}=35$
$\Rightarrow d=\frac{35}{7}=5$
Putting value of $d$ in equation (i)
$a+4 \times 5=30$
$\Rightarrow \mathrm{a}=30-20=10$
$\therefore$ Sum of first 20 terms $=\frac{n}{2}[2 a+(n-1) d]$
$=\frac{20}{2}[2 \times 10+(20-1) \times 5]$
$=10[20+95]$
$=10 \times 115$
$=1150$
29. The given system of equations may be written as
$2 x+3 y-7=0$
$2 a x+a y+b y-28=0 \Rightarrow 2 a x+(a+b) y-28=0$
This system of equations is of the form
$a_{1} x+b_{1} y+c_{1}=0$
$a_{2} x+b_{2} y+c_{2}=0$
where, $\mathrm{a}_{1}=2, \mathrm{~b}_{1}=3, \mathrm{c}_{1}=-7$
And, $\mathrm{a}_{2}=2 \mathrm{a}, \mathrm{b}_{2}=\mathrm{a}+\mathrm{b}, \mathrm{c}_{2}=-28$
For the system of equations to have infinite solutions,
$\frac{a_{1}}{a_{2}}=\frac{b_{1}}{b_{2}}=\frac{c_{1}}{c_{2}}$
$\Rightarrow \frac{2}{2 a}=\frac{3}{a+b}=\frac{-7}{-28}$
$\Rightarrow \frac{1}{a}=\frac{3}{a+b}=\frac{1}{4}$
Now, $\frac{1}{a}=\frac{1}{4}$
$\Rightarrow \mathrm{a}=4$
And, $\frac{1}{a}=\frac{3}{a+b}$
$\Rightarrow a+b=3 a$
$\Rightarrow 2 a=b$
$\Rightarrow 2 \times 4=\mathrm{b}$
$\Rightarrow b=8$
Hence, the given system of equations will have infinite number of solutions for $a=4 a n d b=8$.

## OR

The given pair of linear equations
$2 x+3 y=11$
$2 x-4 y=-24$
From equation (1), $3 y=11-2 x$
$\Rightarrow \quad y=\frac{11-2 x}{3}$
Substituting this value of y in equation (2), we get
$2 x-4\left(\frac{11-2 x}{3}\right)=-24$
$\Rightarrow 6 x-44+8 x=-72$
$\Rightarrow 14 x-44=-72$
$\Rightarrow 14 x=44-72$
$\Rightarrow 14 x=-28$
$\Rightarrow x=-\frac{28}{14}=-2$
Substituting this value of x in equation (3), we get
$y=\frac{11-2(-2)}{3}=\frac{11+4}{3}=\frac{15}{3}=5$
Verification, Substituting $x=-2$ and $y=5$, we find that both the equations (1) and (2) are satisfied as shown below:
$2 x+3 y=2(-2)+3(5)=-4+15=11$
$2 x-4 y=2(-2)-4(5)=-4-20=-24$
This verifies the solution,
Now, $\mathrm{y}=\mathrm{axe}+3$
$\Rightarrow 5=m(-2)+3$
$\Rightarrow-2 m=5-3$
$\Rightarrow-2 m=2$
$\Rightarrow \mathrm{m}=\frac{2}{-2}=-1$
30. Using long division method, we obtain

$$
\begin{gathered}
3 x ^ { 2 } + 2 x - 4 \longdiv { 3 0 x ^ { 4 } + 1 1 x ^ { 3 } - 8 2 x ^ { 2 } - 1 2 x + 4 8 ( 1 0 x ^ { 2 } - 3 x - 1 2 } \begin{array} { c } 
{ 3 0 x ^ { 4 } + 2 0 x ^ { 3 } - 4 0 x ^ { 2 } } \\
{ - \quad - \quad + } \\
{ - \begin{array} { l } 
{ - 9 x ^ { 3 } - 4 2 x ^ { 2 } - 1 2 x + 4 8 } \\
{ - 9 x ^ { 3 } - 6 x ^ { 2 } + 1 2 x }
\end{array} } \\
{ \frac { + \quad + } { + 3 6 x ^ { 2 } - 2 4 x + 4 8 } } \\
{ - 3 6 x ^ { 2 } - 2 4 x + 4 8 }
\end{array}
\end{gathered}
$$

Clearly, quotient $\mathrm{q}(\mathrm{x})=10 \mathrm{x}^{2}-3 \mathrm{x}-12$ and remainder $\mathrm{r}(\mathrm{x})=0$.
Also,
$\mathrm{g}(\mathrm{x}) \mathrm{q}(\mathrm{x})+\mathrm{r}(\mathrm{x})=\left(3 \mathrm{x}^{2}+2 \mathrm{x}-4\right)\left(10 \mathrm{x}^{2}-3 \mathrm{x}-12\right)+0$
$=3 x^{2}\left(10 x^{2}-3 x-12\right)+2 x\left(10 x^{2}-3 x-12\right)-4\left(10 x^{2}-3 x-12\right)+0$
$=30 \mathrm{x}^{4}-9 \mathrm{x}^{3}-36 \mathrm{x}^{2}+20 \mathrm{x}^{3}-6 \mathrm{x}^{2}-24 \mathrm{x}-40 \mathrm{x}^{2}+12 \mathrm{x}+48+0$
$=30 x^{4}-9 x^{3}+20 x^{3}-36 x^{2}-6 x^{2}-40 x^{2}-24 x+12 x+48+0$
$=30 \mathrm{x}^{4}+11 \mathrm{x}^{3}-82 \mathrm{x}^{2}-12 \mathrm{x}+48$
i.e. $f(x)=g(x) q(x)+r(x)=30 x^{4}+11 x^{3}-82 x^{2}-12 x+48=f(x)$
or, Dividend $=$ Quotient $\times$ Divisor + Remainder.
31. $(-3,5),(3,1),(0,3),(-1,-4)$

Let $\mathrm{A} \rightarrow(-3,5), \mathrm{B} \rightarrow(3,1), \mathrm{C} \rightarrow(0,3)$ and $\mathrm{D} \rightarrow(-1,-4)$
Then, $A B=\sqrt{(3-(-3))^{2}+(1-5)^{2}}=\sqrt{(6)^{2}+(-4)^{2}}$
$=\sqrt{36+16}=\sqrt{52}=2 \sqrt{13}$
$B C=\sqrt{(0-3)^{2}+(3-1)^{2}}=\sqrt{9+4}=\sqrt{13}$
$C D=\sqrt{(-1-0)^{2}+(-4-3)^{2}}=\sqrt{1+49}=\sqrt{50}$
$D A=\sqrt{[(-3)-(-1)]^{2}+[5-(-4)]^{2}}=\sqrt{4+81}=\sqrt{85}$
$A C=\sqrt{[0-(-3)]^{2}+(3-5)^{2}}=\sqrt{13}$
$B D=\sqrt{(-1-3)^{2}+(-4-1)^{2}}=\sqrt{41}$
We see that $\mathrm{BC}+\mathrm{AC}=\mathrm{AB}$
Hence, the points $\mathrm{A}, \mathrm{B}$ and C are collinear.
So, $A B C D$ is not a quadrilateral.
32. We have to prove that :-
$\Rightarrow \sec ^{6} \theta=\tan ^{6} \theta+3 \tan ^{2} \theta \sec ^{2} \theta+1$
$\Rightarrow \sec ^{6} \theta-\tan ^{6} \theta=3 \tan ^{2} \theta \sec ^{2} \theta+1$
Now, LHS
$=\sec ^{6} \theta-\tan ^{6} \theta$
$=\left(\sec ^{2} \theta\right)^{3}-\left(\tan ^{2} \theta\right)^{3}$
$=\left(\sec ^{2} \theta-\tan ^{2} \theta\right)\left[\left(\sec ^{2} \theta\right)^{2}+\sec ^{2} \theta \tan ^{2} \theta+\left(\tan ^{2} \theta\right)^{2}\right]\left\{\right.$ Since, $\mathrm{a}^{3}-\mathrm{b}^{3}=(\mathrm{a}-\mathrm{b})\left(\mathrm{a}^{2}-\right.$
$\left.\left.a b+b^{2}\right)\right\}$
$=1\left[\sec ^{4} \theta+\sec ^{2} \theta \tan ^{2} \theta+\tan ^{4} \theta\right]\left[\because \sec ^{2} \theta-\tan ^{2} \theta=1\right]$
$=\sec ^{4} \theta+\tan ^{4} \theta+\sec ^{2} \theta \tan ^{2} \theta$
$=\left(\sec ^{2} \theta\right)^{2}+\left(\tan ^{2} \theta\right)^{2}+\sec ^{2} \theta \tan ^{2} \theta$
Adding and subtracting $2 \sec ^{2} \theta \tan ^{2} \theta$
$=\left(\sec ^{2} \theta\right)^{2}+\left(\tan ^{2} \theta\right)^{2}-2 \sec ^{2} \theta \tan ^{2} \theta+2 \sec ^{2} \theta \tan ^{2} \theta+\sec ^{2} \theta \tan ^{2} \theta$
$=\left(\sec ^{2} \theta-\tan ^{2} \theta\right)^{2}+3 \sec ^{2} \theta \tan ^{2} \theta\left[\because(a-b)^{2}=a^{2}+b^{2}-2 a b\right]$
$=1+3 \sec ^{2} \theta \tan ^{2} \theta\left[\because \sec ^{2} \theta-\tan ^{2} \theta=1\right]$
= RHS
Hence proved
OR
Given,
$\sec \theta+\tan \theta=p \ldots$..(i)
Also, we know that,
$\sec ^{2} \theta-\tan ^{2} \theta=1$
$\Rightarrow(\sec \theta-\tan \theta)(\sec \theta+\tan \theta)=1\left[\because a^{2}-b^{2}=(a+b)(a-b)\right]$
$\Rightarrow(\sec \theta-\tan \theta) p=1 \quad$ [using equation (i)]
$\Rightarrow \sec \theta-\tan \theta=\frac{1}{p}$
(i)+(ii), we get,
$\sec \theta+\tan \theta+\sec \theta-\tan \theta=p+\frac{1}{p}$
$\Rightarrow 2 \sec \theta=\frac{p^{2}+1}{p}$
$\Rightarrow \sec \theta=\frac{p^{2}+1}{2 p}$
$\Rightarrow \frac{1}{\cos \theta}=\frac{p^{2}+1}{2 p}$
$\Rightarrow \cos \theta=\frac{2 p}{p^{2}+1}----$
Now, we know that,

$$
\left.\sin \theta=\sqrt{( } 1-\cos ^{2} \theta\right)
$$

put the value of $\cos \theta$ from eq. (iii), we get,

$$
\sin \theta=\sqrt{\left(1-\left(\frac{2 p}{p^{2}+1}\right)^{2}\right)}
$$

$\left.\Rightarrow \sin \theta=\sqrt{( } 1-\frac{4 p^{2}}{\left(p^{2}+1\right)^{2}}\right)$
$\left.\Rightarrow \sin \theta=\sqrt{( } \frac{\left(p^{2}+1\right)^{2}-4 p^{2}}{\left(p^{2}+1\right)^{2}}\right)$
$\Rightarrow \sin \theta=\sqrt{\left(\frac{p^{4}+1+2 p^{2}-4 p^{2}}{\left(p^{2}+1\right)^{2}}\right)}$
$\Rightarrow \sin \theta=\sqrt{\left(\frac{p^{4}+1-2 p^{2}}{\left(p^{2}+1\right)^{2}}\right)}$
$\Rightarrow \sin \theta=\sqrt{\left(\frac{\left(p^{2}-1\right)^{2}}{\left(p^{2}+1\right)^{2}}\right)}$
$\Rightarrow \sin \theta=\frac{p^{2}-1}{p^{2}+1}$
$\operatorname{cosec} \theta=\frac{p^{2}+1}{p^{2}-1}\left[\because \operatorname{cosec} \theta=\frac{1}{\sin \theta}\right]$
hence, $\operatorname{cosec} \theta=\frac{1+p^{2}}{1-p^{2}}$
33.


Radius of circle $=\mathrm{r}=5 \mathrm{~cm}$
Angle of the corresponding sector $=\theta=90^{\circ}$
Area of the minor segment $=\left[\frac{\pi}{360} \times \theta-\sin \frac{\theta}{2} \cos \frac{\theta}{2}\right] r^{2}$
$=\left[\frac{3.14}{360} \times 90^{\circ}-\sin 45^{\circ} \cos 45^{\circ}\right] \times 5 \times 5$
$=\left[\frac{3.14}{4}-\frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}}\right] \times 25$
$=\left[\frac{3.14}{4}-\frac{1}{2}\right] \times 25$
$=\left[\frac{1.57}{2}-\frac{1}{2}\right] \times 25$
$=\left[\frac{0.57}{2}\right] \times 25$
$=7.125 \mathrm{~cm}^{2}$
Area of a circle $=\pi r^{2}=3.14 \times(5)^{2}=78.5 \mathrm{~cm}^{2}$
Now, Area of major segment = Area of circle - Area of minor segment
$=(78.5-7.125) \mathrm{cm}^{2}$
$=71.375 \mathrm{~cm}^{2}$
34. Sum of the frequencies $=181$
$\Rightarrow x+15+18+30+50+48+x=181$
$\Rightarrow 2 x+161=181$
$\Rightarrow x=10$
Thus, the missing frequencies are 10 and 10.
Clearly, the modal class is 13-15, as it has the maximum frequency.
$\therefore l=13, \mathrm{~h}=2, \mathrm{f}_{1}=50, \mathrm{f}_{0}=30, \mathrm{f}_{2}=48$
Mode, $\mathrm{M}_{\mathrm{O}}=l+\left\{h \times \frac{\left(f_{1}-f_{0}\right)}{\left(2 f_{1}-f_{0}-f_{2}\right)}\right\}$
$=13+2\left\{\frac{50-30}{2(50)-30-48}\right\}$
$=13+2 \times \frac{20}{22}$
$=13+1.81=14.81$

## Section D

35. Given, An isosceles $\triangle A B C$ with base $\mathrm{BC}=6 \mathrm{~cm}, A B=A C$ and $\angle A=90^{\circ}$

Then, $\angle B=\angle C=\frac{1}{2} \times 90^{\circ}=45^{\circ}$
Required, $\triangle A^{\prime} B C^{\prime} \sim \triangle A B C$ with the scale factor $\frac{4}{5}$
Steps of construction are as below:
i. First of all, construct an isosceles triangle $\triangle A B C$ where the base $B C=6 \mathrm{~cm}$, $A B=A C, \angle A=90^{\circ}, \angle B=45^{\circ}$ and $\angle C=45^{\circ}$
ii. Through point B , construct an acute angle $\angle C B X$ on the side opposite to the vertex A.
iii. Mark five points $B_{1}, B_{2}, B_{3}, B_{4}, B_{5}$ on BX such that
$B B_{1}=B_{1} B_{2}=B_{2} B_{3}=B_{3} B_{4}=B_{4} B_{5}$
iv. Join the points $B_{5} C$
v. From, point $B_{4}$ draw $B_{4} C^{\prime} \| B_{5} C$ intersecting line segment BC at $C^{\prime}$
vi. Through $C^{\prime}$, draw $C^{\prime} A^{\prime} \| C A$ intersecting AB at $A$,


Hence, $\triangle A^{\prime} B C^{\prime}$ is the required triangle as per the question.
Justification of the triangle drawn is as below:
By the construction, $B_{4} C^{\prime} \| B_{5} C$
Therefore, $\frac{B C^{\prime}}{C^{\prime} C}=\frac{4}{5-4}=\frac{4}{1}$
$\Rightarrow \frac{C^{\prime} C}{B C^{\prime}}=\frac{1}{4}$
Now, $\frac{B C}{B C^{\prime}}=\frac{B C^{\prime}+C^{\prime} C}{B C^{\prime}}$
$\Rightarrow 1+\frac{C^{\prime} C}{B C^{\prime}}=1+\frac{1}{4}$
$\Rightarrow 1+\frac{C^{\prime} C}{B C^{\prime}}=\frac{5}{4}$
i.e, $\frac{B C}{B C^{\prime}}=\frac{5}{4}$

Also, $\triangle A^{\prime} B C^{\prime} \sim \triangle A B C$ [by AA similarity]
Hence it is proved that, $\frac{A^{\prime} C^{\prime}}{A C}=\frac{B C^{\prime}}{B C}=\frac{A^{\prime} B}{A B}=\frac{4}{5}$
OR

## STEPS OF CONSTRUCTION

1. Draw a circle of radius 2 cm and O as centre.
2. Mark a point P outside the circle such that $\mathrm{OP}=6.5 \mathrm{~cm}$.

3. Join OP and bisect it at M.
4. Draw a circle with M as centre and radius equal to MP, to intersect the given circle at the points, T and T .
5. Join PT and PT'.

So, PT and PT' are required tangents.
36. By given condition, we have,
$\frac{A B}{P Q}=\frac{A C}{P R}=\frac{A D}{P M}$
To Prove $\triangle A B C \sim \triangle P Q R$
Construction: produce AD to E such that AD = AE and Produce PM and N such that PM $=\mathrm{MN}$.

Join EC and NR.


Proof In $\triangle A B D$ and $\triangle E C D$, we have
$\mathrm{BD}=\mathrm{CD}[\because \mathrm{D}$ is the midpoint of BC$]$
$\mathrm{AD}=\mathrm{ED}$ [by construction]
$\angle B D A=\angle C D E$ [vertically opposite angles]
$\therefore \triangle A B D \cong \triangle E C D$ [by SAS-congruency).
Therefore, $\mathrm{AB}=\mathrm{EC} . .$. (i) [cpct]
Similarly, $\triangle P Q M \cong \triangle N R M$
Therefore, $\mathrm{PQ}=\mathrm{NR}$. ...(ii) [cpct]
Now, $\frac{A B}{P Q}=\frac{A C}{P R}=\frac{A D}{P M}$ (given)
$\Rightarrow \quad \frac{E C}{N R}=\frac{A C}{P R}=\frac{A D}{P M}$ [using (i) and (ii)]
$\Rightarrow \quad \frac{E C}{N R}=\frac{A C}{P R}=\frac{2 A D}{2 P M}=\frac{A E}{P N}[\because 2 \mathrm{AD}=\mathrm{AE}, 2 \mathrm{PM}=\mathrm{PN}]$
$\Rightarrow \triangle A C E \sim \triangle P N R$ [SSS-similarity].
$\therefore \quad \angle 2=\angle 4$
[corresponding angles of similar triangles are equal].
Similarly, $\angle 1=\angle 3$ [it can be proved by joining $B E$ and $Q N$ and showing
$\triangle A B E \sim \triangle P Q N]$.
$\therefore \quad \angle 1+\angle 2=\angle 3+\angle 4$, i.e, $\angle B A C=\angle Q P R$.
Now, in $\triangle A B C$ and $\triangle P Q R$, we have
$\frac{A B}{P Q}=\frac{A C}{P R}$ [given]
$\angle B A C=\angle Q P R$ [from (iii)]
$\therefore \quad \triangle A B C \sim \triangle P Q R$ [by SAS-similarity].
37. Given equations, $x+2 y-7=0$ and $2 x-y-4=0$

Now, $x+2 y-7=0$
$x=7-2 y$
When $y=1 \Rightarrow x=5$
When $y=2 \Rightarrow x=3$
Thus, we have the following table giving points on the line $x+2 y-7=0$

| x | 5 | 3 |
| :---: | :---: | :---: |
| y | 1 | 2 |

Now, $2 x-y-4=0$
$\Rightarrow y=2 x-4$
When $\mathrm{x}=2$, then $\mathrm{y}=0$
When $x=0$, then $y=-4$
Thus, we have the following table giving points on the line $2 x-y-4=0$

| x | 2 | 0 |
| :---: | :---: | :---: |
| y | 0 | -4 |

Graph:


Clearly, two intersect at P(3,2)

Hence, $x=3$ and $y=2$ is the solution of the given system of equations.

OR

Suppose initially, they had Rs x and Rs. y with them respectively. as per condition given in the question, we obtain
$x+100=2(y-100)$
$\Rightarrow \mathrm{x}+100=2 \mathrm{y}-200$
$\Rightarrow \mathrm{x}-2 \mathrm{y}=-300$
and $6(\mathrm{x}-10)=(\mathrm{y}+10)$
$6 x-60=y+10$
$\Rightarrow 6 \mathrm{x}-\mathrm{y}=70$
Multiplying equation (ii) by 2 \& then subtracting eqeation (i) from it, we obtain:-
$(12 x-2 y)-(x-2 y)=140-(-300)$
$\Rightarrow 11 \mathrm{x}=140+300$
$\Rightarrow 11 \mathrm{x}=440$
$\Rightarrow \mathrm{x}=40$
Putting $x=40$ in equation (i), we obtain
$40-2 y=-300$
$\Rightarrow 40+300=2 \mathrm{y}$
$\Rightarrow 2 \mathrm{y}=340$
$\Rightarrow \mathrm{y}=170$
Therefore, initially they had Rs 40 and Rs 170 with them respectively.
38. Let ABB ' A ' be the friction clutch of slant height l cm .


We have,
$\mathrm{R}=16 \mathrm{~cm}, \mathrm{r}=10 \mathrm{~cm}$ and $\mathrm{h}=8 \mathrm{~cm}$
$\therefore \quad l^{2}=h^{2}+(R-r)^{2}$
$=(8)^{2}+(16-10)^{2}$
$=64+(6)^{2}$
$\Rightarrow \quad l^{2}=64+36 \Rightarrow l=10 \mathrm{~cm}$
Bearing surface of the clutch = Lateral surface of the frustum
$\Rightarrow \quad S=\pi(R+r) l$
$=\frac{22}{7} \times(16+10) \times 10 \mathrm{~cm}^{2}$
$=817.14 \mathrm{~cm}^{2}$
$V=\frac{1}{3} \pi h\left(R^{2}+R r+r^{2}\right)$
$\Rightarrow \quad V=\frac{1}{3} \times \frac{22}{7} \times 8 \times\left(16^{2}+16 \times 10+10^{2}\right) \mathrm{cm}^{3}$
$\Rightarrow \quad V=\frac{1}{3} \times \frac{22}{7} \times 8 \times(256+160+100) \mathrm{cm}^{3}=\frac{176}{21} \times 516 \mathrm{~cm}^{3}$

$$
=4324.57 \mathrm{~cm}^{3}
$$

## OR

Let the sides containing the right angle be x cm and $(\mathrm{x}-14) \mathrm{cm}$.
Then, its area $=\left[\frac{1}{2} \times x \times(x-14)\right] \mathrm{cm}^{2}$.
But according to question it is given that area of a triangle is $120 \mathrm{~cm}^{2}$
$\therefore \quad \frac{1}{2} x(x-14)=120 \Rightarrow x^{2}-14 x-240=0$
$\Rightarrow \quad x^{2}-24 x+10 x-240=0 \Rightarrow x(x-24)+10(x-24)=0$
$\Rightarrow x=24,-10$
$\therefore$ one side $=24 \mathrm{~cm}$, and other side $=(24-14) \mathrm{cm}=10 \mathrm{~cm}$.
hypotenuse $=\sqrt{(24)^{2}+(10)^{2}} \mathrm{~cm}$
$=\sqrt{576+100} \mathrm{~cm}$
$=\sqrt{676} \mathrm{~cm}=26 \mathrm{~cm}$
$\therefore$ perimeter of the triangle $=(24+10+26) \mathrm{cm}=60 \mathrm{~cm}$.
39.


Let us suppose that BC be the height of tower = h m
Suppose DC denotes distance $=\mathrm{x} \mathrm{m}$
Now, in $\triangle B C D$
$\tan 30^{\circ}=\frac{B C}{D C}$
$\Rightarrow \frac{1}{\sqrt{3}}=\frac{h}{x}$
$\Rightarrow x=h \sqrt{3}$
In $\triangle A C D$
$\tan 45^{\circ}=\frac{A C}{D C}$
$\Rightarrow 1=\frac{7+h}{x}$
$\Rightarrow x=7+h$
$\Rightarrow h \sqrt{3}-h=7$ [By Using (i)]
$\Rightarrow h=\frac{7}{\sqrt{3}-1} \times \frac{\sqrt{3}+1}{\sqrt{3}+1}$
$\Rightarrow h=\frac{7(\sqrt{3}+1)}{3-1}$
$\Rightarrow h=\frac{7(1.73+1)}{2}$
$=\frac{19.11}{2}$
$\therefore$ Height of tower $=9.555 \mathrm{~m}$.
Thus, the height of the tower is 9.552 m
40.

| Students | c.f. |
| :---: | :---: |
| Less than 7 | 20 |
|  |  |


| Less than 9 | 38 |
| :---: | :---: |
| Less than 11 | 60 |
| Less than 13 | 85 |
| Less than 15 | 105 |
| Less than 17 | 120 |
| Less than 19 | 130 |

Units: x -axis $1 \mathrm{~cm}=2$; y-axis $1 \mathrm{~cm}=10$


This curve is the required cumulative frequency curve or an ogive of the less than type.
Here, $\mathrm{N}=130$,
So, $\frac{N}{2}=\frac{130}{2}=65$
Now, we locate the point on the ogive whose ordinate is 65 . The $x$-coordinate corresponding to this ordinate is 11.4.

Hence, the required median on the graph is 11.4.

