

CBSE Test Paper 01
CH-06 Linear Inequalities

1. The solution set of the inequation $3x < 5$, when x is a natural number is
 - a. $\{1,2\}$
 - b. $\{1\}$
 - c. $\{4\}$
 - d. $\{0,1\}$
2. The longest side of a triangle is three times the shortest side and the third side is 2cm shorter than the longest side if the perimeter of the triangles at least 61cm, find the minimum length of the shortest side.
 - a. 16cm
 - b. 61cm
 - c. 9cm
 - d. 11cm
3. What is the solution set for $\frac{2(x-1)}{5} \leq \frac{3(2+x)}{7}$?
 - a. $[-44, \infty)$
 - b. $(-24, \infty)$
 - c. $(-12, \infty)$
 - d. $(-4, \infty)$
4. The graph of the inequalities $x \geq 0$, $y \geq 0$, $2x + y + 6 \leq 0$ is
 - a. none of these
 - b. a triangle
 - c. a square
 - d. $\{\}$
5. $-3x + 17 < -13$, then
 - a. $x \in (-\infty, 10]$
 - b. $x \in [10, \infty)$
 - c. none of these
 - d. $x \in (10, \infty)$
6. Fill in the blanks:

If a and b are real numbers, such that $a < b$, then the set of all real numbers x , such

that $a < x < b$, is called an _____ interval and is denoted by (a, b) or $]a, b[$.

7. Fill in the blanks:

The value of inequality $37 - (3x + 5) \geq 9x - 8(x - 3)$ is _____.

8. Check whether the given plane $3x - 6y \leq 0$ contains the point $(3, 1)$.

9. Solve: $\frac{x}{5} < \frac{3x-2}{4} - \frac{5x-3}{5}$

10. Solve: $-4x > 30$, when

i. $x \in \mathbb{R}$

ii. $x \in \mathbb{Z}$

11. The cost and revenue functions of a product are given by $C(x) = 2x + 400$ and $R(x) = 6x + 20$ respectively, where x is the number of items produced by the manufacturer. How many items the manufacturer must sell to realize some profit?

12. Solve the inequalities and show the graph of the solution in case on number line.

$$5x - 3 \geq 3x - 5$$

13. Solve the following system of inequalities graphically: $x - 2y \leq 3$, $3x + 4y \geq 12$,
 $x \geq 0, y \geq 1$

14. Solve the following system of inequalities graphically: $x \geq 3, y \geq 2$

15. Solve for x , $\frac{|x+3|+x}{x+2} > 1$

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Solution

1. (b) { 1 }

Explanation: $3x < 5$

$$\Rightarrow x < \frac{5}{3}$$

$$\Rightarrow x < 1\frac{2}{3}$$

Hence solution set = $\{x : x < 1\frac{2}{3}, x \in N\} = \{1\}$

2. (c) 9cm

Explanation: Let the shortest side of a triangle be x cm. Then the length of the longest side is $3x$ cm and the length of the third side is $(3x-2)$ cm.

Given the perimeter of the triangles at least 61cm

$$\Rightarrow x + 3x + (3x - 2) \geq 61$$

$$\Rightarrow 7x - 2 \geq 61$$

$$\Rightarrow 7x \geq 63 \Rightarrow x \geq 9$$

Hence the minimum length of the shortest side = 9 cm

3. (a) $[-44, \infty)$

Explanation:

$$\text{Given } \frac{2(x-1)}{5} \leq \frac{3(2+x)}{7}$$

Multiplying both sides by $\text{LCM}(5, 7) = 35$, we get

$$35 \cdot \frac{2(x-1)}{5} \leq 35 \cdot \frac{3(2+x)}{7}$$

$$\Rightarrow 14(x-1) \leq 15(2+x)$$

$$\Rightarrow 14x - 14 \leq 30 + 15x$$

$$\Rightarrow 14x - 15x \leq 30 + 14$$

$$\Rightarrow -x \leq 44$$

$$\Rightarrow x \geq -44$$

Solution set is $[-44, \infty)$

4. (d) $\{ \}$

Explanation:

We have $x \geq 0 \Rightarrow 2x \geq 0$

Also given $y \geq 0$

Hence $2x + y \geq 0$, which means the minimum value possible for $2x + y$ is zero.

Now $2x + y + 6 \leq 0 \Rightarrow 2x + y \leq -6$ which is not possible

Hence the system $x \geq 0, y \geq 0, 2x + y + 6 \leq 0$ has no solution.

5. (d) $x \in (10, \infty)$

Explanation:

$$-3x + 17 < -13$$

$$\Rightarrow -3x + 17 - 17 < -13 - 17$$

$$\Rightarrow -3x < -30$$

$$\Rightarrow \frac{-3x}{-3} > \frac{-30}{-3}$$

$$\Rightarrow x > 10$$

$$\Rightarrow x \in (10, \infty)$$

6. open

7. $x \leq 2$

8. We have, $3x - 6y \leq 0$

On putting $x = 3$ and $y = 1$, we get $3(3) - 6(1) \leq 0$

$$\Rightarrow 9 - 6 \leq 0$$

$$\Rightarrow 3 \leq 0, \text{ which is not true.}$$

\therefore the given plane does not contain the point $(3, 1)$.

$$9. \Rightarrow \frac{x}{5} < \frac{3x-2}{4} - \frac{(5x-3)}{5}$$

$$\Rightarrow \frac{x}{5} < \frac{5(3x-2)-4(5x-3)}{20}$$

$$\Rightarrow x < \frac{15x-10-20x+12}{4}$$

$$\Rightarrow 4x < -5x + 2$$

$$\Rightarrow 4x + 5x < 2$$

$$\Rightarrow 9x < 2$$

$$\Rightarrow x < \frac{2}{9}$$

\therefore The solution set is $\left(-\infty, \frac{2}{9}\right)$

10. Now, $-4x > 30$

$$\Rightarrow x < \frac{-30}{4} = \frac{-15}{2}$$

i. If $x \in \mathbb{R}$, $\Rightarrow x \in \left(-\infty, -\frac{15}{2}\right)$

ii. If $x \in \mathbb{Z}$, $\Rightarrow x \in \{\dots, -10, -9 - 8\}$

11. We know that: profit = Revenue - cost. Therefore, to earn some profit, we must have revenue > Cost

$$\Rightarrow 6x + 20 > 2x + 400$$

$$\Rightarrow 6x - 2x > 400 - 20 \Rightarrow 4x > 380 \Rightarrow x > \frac{380}{4} = 95$$

Hence, the manufacturer must sell more than 95 items to realize some profit.

12. Here $5x - 3 \geq 3x - 5$

$$\Rightarrow 5x - 3x \geq -5 + 3$$

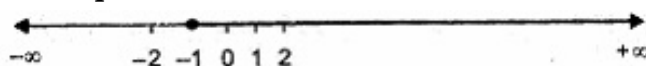
$$\Rightarrow 2x \geq -2$$

Dividing both sides by 2, we have

$$x \geq -1$$

The solution set is $[-1, \infty)$

The representation of the solution set on the number line is



13. The given inequality is $x - 2y \leq 3$

Draw the graph of the line $x - 2y = 3$

Table of values satisfying the equation $x - 2y = 3$

X	1	5

Y	-1	1
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Putting (0, 0) in the given inequation, we have

$$0 - 2 \times 0 \leq 3 \Rightarrow 0 \leq 3, \text{ which is true.}$$

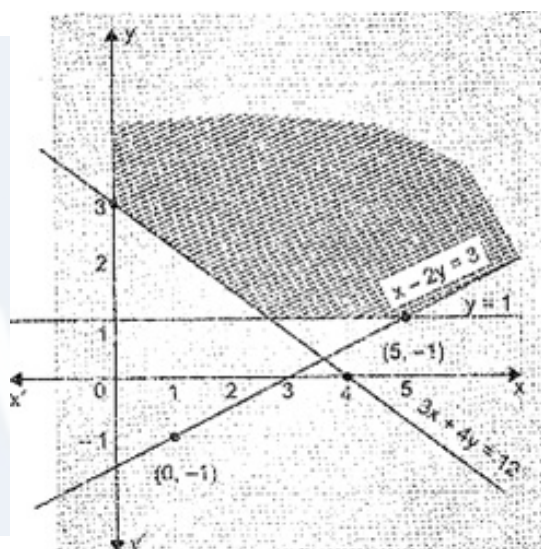
\therefore Half plane of $x - 2y \leq 3$ is towards origin.

Also the given inequality is $3x + 4y \geq 12$

Draw the graph of the line $3x + 4y = 12$

Table of values satisfying the equation $3x + 4y = 12$

X	4	0
Y	0	3



Putting (0, 0) in the given inequation, we have

$$3 \times 0 + 4 \times 0 \geq 12 \Rightarrow 0 \geq 12, \text{ which is false.}$$

\therefore Half plane of $3x + 4y \geq 12$ is away from origin.

The given inequality is $y \geq 1$.

Draw the graph of the line $y = 1$.

Putting (0, 0) in the given inequation, we have

$$0 \geq 1, \text{ which is false.}$$

\therefore Half plane of $y \geq 1$ is away from origin.

14. The given inequality is $x \geq 3$.

Draw the graph of the line $x = 3$.

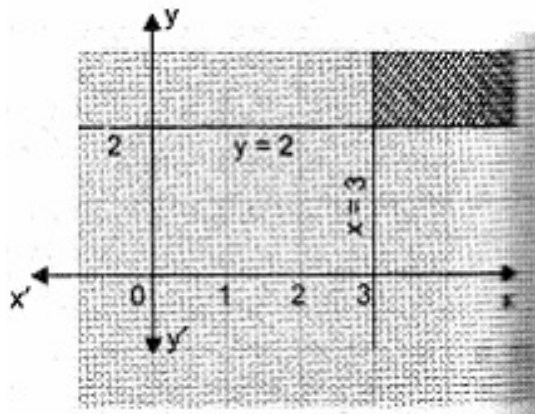
Putting (0, 0) in the given in equation, we have $0 \geq 3$ which is false.

\therefore Half plane of $x \geq 3$ is away from origin.

Also the given inequality is $y \geq 2$

Draw the graph of the line $y = 3$.

Putting $(0, 0)$ in the given inequation, we have $0 \geq 2$ which is false.



\therefore Half plane of $y \geq 2$ is away from origin.

15. We have, $\frac{|x+3|+x}{x+2} > 1$

$$\Rightarrow \frac{|x+3|+x}{x+2} - 1 > 0$$

$$\Rightarrow \frac{|x+3|+x-x-2}{x+2} > 0$$

$$\Rightarrow \frac{|x+3|-2}{x+2} > 0$$

Let $x + 3 = 0$

$$\Rightarrow x = -3$$

$\therefore x = -3$ is a critical point.

So, here we have two intervals $(-\infty, -3)$ and $[-3, \infty)$

Case I: When $-3 \leq x < \infty$, then $|x + 3| = (x + 3)$

$$\therefore \frac{|x+3|-2}{x+2} > 0$$

$$\Rightarrow \frac{x+3-2}{x+2} > 0$$

$$\Rightarrow \frac{x+1}{x+2} > 0$$

$$\Rightarrow \frac{(x+1)(x+2)^2}{(x+2)} > 0 \times (x+2)^2$$

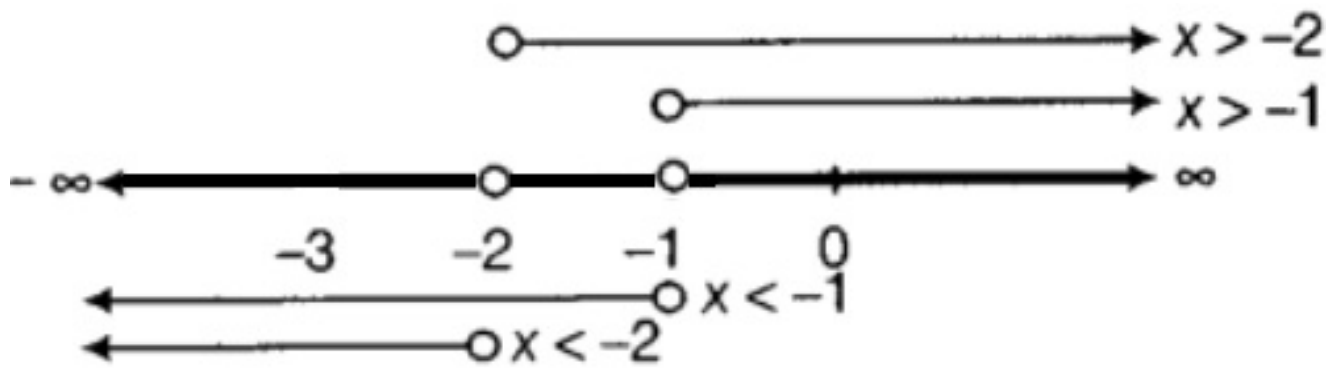
$$\Rightarrow (x+1)(x+2) > 0$$

Product of $(x + 1)$ and $(x + 2)$ will be positive, if both are of same sign.

$\therefore (x + 1) > 0$ and $(x + 2) > 0$ or $(x + 1) < 0$ and $(x + 2) < 0$

$\Rightarrow x > -1$ and $x > -2$ or $x < -1$ and $x < -2$

On number line, these inequalities can be represented as,



Thus, $-1 < x < \infty$ or $-\infty < x < -2$

But, here $-3 \leq x < \infty$

$\therefore -1 < x < \infty$ or $-3 \leq x < -2$

Then, solution set in this case is

$$x \in [-3, -2) \cup (-1, \infty)$$

Case II: When $x < -3$, then $|x + 3| = -(x + 3)$

$$\therefore \frac{|x+3|-2}{x+2} > 0$$

$$\Rightarrow \frac{-x-3-2}{x+2} > 0$$

$$\Rightarrow \frac{-(x+5)}{x+2} > 0$$

$$\Rightarrow \frac{x+5}{x+2} < 0$$

$$\Rightarrow \frac{(x+5)(x+2)^2}{x+2} < 0 \times (x+2)^2$$

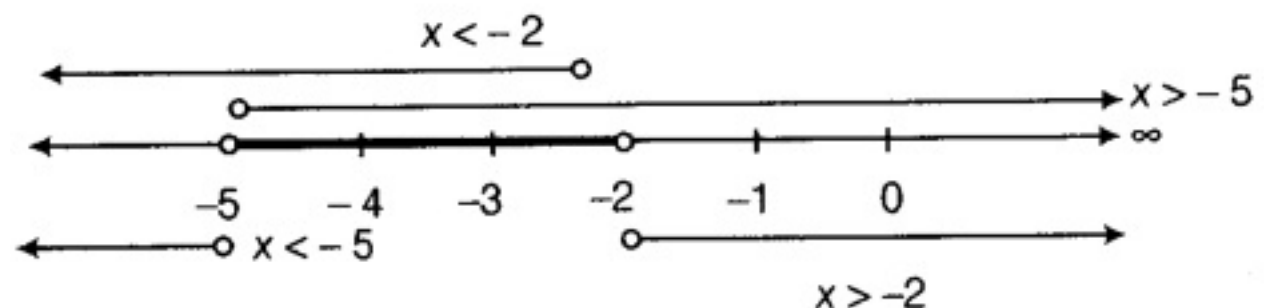
$$\Rightarrow (x+5)(x+2) < 0$$

Product of $(x + 5)$ and $(x + 2)$ will be negative, if both are of opposite sign.

$\therefore (x + 5) > 0$ and $(x + 2) < 0$ or $(x + 5) < 0$ and $(x + 2) > 0$

$\Rightarrow x > -5$ and $x < -2$ or $x < -5$ and $x > -2$

On number line, these inequalities can be represented as,



Thus, $-5 < x < -2$ i.e., solution set in the case is $x \in (-5, -2)$.

On combining cases I and II, we get the required solution set of given inequality,

which is $x \in (-5, -2) \cup (-1, \infty)$