## Mathematics

(Chapter 3) (Understanding Quadrilaterals)
(Class - VIII)
Exercise 3.1

## Question 1:

Given here are some figures:

(1)

(5)

(2)

(6)

(3)

(7)

(4)

(8)

Classify each of them on the basis of the following:
(a) Simple curve
(b) Simple closed curve
(c) Polygon
(d) Convex polygon
(e) Concave polygon

## Answer 1:

(a) Simple curve

(1)

(2)

(5)

(6)
(7)

(b) Simple closed curve

(1)

(5)

(b)
(7)
(c) Polygons

(1)

(2)

(4)
(d) Convex polygons

(1)
(e) Concave polygon

(1)

(4)

## Question 2:

How many diagonals does each of the following have?
(a) A convex quadrilateral
(b) A regular hexagon
(c) A triangle

Answer 2:
(a) A convex quadrilateral has two diagonals.

Here, AC and BD are two diagonals.

(b) A regular hexagon has 9 diagonals.

Here, diagonals are $\mathrm{AD}, \mathrm{AE}, \mathrm{BD}, \mathrm{BE}, \mathrm{FC}, \mathrm{FB}, \mathrm{AC}, \mathrm{EC}$ and FD .
(c) A triangle has no diagonal.


## Question 3:

What is the sum of the measures of the angles of a convex quadrilateral? Will this property hold if the quadrilateral is not convex? (Make a non-convex quadrilateral and try)

## Answer 3:

Let $A B C D$ is a convex quadrilateral, then we draw a diagonal $A C$ which divides the quadrilateral in two triangles.

$$
\begin{aligned}
& \angle \mathrm{A}+\mathrm{B}+\angle \mathrm{C}+\angle \mathrm{D}=\angle 1+\angle 6+\angle 5+\angle 4+\angle 3+\angle 2 \\
& =(\angle 1+\angle 2+\angle 3)+(\angle 4+\angle 5+\angle 6) \\
& =180^{\circ}+180^{\circ} \quad \text { [By Angle sum property of triangle] } \\
& =360^{\circ} \quad
\end{aligned}
$$

Hence, the sum of measures of the triangles of a convex quadrilateral is $360^{\circ}$.
Yes, if quadrilateral is not convex then, this property will also be applied.


Let ABCD is a non-convex quadrilateral and join BD , which also divides the quadrilateral in two triangles.

Using angle sum property of triangle,
In $\triangle \mathrm{ABD}, \quad \angle 1+\angle 2+\angle 3=180^{\circ} \square$ (i)
In $\triangle \mathrm{BDC}, \quad \angle 4+\angle 5+\angle 6=180^{\circ} \square$ (i)
Adding eq. (i) and (ii),

$$
\begin{array}{ll} 
& \angle 1+\angle 2+\angle 3+\angle 4+\angle 5+\angle 6=360^{\circ} \\
\Rightarrow & \angle 1+\angle 2+(\angle 3+\angle 4)+\angle 5+\angle 6=360^{\circ} \\
\Rightarrow & \angle \mathrm{A}+\angle \mathrm{B}+\angle \mathrm{C}+\angle \mathrm{D}=360^{\circ}
\end{array}
$$

Hence proved.


## Question 4:

Examine the table. (Each figure is divided into triangles and the sum of the angles deduced from that.)

| Figure |  |  |  |
| :--- | :---: | :---: | :---: |
| Side | 3 | 4 | 5 |

What can you say about the angle sum of a convex polygon with number of sides?
Answer 4:
(a) When $n=7$, then

Angle sum of a polygon $=(n-2) \times 180^{\circ}=(7-2) \times 180^{\circ}=5 \times 180^{\circ}=900^{\circ}$
(b) When $n=8$, then

Angle sum of a polygon $=(n-2) \times 180^{\circ}=(8-2) \times 180^{\circ}=6 \times 180^{\circ}=1080^{\circ}$
(c) When $n=10$, then

Angle sum of a polygon $=(n-2) \times 180^{\circ}=(10-2) \times 180^{\circ}=8 \times 180^{\circ}=1440^{\circ}$
(d) When $n=n$, then

Angle sum of a polygon $=(n-2) \times 180^{\circ}$


## Question 5:

What is a regular polygon? State the name of a regular polygon of:
(a) 3 sides
(b) 4 sides
(c) 6 sides

Answer 5:
A regular polygon: A polygon having all sides of equal length and the interior angles of equal size is known as regular polygon.
(i) 3 sides

Polygon having three sides is called a triangle.
(ii) 4 sides

Polygon having four sides is called a quadrilateral.
(iii) 6 sides

Polygon having six sides is called a hexagon.

## Question 6:

Find the angle measures $x$ in the following figures:

(a)

(c)

(b)

(d)


## Answer 6:

(a) Using angle sum property of a quadrilateral,

$$
\begin{array}{ll} 
& 50^{\circ}+130^{\circ}+120^{\circ}+x=360^{\circ} \\
\Rightarrow & 300^{\circ}+x=360^{\circ} \\
\Rightarrow & x=360^{\circ}-300^{\circ} \\
\Rightarrow & x=60^{\circ}
\end{array}
$$


(a)

(b)
(c) First base interior angle $=180^{\circ}-70^{\circ}=110^{\circ}$

Second base interior angle $=180^{\circ}-60^{\circ}=120^{\circ}$ There are 5 sides, $n=5$

$$
\therefore \quad \text { Angle sum of a polygon }=(n-2) \times 180^{\circ}
$$

$$
\begin{aligned}
& =(5-2) \times 180^{\circ}=3 \times 180^{\circ}=540^{\circ} \\
\therefore \quad & 30^{\circ}+x+110^{\circ}+120^{\circ}+x=540^{\circ}
\end{aligned}
$$

$$
\Rightarrow \quad 260^{\circ}+2 x=540^{\circ}
$$

$$
\Rightarrow \quad 2 x=540^{\circ}-260^{\circ}
$$

$$
\Rightarrow \quad 2 x=280^{\circ}
$$

$$
\Rightarrow \quad x=140^{\circ}
$$

(d) Angle sum of a polygon $=(n-2) \times 180^{\circ}$

$$
\begin{aligned}
& =(5-2) \times 180^{\circ}=3 \times 180^{\circ}=540^{\circ} \\
& \therefore \quad x+x+x+x+x=540^{\circ} \\
& \Rightarrow \quad 5 x=540^{\circ} \\
& \Rightarrow \quad x=108^{\circ}
\end{aligned}
$$


(d)

Hence each interior angle is $108^{\circ}$.


## Question 7:

(a) Find $x+y+z$
(b) Find $x+y+z+w$


## Answer 7:

(a) Since sum of linear pair angles is $180^{\circ}$.

$$
\begin{array}{ll}
\therefore & 90^{\circ}+x=180^{\circ} \\
\Rightarrow & x=180^{\circ}-90^{\circ}=90^{\circ} \\
\text { And } & z+30^{\circ}=180^{\circ} \\
\Rightarrow & z=180^{\circ}-30^{\circ}=150^{\circ} \\
\text { Also } \quad y=90^{\circ}+30^{\circ}=120^{\circ}
\end{array}
$$

[Exterior angle property]
$\therefore x+y+x=90^{\circ}+120^{\circ}+150^{\circ}=360^{\circ}$
(b) Using angle sum property of a quadrilateral,

$$
\begin{aligned}
& 60^{\circ}+80^{\circ}+120^{\circ}+n=360^{\circ} \\
& \Rightarrow \quad 260^{\circ}+n=360^{\circ} \\
& \Rightarrow \quad n=360^{\circ}-260^{\circ} \\
& \Rightarrow \quad n=100^{\circ}
\end{aligned}
$$

Since sum of linear pair angles is $180^{\circ}$.

$\therefore \quad w+100=180^{\circ} \square(\mathrm{i})$
$x+120^{\circ}=180^{\circ} \square$
$y+80^{\circ}=180^{\circ} \square$ (iii)
$z+60^{\circ}=180^{\circ} \square$ (iv)
Adding eq. (i), (ii), (iii) and (iv),
$\Rightarrow \quad x+y+z+w+100^{\circ}+120^{\circ}+80^{\circ}+60^{\circ}=180^{\circ}+180^{\circ}+180^{\circ}+180^{\circ}$
$\Rightarrow \quad x+y+z+w+360^{\circ}=720^{\circ}$
$\Rightarrow \quad x+y+z+w=720^{\circ}-360^{\circ}$
$\Rightarrow \quad x+y+z+w=360^{\circ}$


## Exercise 3.2

## Question 1:

Find $x$ in the following figures:

(a)

(b)

## Answer 1:

(a) Here, $125^{\circ}+m=180^{\circ}$
[Linear pair]

$$
\begin{array}{lll}
\Rightarrow & m=180^{\circ}-125^{\circ}=55^{\circ} & \\
\text { and } & 125^{\circ}+n=180^{\circ} & \text { [Linear pair] } \\
\Rightarrow & n=180^{\circ}-125^{\circ}=55^{\circ} &
\end{array}
$$

$\because \quad$ Exterior angle $x^{\circ}=$ Sum of opposite interior angles

$\therefore \quad x^{\circ}=55^{\circ}+55^{\circ}=110^{\circ}$
(b) Sum of angles of a pentagon $=(n-2) \times 180^{\circ}$

$$
\begin{aligned}
& =(5-2) \times 180^{\circ} \\
& =3 \times 180^{\circ}=540^{\circ}
\end{aligned}
$$

By linear pairs of angles,

$$
\begin{aligned}
& \angle 1+90^{\circ}=180^{\circ} \square \text { (i) } \\
& \angle 2+60^{\circ}=180^{\circ} \square \text { (ii) } \\
& \angle 3+90^{\circ}=180^{\circ} \square \text { (iii) } \\
& \angle 4+70^{\circ}=180^{\circ} \square \text { (iv) } \\
& \angle 5+x=180^{\circ} \square \text { (v) } \\
& \text { Adding eq. (i), (ii), (iii), (iv) and (v), } \\
& x+(\angle 1+\angle 2+\angle 3+\angle 4+\angle 5)+310^{\circ}=900 \\
& \Rightarrow \quad x+540^{\circ}+310^{\circ}=900^{\circ} \\
& \Rightarrow \quad x+850^{\circ}=900^{\circ} \\
& \Rightarrow \quad x=900^{\circ}-850^{\circ}=50^{\circ}
\end{aligned}
$$



## Question 2:

Find the measure of each exterior angle of a regular polygon of:
(a) 9 sides
(b) 15 sides

## Answer 2:

(i) Sum of angles of a regular polygon $=(n-2) \times 180^{\circ}$

$$
=(9-2) \times 180^{\circ}=7 \times 180^{\circ}=1260^{\circ}
$$

Each interior angle $=\frac{\text { Sum of interior angles }}{\text { Number of sides }}=\frac{1260^{\circ}}{9}=140^{\circ}$
Each exterior angle $=180^{\circ}-140^{\circ}=40^{\circ}$
(ii) Sum of exterior angles of a regular polygon $=360^{\circ}$

$$
\text { Each interior angle }=\frac{\text { Sum of interior angles }}{\text { Number of sides }}=\frac{360^{\circ}}{15}=24^{\circ}
$$

## Question 3:

How many sides does a regular polygon have, if the measure of an exterior angle is $24^{\circ}$ ?

## Answer 3:

Let number of sides be $n$.

> Sum of exterior angles of a regular polygon $=360^{\circ}$
> Number of sides $=\frac{\text { Sum of exterior angles }}{\text { Each interior angle }}=\frac{360^{\circ}}{24^{\circ}}=15$

Hence, the regular polygon has 15 sides.

## Question 4:

How many sides does a regular polygon have if each of its interior angles is $165^{\circ}$ ?

## Answer 4:

Let number of sides be $n$.

$$
\begin{aligned}
& \text { Exterior angle }=180^{\circ}-165^{\circ}=15^{\circ} \\
& \text { Sum of exterior angles of a regular polygon }=360^{\circ} \\
& \text { Number of sides }=\frac{\text { Sum of exterior angles }}{\text { Each interior angle }}=\frac{360^{\circ}}{15^{\circ}}=24
\end{aligned}
$$

Hence, the regular polygon has 24 sides.


## Question 5:

(a) Is it possible to have a regular polygon with of each exterior angle as $22^{\circ}$ ?
(b) Can it be an interior angle of a regular polygon? Why?

Answer 5:
(a) No. (Since 22 is not a divisor of $360^{\circ}$ )
(b) No, (Because each exterior angle is $180^{\circ}-22^{\circ}=158^{\circ}$, which is not a divisor of $360^{\circ}$ )

## Question 6:

(a) What is the minimum interior angle possible for a regular polygon? Why?
(b) What is the maximum exterior angle possible for a regular polygon?

Answer 6:
(a) The equilateral triangle being a regular polygon of 3 sides has the least measure of an interior angle of $60^{\circ}$.
$\because \quad$ Sum of all the angles of a triangle $=180^{\circ}$
$\therefore \quad x+x+x=180^{\circ}$
$\Rightarrow \quad 3 x=180^{\circ}$
$\Rightarrow \quad x=60^{\circ}$
(b) By (a), we can observe that the greatest exterior angle is $180^{\circ}-60^{\circ}=120^{\circ}$.


## Exercise 3.3

## Question 1:

Given a parallelogram ABCD. Complete each statement along with the definition or property used.
(i) $\mathrm{AD}=$ $\qquad$
(ii) $\angle \mathrm{DCB}=$ $\qquad$
(iii) $\mathrm{OC}=$ $\qquad$

(iv) $m \angle \mathrm{DAB}+m \angle \mathrm{CDA}=$ $\qquad$

## Answer 1:

(i) $\mathrm{AD}=\mathrm{BC} \quad$ [Since opposite sides of a parallelogram are equal]
(ii) $\quad \angle \mathrm{DCB}=\angle \mathrm{DAB} \quad$ [Since opposite angles of a parallelogram are equal]
(iii) $\quad \mathrm{OC}=\mathrm{OA} \quad$ [Since diagonals of a parallelogram bisect each other]
(iv) $m \angle \mathrm{DAB}+m \angle \mathrm{CDA}=180^{\circ}$
[Adjacent angles in a parallelogram are supplementary]

## Question 2:

Consider the following parallelograms. Find the values of the unknowns $x, y, z$.

(i)

(ii)

(iv)

(v)

Note: For getting correct answer, read $3^{\circ}=30^{\circ}$ in figure (iii)


## Answer 2:

(i)
$\angle \mathrm{B}+\angle \mathrm{C}=180^{\circ}$ [Adjacent angles in a parallelogram are supplementary]
$\Rightarrow \quad 100^{\circ}+x=180^{\circ}$
$\Rightarrow \quad x=180^{\circ}-100^{\circ}=80^{\circ}$

and $z=x=80^{\circ} \quad$ [Since opposite angles of a parallelogram are equal] also $y=100^{\circ} \quad$ [Since opposite angles of a parallelogram are equal]
(ii) $x+50^{\circ}=180^{\circ} \quad$ [Adjacent angles in a ||gm are supplementary]


$$
\Rightarrow \quad x=180^{\circ}-50^{\circ}=130^{\circ}
$$

$\Rightarrow \quad z=x=130^{\circ}$
[Corresponding angles]
(iii) ( $\quad x=90^{\circ}$
[Vertically opposite angles]
$\begin{aligned} \mathrm{i} \\ \mathrm{i} \\ \mathrm{i} \\ \mathrm{i}\end{aligned} \mathrm{A} \quad y+x+30^{\circ}=180^{\circ}$
[Angle sum property of a triangle]
(iv) $z=80^{\circ}$
[Corresponding angles]
$\Rightarrow \quad x+80^{\circ}=180^{\circ}$
[Adjacent angles in a ||gm are supplementary]
[Alternate angles]

$$
0
$$

$$
\Rightarrow \quad x=180^{\circ}-80^{\circ}=100^{\circ}
$$


and $y=80^{\circ} \quad$ [Opposite angles are equal in a $|\mid \mathrm{gm}$ ]

$$
\sum[2]
$$


(v)

$$
\begin{array}{ll}
y=112^{\circ} & \text { [Opposite angles are equal in a \|gm] } \\
\Rightarrow & 40^{\circ}+y+x=180^{\circ} \\
\Rightarrow & 40^{\circ}+112^{\circ}+x=180^{\circ} \\
\Rightarrow & 152^{\circ}+x=180^{\circ} \\
\text { [Angle sum property of a triangle] } \\
\Rightarrow \quad & x=180^{\circ}-152^{\circ}=28^{\circ} \\
\text { and } \quad z=x=28^{\circ} \quad \text { [Alternate angles] }
\end{array}
$$

## Question 3:

Can a quadrilateral ABCD be a parallelogram, if:
(i) $\angle \mathrm{D}+\angle \mathrm{B}=180^{\circ}$ ?
(ii) $\mathrm{AB}=\mathrm{DC}=8 \mathrm{~cm}, \mathrm{AD}=4 \mathrm{~cm}$ and $\mathrm{BC}=4.4 \mathrm{~cm}$ ?
(iii) $\angle \mathrm{A}=70^{\circ}$ and $\angle \mathrm{C}=65^{\circ}$ ?

Answer 3:
(i)
$\angle \mathrm{D}+\angle \mathrm{B}=180^{\circ}$
It can be, but here, it needs not to be.

(ii) No, in this case because one pair of opposite sides are equal and another pair of opposite sides are unequal. So, it is not a parallelogram.

(iii) No. $\angle \mathrm{A} \neq \angle \mathrm{C}$.

Since opposite angles are equal in parallelogram and here opposite angles are not equal in quadrilateral ABCD . Therefore it is not a parallelogram.


## Question 4:

Draw a rough figure of a quadrilateral that is not a parallelogram but has exactly two opposite angles of equal measures.

## Answer 4:

ABCD is a quadrilateral in which angles $\angle \mathrm{A}=\angle \mathrm{C}=110^{\circ}$.

Therefore, it could be a kite.


## Question 5:

The measure of two adjacent angles of a parallelogram are in the ratio 3:2. Find the measure of each of the angles of the parallelogram.

## Answer 5:

Let two adjacent angles be $3 x$ and $2 x$.
Since the adjacent angles in a parallelogram are supplementary.

$$
\begin{array}{ll}
\therefore & 3 x+2 x=180^{\circ} \\
\Rightarrow & 5 x=180^{\circ} \\
\Rightarrow & x=\frac{180^{\circ}}{5}=36^{\circ}
\end{array}
$$


$\therefore \quad$ One angle $\quad=3 x=3 \times 36^{\circ}=108^{\circ}$
and another angle $=2 x=2 \times 36^{\circ}=72^{\circ}$

## Question 6:

Two adjacent angles of a parallelogram have equal measure. Find the measure of the angles of the parallelogram.

## Answer 6:

Let each adjacent angle be $x$.
Since the adjacent angles in a parallelogram are supplementary.

$$
\begin{array}{ll}
\therefore & x+x=180^{\circ} \\
\Rightarrow & 2 x=180^{\circ}
\end{array}
$$



$$
\Rightarrow \quad x=\frac{180^{\circ}}{2}=90^{\circ}
$$

Hence, each adjacent angle is $90^{\circ}$.

$$
\begin{array}{ll}
\therefore & x+x+x=180^{\circ} \\
\Rightarrow & 3 x=180^{\circ} \\
\Rightarrow & x=60^{\circ}
\end{array}
$$

## Question 7:

The adjacent figure HOPW is a parallelogram. Find the angle measures $x, y$ and $z$. State the properties you use to find them.


## Answer 7:

Here $\angle \mathrm{HOP}+70^{\circ}=180^{\circ}$
[Angles of linear pair]
$\angle \mathrm{HOP}=180^{\circ}-70^{\circ}=110^{\circ}$
and $\quad \angle \mathrm{E}=\angle \mathrm{HOP}$
[Opposite angles of a ||gm are equal]

$$
\Rightarrow \quad x=110^{\circ}
$$


$\angle \mathrm{PHE}=\angle \mathrm{HPO}$
[Alternate angles]
$\therefore \quad y=40^{\circ}$
Now $\quad \angle \mathrm{EHO}=\angle \mathrm{O}=70^{\circ}$ [Corresponding angles]
$\Rightarrow \quad 40^{\circ}+z=70^{\circ}$
$\Rightarrow \quad z=70^{\circ}-40^{\circ}=30^{\circ}$
Hence, $\quad x=110^{\circ}, y=40^{\circ}$ and $z=30^{\circ}$


## Question 8:

The following figures GUNS and RUNS are parallelograms. Find $x$ and $y$. (Lengths are in cm)
(i)

(ii)


## Answer 8:

(i) In parallelogram GUNS,

$$
\begin{array}{lll} 
& \mathrm{GS}=\mathrm{UN} & \text { [Opposite sides of parallelogram are equal] } \\
\Rightarrow & 3 x=18 & \\
\Rightarrow & x=\frac{18}{3}=6 \mathrm{~cm} & \\
\text { Also } & \mathrm{GU}=\mathrm{SN} & \text { [Opposite sides of parallelogram are equal] } \\
\Rightarrow & 3 y-1=26 & \\
\Rightarrow & 3 y=26+1 & \\
\Rightarrow & 3 y=27 & \\
\Rightarrow & y=\frac{27}{3}=9 \mathrm{~cm} &
\end{array}
$$

Hence, $x=6 \mathrm{~cm}$ and $y=9 \mathrm{~cm}$.
(ii) In parallelogram RUNS,

$$
\begin{array}{ll}
y+7= & 20 \quad \text { [Diagonals of } \| \mathrm{gm} \text { bisects each other] } \\
\Rightarrow & y=20-7=13 \mathrm{~cm} \\
\text { and } & x+y=16 \\
\Rightarrow & x+13=16 \\
\Rightarrow & x=16-13 \\
\Rightarrow & x=3 \mathrm{~cm} \\
\text { Hence, } x=3 \mathrm{~cm} \text { and } y=13 \mathrm{~cm} .
\end{array}
$$



## Question 9:

In the figure, both RISK and CLUE are parallelograms. Find the value of $x$.


## Answer 9:

In parallelogram RISK,

$$
\angle \mathrm{RIS}=\angle \mathrm{K}=120^{\circ}
$$

[Opposite angles of a ||gm are equal]


$$
\begin{array}{ll}
\angle m+120^{\circ}=180^{\circ} \\
\Rightarrow & \angle m=180^{\circ}-120^{\circ}=60^{\circ} \\
\text { and } & \angle \mathrm{ECI}=\angle \mathrm{L}=70^{\circ} \\
\Rightarrow & m+n+\angle \mathrm{ECI}=180^{\circ} \\
\Rightarrow & 60^{\circ}+n+70^{\circ}=180^{\circ} \\
\Rightarrow & 130^{\circ}+n=180^{\circ} \\
\Rightarrow & n=180^{\circ}-130^{\circ}=50^{\circ}
\end{array}
$$

[Linear pair]
[Corresponding angles]

$$
\Rightarrow \quad m+n+\angle \mathrm{ECI}=180^{\circ} \quad \text { [Angle sum property of a triangle] }
$$

$$
\text { also } \quad x=n=50^{\circ} \quad \text { [Vertically opposite angles] }
$$



## Question 10:

Explain how this figure is a trapezium. Which is its two sides are parallel?


## Answer 10:

Here, $\quad \angle \mathrm{M}+\angle \mathrm{L}=100^{\circ}+80^{\circ}=180^{\circ}$ [Sum of interior opposite angles is $180^{\circ}$ ] $\therefore \quad \mathrm{NM}$ and KL are parallel.

Hence, KLMN is a trapezium.


## Question 11:

1. Find $m \angle \mathrm{C}$ in figure , if $\bar{A} \| \bar{D}$,


Answer 11:
Here, $\quad \angle \mathrm{B}+\angle \mathrm{C}=180^{\circ} \quad[\because \overline{A B}| | \bar{D}]$


$$
\begin{array}{ll}
\therefore & 120^{\circ}+m \angle \mathrm{C}=180^{\circ} \\
\Rightarrow & m \angle \mathrm{C}=180^{\circ}-120^{\circ}=60^{\circ}
\end{array}
$$

## Question 12:

Find the measure of $\angle \mathrm{P}$ and $\angle \mathrm{S}$ if $S P \| R Q$ in given figure.
(If you find $m \angle \mathrm{R}$ is there more than one method to find $m \angle \mathrm{P}$ )


## Answer 12:

Here, $\angle \mathrm{P}+\angle \mathrm{Q}=180^{\circ}$
[Sum of co-interior angles is $180^{\circ}$ ]

$$
\begin{array}{ll}
\Rightarrow & \angle \mathrm{P}+130^{\circ}=180^{\circ} \\
\Rightarrow & \angle \mathrm{P}=180^{\circ}-130^{\circ} \\
\Rightarrow & \angle \mathrm{P}=50^{\circ} \\
\because & \angle \mathrm{R}=90^{\circ} \\
\therefore & \angle \mathrm{S}+90^{\circ}=180^{\circ} \\
\Rightarrow & \angle \mathrm{S}=180^{\circ}-90^{\circ} \\
\Rightarrow & \angle \mathrm{S}=90^{\circ}
\end{array}
$$

$$
\because \quad \angle \mathrm{R}=90^{\circ} \quad[\text { Given }]
$$

Yes, one more method is there to find $\angle \mathrm{P}$.

$$
\begin{aligned}
& \angle \mathrm{S}+\angle \mathrm{R}+\angle \mathrm{Q}+\angle \mathrm{P}=360^{\circ} \quad \text { [Angle sum property of quadrilateral] } \\
& \Rightarrow \quad 90^{\circ}+90^{\circ}+130^{\circ}+\angle \mathrm{P}=360^{\circ} \\
& \Rightarrow \quad 310^{\circ}+\angle \mathrm{P}=360^{\circ} \\
& \Rightarrow \quad \angle \mathrm{P}=360^{\circ}-310^{\circ} \\
& \Rightarrow \quad \angle \mathrm{P}=50^{\circ}
\end{aligned}
$$

## Exercise 3.4

## Question 1:

State whether true or false:
(a) All rectangles are squares.
(b) All rhombuses are parallelograms.
(c) All squares are rhombuses and also rectangles.
(d) All squares are not parallelograms.
(e) All kites are rhombuses.
(f) All rhombuses are kites.
(g) All parallelograms are trapeziums.
(h) All squares are trapeziums.

Answer 1:
(a) False. Since, squares have all sides are equal.
(b) True. Since, in rhombus, opposite angles are equal and diagonals intersect at mid-point.
(c) True. Since, squares have the same property of rhombus but not a rectangle.
(d) False. Since, all squares have the same property of parallelogram.
(e) False. Since, all kites do not have equal sides.
(f) True
(g) True. Since, trapezium has only two parallel sides.
(h) True. Since, all squares have also two parallel lines.

## Question 2:

Identify all the quadrilaterals that have:
(a) four sides of equal lengths.
(b) four right angles.

## Answer 2:

(a) Rhombus and square have sides of equal length.
(b) Square and rectangle have four right angles.


## Question 3:

Explain how a square is:
(i) a quadrilateral
(ii) a parallelogram
(iii) a rhombus
(iv) a rectangle

## Answer 3:

(i) A square is a quadrilateral, if it has four unequal lengths of sides.
(ii) A square is a parallelogram, since it contains both pairs of opposite sides equal.
(iii) A square is already a rhombus. Since, it has four equal sides and diagonals bisect at 90 to each other.
(iv) A square is a parallelogram, since having each adjacent angle a right angle and opposite sides are equal.

## Question 4:

Name the quadrilateral whose diagonals:
(i) bisect each other.
(ii) are perpendicular bisectors of each other.
(iii) are equal.

## Answer 4:

(i) If diagonals of a quadrilateral bisect each other then it is a rhombus, parallelogram, rectangle or square.
(ii) If diagonals of a quadrilateral are perpendicular bisector of each other, then it is a rhombus or square.
(iii) If diagonals are equal, then it is a square or rectangle.

## Question 5:

Explain why a rectangle is a convex quadrilateral.

## Answer 5:

A rectangle is a convex quadrilateral since its vertex are raised and both of its diagonals lie in its interior.


## Question 6:

$A B C$ is a right-angled triangle and 0 is the mid-point of the side opposite to the right angle. Explain why 0 is equidistant from A, B and C. (The dotted lines are drawn additionally to help you.)


## Answer 6:

Since, two right triangles make a rectangle where 0 is equidistant point from A, B, C and $D$ because 0 is the mid-point of the two diagonals of a rectangle.

Since AC and BD are equal diagonals and intersect at mid-point.
So, 0 is the equidistant from A, B, C and D.


