Mathematics

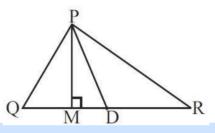
(Chapter – 6) (The Triangle and its Properties) (Class – VII)

Exercise 6.1

Question 1:

In \triangle PQR, D is the mid-point of QR.

PM is PD is _____ Is QM = MR?



Answer 1:

Given: QD = DR \therefore PM is altitude. PD is median. No, $QM \neq MR$ as D is the mid-point of QR.

Question 2:

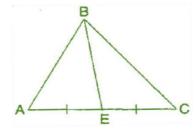
Draw rough sketches for the following:

(a) In \triangle ABC, BE is a median.

- (b) In \triangle PQR, PQ and PR are altitudes of the triangle.
- (c) In Δ XYZ, YL is an altitude in the exterior of the triangle.

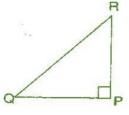
Answer 2:

(a) Here, BE is a median in $\triangle ABC$ and AE = EC.





(b) Here, PQ and PR are the altitudes of the Δ PQR and RP \perp QP.



(c) YL is an altitude in the exterior of \triangle XYZ.

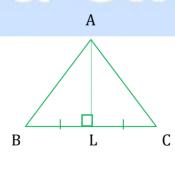
Question 3:

Verify by drawing a diagram if the median and altitude of a isosceles triangle can be same.

Answer 3:

Isosceles triangle means any two sides are same. Take \triangle ABC and draw the median when AB = AC.

AL is the median and altitude of the given triangle.

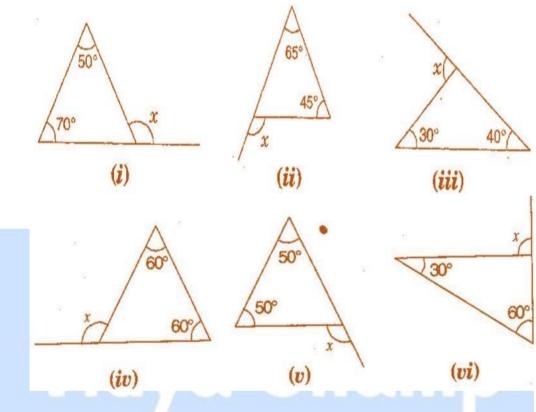




Exercise 6.2

Question 1:

Find the value of the unknown exterior angle *x* in the following diagrams:



Answer 1:

Since, Exterior angle = Sum of interior opposite angles, therefore

- (i) $x = 50^{\circ} + 70^{\circ} = 120^{\circ}$
- (ii) $x = 65^{\circ} + 45^{\circ} = 110^{\circ}$
- (iii) $x = 30^{\circ} + 40^{\circ} = 70^{\circ}$
- (iv) $x = 60^\circ + 60^\circ = 120^\circ$
- (v) $x = 50^{\circ} + 50^{\circ} = 100^{\circ}$

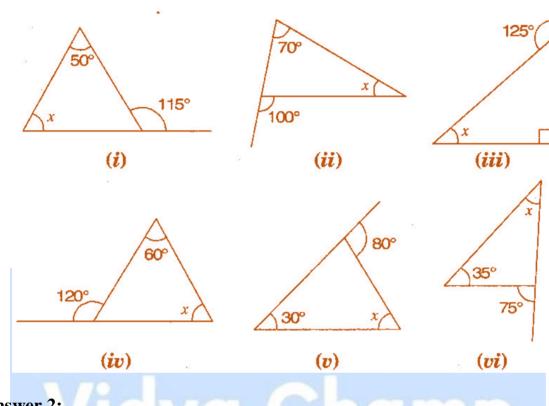
(vi)
$$x = 60^{\circ} + 30^{\circ} = 90^{\circ}$$



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Question 2:

Find the value of the unknown interior angle *x* in the following figures:



Answer 2:

Since, Exterior angle = Sum of interior opposite angles, therefore

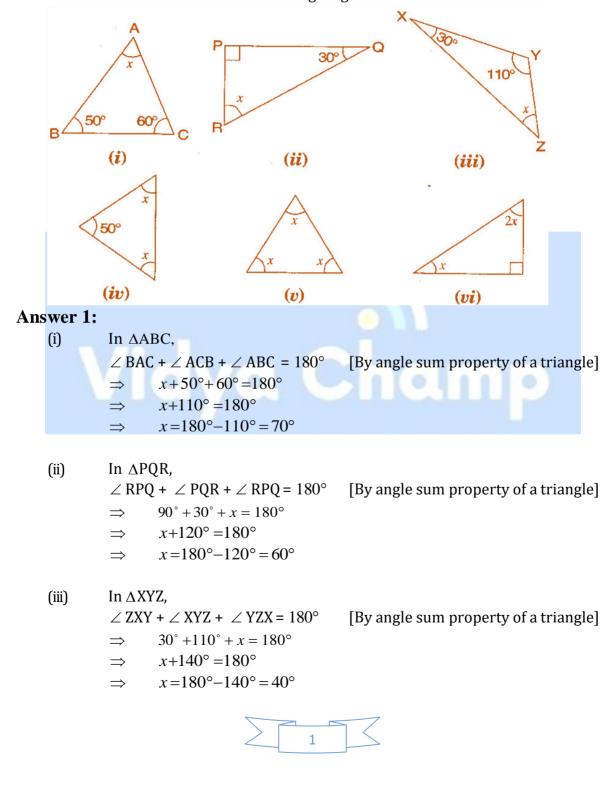
(i)	$x + 50^{\circ} = 115^{\circ}$	⇒	$x = 115^{\circ} - 50^{\circ} = 65^{\circ}$
(ii)	$70^{\circ}+x=100^{\circ}$	\Rightarrow	$x = 100^{\circ} - 70^{\circ} = 30^{\circ}$
(iii)	$x + 90^{\circ} = 125^{\circ}$	\Rightarrow	$x = 120^{\circ} - 90^{\circ} = 35^{\circ}$
(iv)	$60^{\circ}+x=120^{\circ}$	\Rightarrow	$x = 120^{\circ} - 60^{\circ} = 60^{\circ}$
(v)	$30^{\circ}+x = 80^{\circ}$	\Rightarrow	$x = 80^{\circ} - 30^{\circ} = 50^{\circ}$
(vi)	$x + 35^\circ = 75^\circ$	\Rightarrow	$x = 75^{\circ} - 35^{\circ} = 40^{\circ}$



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Exercise 6.3

Question 1: Find the value of unknown *x* in the following diagrams:



(iv) In the given isosceles triangle, $x+x+50^\circ = 180^\circ$

- $\Rightarrow 2x + 50^{\circ} = 180^{\circ}$ $\Rightarrow 2x = 180^{\circ} 50^{\circ}$
- $\Rightarrow 2x = 130^{\circ}$

$$\Rightarrow \qquad x = \frac{130^{\circ}}{2} = 65^{\circ}$$

(v) In the given equilateral triangle, $x + x + x = 180^{\circ}$ [By $\Rightarrow 3x = 180^{\circ}$ $\Rightarrow x = \frac{180^{\circ}}{3} = 60^{\circ}$

[By angle sum property of a triangle]

[By angle sum property of a triangle]

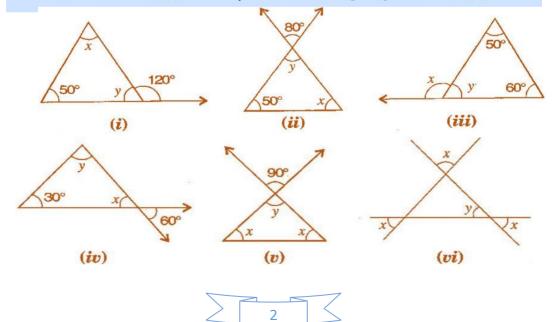
(vi) In the given right angled triangle, $r + 2r + 90^\circ - 180^\circ$

$$\Rightarrow 3x + 90^{\circ} = 180^{\circ}$$
$$\Rightarrow 3x + 90^{\circ} = 180^{\circ}$$
$$\Rightarrow 3x = 180^{\circ} - 90^{\circ}$$
$$\Rightarrow 3x = 90^{\circ}$$
$$\Rightarrow x = \frac{90^{\circ}}{3} = 30^{\circ}$$

[By angle sum property of a triangle]

Question 2:

Find the values of the unknowns *x* and *y* in the following diagrams:



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Answer 2: (i)	$50^{\circ} + x = 120^{\circ}$ $\Rightarrow x = 120^{\circ} - 50^{\circ} = 70^{\circ}$ Now, $50^{\circ} + x + y = 180^{\circ}$ $\Rightarrow 50^{\circ} + 70^{\circ} + y = 180^{\circ}$ $\Rightarrow 120^{\circ} + y = 180^{\circ}$ $\Rightarrow y = 180^{\circ} - 120^{\circ} = 60^{\circ}$	[Exterior angle property of a Δ] [Angle sum property of a Δ]			
(ii)	$y = 80^{\circ} \qquad \dots \dots (i)$ Now, $50^{\circ} + x + y = 180^{\circ}$ $\Rightarrow \qquad 50^{\circ} + 80^{\circ} + y = 180^{\circ}$ $\Rightarrow \qquad 130^{\circ} + y = 180^{\circ}$ $\Rightarrow \qquad y = 180^{\circ} - 130^{\circ} = 50^{\circ}$	[Vertically opposite angle] [Angle sum property of a ∆] [From equation (i)]			
(iii)	$50^\circ + 60^\circ = x$	[Exterior angle property of a Δ]			
(iv)	$\Rightarrow x = 110^{\circ}$ Now $50^{\circ} + 60^{\circ} + y = 180^{\circ}$ $\Rightarrow 110^{\circ} + y = 180^{\circ}$ $\Rightarrow y = 180^{\circ} - 110^{\circ}$ $\Rightarrow y = 70^{\circ}$ $x = 60^{\circ} \qquad \dots \dots (i)$ Now, $30^{\circ} + x + y = 180^{\circ}$ $\Rightarrow 50^{\circ} + 60^{\circ} + y = 180^{\circ}$ $\Rightarrow 90^{\circ} + y = 180^{\circ}$ $\Rightarrow y = 180^{\circ} - 90^{\circ} = 90^{\circ}$	[Angle sum property of a Δ] [Vertically opposite angle] [Angle sum property of a Δ] [From equation (i)]			
(v)	$y = 90^{\circ} \qquad \dots \dots (i)$ Now, $y + x + x = 180^{\circ}$ $\Rightarrow \qquad 90^{\circ} + 2x = 180^{\circ}$ $\Rightarrow \qquad 2x = 180^{\circ} - 90^{\circ}$ $\Rightarrow \qquad 2x = 90^{\circ}$ $\Rightarrow \qquad x = \frac{90^{\circ}}{2} = 45^{\circ}$	[Vertically opposite angle] [Angle sum property of a ∆] [From equation (i)]			
3					

(vi) x = y(i) Now, $x + x + y = 180^{\circ}$ $\Rightarrow 2x + x = 180^{\circ}$ $\Rightarrow 3x = 180^{\circ}$ $\Rightarrow x = \frac{180^{\circ}}{3} = 60^{\circ}$ [Vertically opposite angle][Angle sum property of a ∆][From equation (i)]





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Exercise 6.4

Question 1:

Is it possible to have a triangle with the following sides?

- (i) 2 cm, 3 cm, 5 cm
- (ii) 3 cm, 6 cm, 7 cm
- (iii) 6 cm, 3 cm, 2 cm

Answer 1:

Since, a triangle is possible whose sum of the lengths of any two sides would be greater than the length of third side.

(i) 2 cm, 3 cm,	5 cm	(ii) 3 cm, 6 cm, 7 cm	
2 + 3 > 5	No	3 + 6 > 7	Yes
2 + 5 > 3	Yes	6 + 7 > 3	Yes
3 + 5 > 2	Yes	3 + 7 > 6	Yes
This triangle is not possible.		This triangle is possible.	

(iii) 6 cm, 3 cm, 2 cm 6 + 3 > 2 Yes 6 + 2 > 3 Yes 2 + 3 > 6 No

This triangle is not possible.

Question 2:

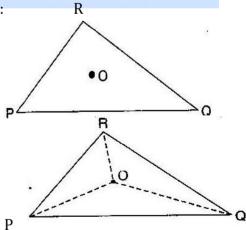
Take any point O in the interior of a triangle PQR. Is:

- (i) OP + OQ > PQ?
- (ii) OQ + OR > QR?
- (iii) OR + OP > RP?

Answer 2:

Join OR, OQ and OP.

- (i) Is OP + OQ > PQ ? Yes, POQ form a triangle.
- (ii) Is OQ + OR > QR ?Yes, RQO form a triangle.
- (iii) Is OR + OP > RP ?Yes, ROP form a triangle.

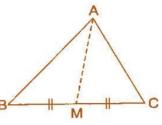




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Question 3:

AM is a median of a triangle ABC. Is AB + BC + CA > 2AM? (Consider the sides of triangles \triangle ABM and \triangle AMC.)



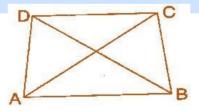
Answer 3:

Since, the sum of lengths of any two sides in a triangle should be greater than the length of third side.

Therefore,	In ∆ABM,	AB + BM > AM	(i)			
	In ∆AMC,	AC + MC > AM	(ii)			
Adding eq. (i) and (ii),						
AB + BM + AC + MC > AM + AM						
\Rightarrow	AB + AC + (B	3M + MC) > 2AM				
\Rightarrow	AB + AC + BC	C > 2AM				
Hence, it is true.						

Question 4:

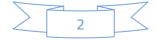
ABCD is a quadrilateral. Is AB + BC + CD + DA > AC + BD?



Answer 4:

Since, the sum of lengths of any two sides in a triangle should be greater than the length of third side.

Therefore, In $\triangle ABC$, AB + BC > AC.....(i) In $\triangle ADC$, AD + DC > AC.....(ii) In $\triangle DCB$, DC + CB > DB.....(iii) In $\triangle ADB$, AD + AB > DB....(iv) Adding equations (i), (ii), (iii) and (iv), we get



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AB + BC + AD + DC + DC + CB + AD + AB > AC + AC + DB + DB

\Rightarrow (AB + AB) + (BC + BC) + (AD + AD) + (DC + DC) > 2AC + 2DB

\Rightarrow 2AB + 2BC + 2AD + 2DC > 2(AC + DB)

\Rightarrow 2(AB + BC + AD + DC) > 2(AC + DB)

\Rightarrow AB + BC + AD + DC > AC + DB
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\Rightarrow AB + BC + CD + DA > AC + DB
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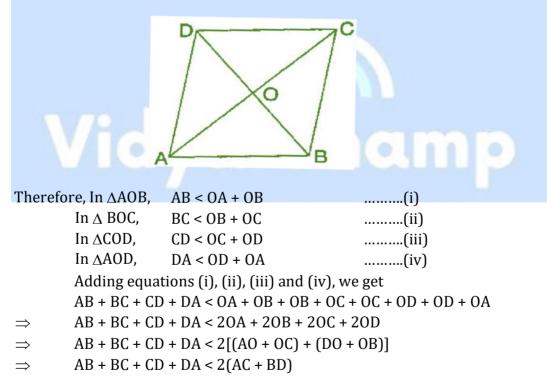
Hence, it is true.

Question 5:

ABCD is quadrilateral. Is AB + BC + CD + DA < 2 (AC + BD)?

Answer 5:

Since, the sum of lengths of any two sides in a triangle should be greater than the length of third side.



Hence, it is proved.



Question 6:

The lengths of two sides of a triangle are 12 cm and 15 cm. Between what two measures should the length of the third side fall?

Answer 6:

Since, the sum of lengths of any two sides in a triangle should be greater than the length of third side.

It is given that two sides of triangle are 12 cm and 15 cm.

Therefore, the third side should be less than 12 + 15 = 27 cm.

And also the third side cannot be less than the difference of the two sides.

Therefore, the third side has to be more than 15 - 12 = 3 cm.

Hence, the third side could be the length more than 3 cm and less than 27 cm.





Exercise 6.5

Question 1:

PQR is a triangle, right angled at P. If PQ = 10 cm and PR = 24 cm, find QR.

Answer 1:

Given: PQ = 10 cm, PR = 24 cm Let QR be *x* cm. In right angled triangle QPR, $(Hypotenuse)^2 = (Base)^2 + (Perpendicular)^2$ [By Pythagoras theorem] $(QR)^2 = (PQ)^2 + (PR)^2$ \Rightarrow $x^{2} = (10)^{2} + (24)^{2}$ \Rightarrow $x^2 = 100 + 576 = 676$ \Rightarrow 24 cm $x = \sqrt{676} = 26 \text{ cm}$ \Rightarrow Thus, the length of QR is 26 cm. O 10 cm

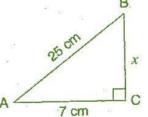
Question 2:

ABC is a triangle, right angled at C. If AB = 25 cm and AC = 7 cm, find BC.

Answer 2:

Given: AB = 25 cm, AC = 7 cm Let BC be *x* cm. In right angled triangle ACB, $(Hypotenuse)^2 = (Base)^2 + (Perpendicular)^2$ [By Pythagoras theorem] $(AB)^2 = (AC)^2 + (BC)^2$ \Rightarrow B. $(25)^2 = (7)^2 + x^2$ \Rightarrow $625 = 49 + x^2$ \Rightarrow x $x^2 = 625 - 49 = 576$ \Rightarrow \Rightarrow

 $x = \sqrt{576} = 24$ cm Thus, the length of BC is 24 cm.

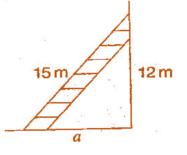




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Question 3:

A 15 m long ladder reached a window 12 m high from the ground on placing it against a wall at a distance *a*. Find the distance of the foot of the ladder from the wall.



Answer 3:

Let AC be the ladder and A be the window. Given: AC = 15 m, AB = 12 m, CB = a mIn right angled triangle ACB, $(Hypotenuse)^2 = (Base)^2 + (Perpendicular)^2$ [By Pythagoras theorem] $(AC)^2 = (CB)^2 + (AB)^2$ \Rightarrow $(15)^2 = (a)^2 + (12)^2$ \Rightarrow $225 = a^2 + 144$ 15 m \Rightarrow 12 m $a^2 = 225 - 144 = 81$ \Rightarrow $a = \sqrt{81} = 9 \text{ cm}$ \Rightarrow

Thus, the distance of the foot of the ladder from the wall is 9 m.

Question 4:

Which of the following can be the sides of a right triangle?

- (i) 2.5 cm, 6.5 cm, 6 cm
- (ii) 2 cm, 2 cm, 5 cm
- (iii) 1.5 cm, 2 cm, 2.5 cm

In the case of right angled triangles, identify the right angles.

Answer 4:

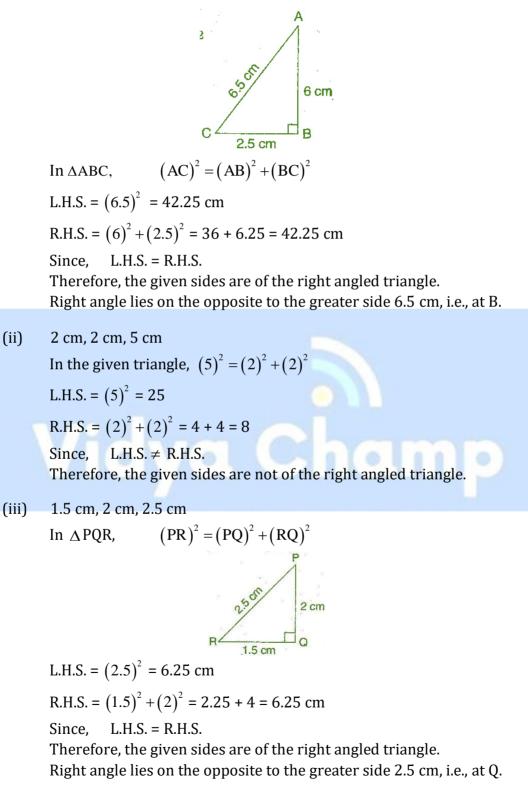
Let us consider, the larger side be the hypotenuse and also using Pythagoras theorem,

 $(Hypotenuse)^2 = (Base)^2 + (Perpendicular)^2$



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(i) 2.5 cm, 6.5 cm, 6 cm



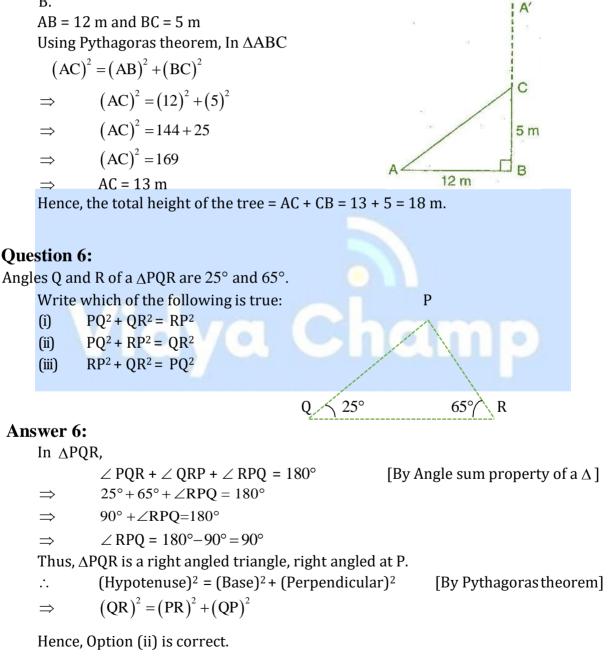


Question 5:

A tree is broken at a height of 5 m from the ground and its top touches the ground at a distance of 12 m from the base of the tree. Find the original height of the tree.

Answer 5:

Let A'CB represents the tree before it broken at the point C and let the top A' touches the ground at A after it broke. Then \triangle ABC is a right angled triangle, right angled at B.





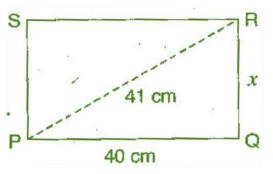
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Question 7:

Find the perimeter of the rectangle whose length is 40 cm and a diagonal is 41 cm. **Answer 7:**

Given diagonal (PR) = 41 cm, length (PQ) = 40 cm

Let breadth (QR) be *x* cm.



Now, in right angled triangle PQR,

$$(PR)^{2} = (RQ)^{2} + (PQ)^{2}$$
 [By Pythagoras theorem]

$$\Rightarrow (41)^{2} = x^{2} + (40)^{2}$$

$$\Rightarrow 1681 = x^{2} + 1600$$

$$\Rightarrow x^{2} = 1681 - 1600$$

$$\Rightarrow x^{2} = 81$$

$$\Rightarrow x = \sqrt{81} = 9 \text{ cm}$$

Therefore the breadth of the rectangle is 9 cm.
Perimeter of rectangle = 2(length + breadth)

$$= 2 (9 + 49)$$

$$= 2 x 49 = 98 \text{ cm}$$

Hence, the perimeter of the rectangle is 98 cm.

Question 8:

The diagonals of a rhombus measure 16 cm and 30 cm. Find its perimeter. **Answer 8:**

Given: Diagonals AC = 30 cm and DB = 16 cm.

Since the diagonals of the rhombus bisect at right angle to each other.

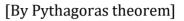


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Therefore, $OD = \frac{DB}{2} = \frac{16}{2} = 8 \text{ cm}$ And $OC = \frac{AC}{2} = \frac{30}{2} = 15 \text{ cm}$ Now, In right angle triangle DOC, A^{4} $(DC)^{2} = (OD)^{2} + (OC)^{2}$ [By F $\Rightarrow (DC)^{2} = (8)^{2} + (15)^{2}$ $\Rightarrow (DC)^{2} = 64 + 225 = 289$ $\Rightarrow DC = \sqrt{289} = 17 \text{ cm}$ Perimeter of rhombus = 4 x side = 4 x 17 = 68 cm

Thus, the perimeter of rhombus is 68 cm.

A B C B



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