

**CBSE Test Paper 01**  
**CH-10 Straight Lines**

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1. The lines  $x + 2y - 3 = 0$ ,  $2x + y - 3 = 0$  and the line  $l$  are concurrent . If the line  $l$  passes through the origin, then its equation is
  - a.  $x - y = 0$
  - b.  $x + y + 0$
  - c.  $x + 2y = 0$
  - d. none of these
2. Projection (the foot of perpendicular) from  $(x, y)$  on the  $x -$  axis is
  - a.  $(-x, 0)$
  - b.  $(0, y)$
  - c.  $(x, 0)$
  - d.  $(0, -y)$
3. The distance of the point  $(\alpha, \beta)$  from  $X$  axis is
  - a.  $|\beta|$
  - b.  $|\alpha|$
  - c. none of these.
  - d.  $\alpha$
4. A line is drawn through the points  $(3, 4)$  and  $(5, 6)$  . If the is extended to a point whose ordinate is  $-1$ , then the abscissa of that point is
  - a. none of these
  - b. 1
  - c. 0
  - d. -2
5. The line which is parallel to  $X$  axis and crosses the curve  $y = \sqrt{x}$  at an angle of  $45^\circ$  is:
  - a.  $y = 1/2$
  - b.  $y = 1$
  - c. none of these
  - d.  $y = \frac{1}{4}$
6. Fill in the blanks:

If  $a, b, c$  are in A.P., then the straight line  $ax + by + c = 0$  will always pass through

\_\_\_\_\_.

7. Fill in the blanks:

The slope of the line, whose inclination is  $150^\circ$  is \_\_\_\_\_.

8. Prove that the line through the point  $(x_1, y_1)$  and parallel to the line  $Ax + By + C = 0$  is  $A(x - x_1) + B(y - y_1) = 0$ .

9. Prove that the points A (1, 4), B (3, -2) and C (4, -5) are collinear.

10. Find the equation of the line, where length of the perpendicular segment from the origin to the line is 4 and the inclination of the perpendicular segment with the positive direction of X - axis is  $30^\circ$ .

11. If a, b, c are variables such that  $3a + 2b + 4c = 0$ , then show that the family of lines given by  $ax + by + c = 0$  pass through a fixed point. Also, find the point.

12. Show that the lines  $4x + y - 9 = 0$ ,  $x - 2y + 3 = 0$ ,  $5x - y - 6 = 0$  make equal intercepts on any line of gradient 2.

13. A line forms a triangle in the first quadrant with the coordinate axes. If the area of the triangle is  $54\sqrt{3}$  sq units and perpendicular drawn from the origin to the line makes an angle  $60^\circ$  with X-axis, then find the equation of the line.

14. Find the equation of the straight lines which passes through the origin and trisect the intercept of line  $3x + 4y = 12$  between the axes.

15. A rectangle has two opposite vertices at the points (1, 2) and (5,5). If the other vertices lie on the line  $x = 3$ , find the equations of the sides of the rectangle.

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**Solution**

1. (a)  $x - y = 0$

**Explanation:** Equation of a line passing through the intersection of two lines is given by  $ax_1 + by_1 + c_1 + k(ax_2 + by_2 + c_2) = 0$

Hence  $x + 2y - 3 + k(2x + y - 3) = 0$

Since it passes through (0,0)

$-3 - 3k = 0$

This implies  $k = -1$

Substituting for  $k$  we get,

$x + 2y - 3 + (-1)(2x + y - 3) = 0$

$-x + y = 0$  or  $x - y = 0$

2. (c)  $(x, 0)$

**Explanation:** Let  $L$  be the foot of the perpendicular from the  $X$  axis. Therefore its  $y$  coordinate is zero

Therefore the coordinates of the point  $L$  is  $(x, 0)$

Hence option 1 is the correct answer

3. (a)  $|\beta|$

**Explanation:**

The distance of a point from  $X$  axis is its  $y$  coordinate.

Hence the distance of the point  $(\alpha, \beta)$  from  $X$  axis is  $|\beta|$

4. (d)  $-2$

**Explanation:**

The slope of the given line is  $\frac{y_2 - y_1}{x_2 - x_1} = \frac{6 - 4}{5 - 3} = 1$

Therefore  $\frac{4 - (-1)}{3 - x} = 1$

That is  $4 + 1 = 3 - x$

Therefore  $x = -2$

5. (a)  $y = 1/2$

**Explanation:** The equation of the line which is a tangent to the curve  $y = \sqrt{x}$  is  $y = mx + a/m$

Since it makes an angle of  $45^\circ$ ,  $m = 1$

$y^2 = x$  implies  $a = 1/4$

Hence the equation of the tangent is  $y = x +$

That is the y intercept is  $\sqrt{\frac{1}{4}} = 1/2$

Hence the equation of the line is  $y = 1/2$

6. (1, -2)

7.  $-\frac{1}{\sqrt{3}}$

8. Equation of the line parallel to line  $Ax + By + C = 0$  is  $Ax + By + K = 0 \dots (i)$

Since line (i) passes through  $(x_1, y_1)$

$Ax_1 + By_1 + K = 0 \dots (ii)$

Subtracting (ii) from (i), we have

$A(x - x_1) + B(y - y_1) = 0$

9. Given points are A (1, 4), B (3, -2) and C(4, -5)

From the condition for collinearity of points A, B and C, we have

The slope of AB = Slope of BC.

$\therefore \frac{-2-4}{3-1} = \frac{-5+2}{4-3} \left[ \because \text{slope} = \frac{y_2 - y_1}{x_2 - x_1} \right]$

$\Rightarrow \frac{-6}{2} = \frac{-3}{1} \Rightarrow -3 = -3$ , which is true.

Hence, points A, B and C are collinear.

10. The normal form of the equation of the line is  $x \cos \omega + y \sin \omega = p$

Given,  $p = 4$ ,  $\omega = 30^\circ$ . Therefore, the equation of the line is  $x \cos 30^\circ + y \sin 30^\circ = 4$ .  
 $\Rightarrow x \frac{\sqrt{3}}{2} + y \frac{1}{2} = 4 \Rightarrow \sqrt{3}x + y = 8$

11. We have,  $3a + 2b + 4c = 0$

$$\Rightarrow c = -\frac{3}{4}a - \frac{1}{2}b$$

On substituting this value of  $c$  in  $ax + by + c = 0$ , we get

$$ax + by - \frac{3}{4}a - \frac{1}{2}b = 0$$

$$\Rightarrow a \left( x - \frac{3}{4} \right) + b \left( y - \frac{1}{2} \right) = 0$$

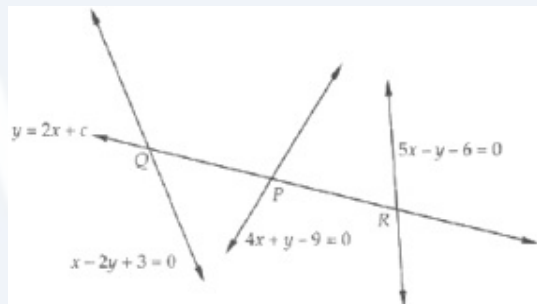
$$\Rightarrow \left( x - \frac{3}{4} \right) + \lambda \left( y - \frac{1}{2} \right) = 0, \text{ where } \lambda = \frac{b}{a}.$$

This equation is of the form  $L_1 + \lambda L_2 = 0$ , which represents a straight line through the intersection of the Line  $L_1 = 0$  and  $L_2 = 0$  i.e.,  $x - \frac{3}{4} = 0$  and  $y - \frac{1}{2} = 0$ .

On solving these two equations, we get the point  $\left( \frac{3}{4}, \frac{1}{2} \right)$  which is a fixed point.

12. The equation of any line of gradient 2 is

$$y = 2x + c \dots(i)$$



The equations of given lines are

$$4x + y - 9 = 0 \dots(ii)$$

$$x - 2y + 3 = 0 \dots(iii)$$

$$5x - y - 6 = 0 \dots(iv)$$

Solving (i) with (ii), (iii) and (iv) respectively, we obtain the coordinates of P, Q and R as

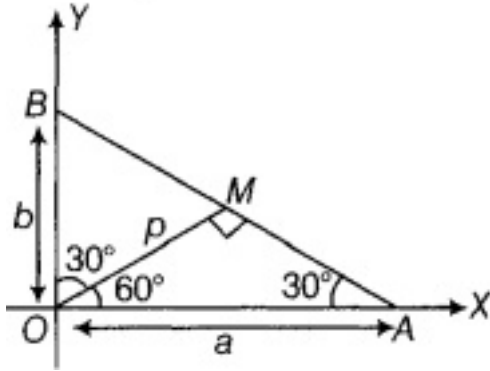
$$P \left( \frac{3}{2} - \frac{c}{6}, 3 + \frac{2c}{3} \right), Q \left( 1 - \frac{2c}{3}, 2 - \frac{c}{3} \right) \text{ and } R \left( 2 + \frac{c}{3}, 4 + \frac{5c}{3} \right)$$

Clearly, P is the mid-point of QR. Therefore  $PQ = PR$ .

Hence, lines (ii), (iii) and (iv) make equal intercepts on any line of gradient 2.

13. Since, OM is the perpendicular line on AB.

$$\text{Here, } \angle MOB = 30^\circ, \angle MOA = 60^\circ$$



Let  $OM = p$ ,  $OA = a$ ,  $OB = b$

In  $\triangle OMA$ ,

$$\frac{p}{a} = \cos 60^\circ = \frac{1}{2} \Rightarrow a = 2p$$

In  $\triangle OMB$ ,

$$\frac{p}{b} = \cos 30^\circ = \frac{\sqrt{3}}{2} \Rightarrow b = \frac{2p}{\sqrt{3}}$$

$$\therefore \text{Area of } \triangle OAB = \frac{1}{2} \times ab = 54\sqrt{3} \text{ [given]}$$

$$\Rightarrow \frac{1}{2}(2p) \times \frac{(2p)}{\sqrt{3}} = 54\sqrt{3}$$

$$\Rightarrow 4p^2 = 54\sqrt{3} \times 2\sqrt{3}$$

$$\Rightarrow p^2 = 81 \Rightarrow p = 9 \text{ [}\because \text{ distance is always positive, so we take positive sign]}$$

Using normal form of the equation of line AB is

$$x \cos \alpha + y \sin \alpha = p$$

$$\therefore x \cos 60^\circ + y \sin 60^\circ = 9$$

$$\Rightarrow x \left(\frac{1}{2}\right) + y \left(\frac{\sqrt{3}}{2}\right) = 9$$

$$\Rightarrow x + \sqrt{3}y - 18 = 0$$

14. The given line is  $3x + 4y = 12 \Rightarrow \frac{x}{4} + \frac{y}{3} = 1 \dots(i)$

Let the line (i) cuts X and Y-axes at A and B, respectively.

Then,  $A = (4, 0)$  and  $B = (0, 3)$ .

Let the line AB be trisected at P and Q, then

$$AP : PB = 1 : 2$$

$$\therefore P = \left( \frac{1 \cdot 0 + 2 \cdot 4}{1+2}, \frac{1 \cdot 3 + 2 \cdot 0}{1+2} \right)$$

$$\Rightarrow P = \left( \frac{8}{3}, 1 \right)$$

and  $AQ : QB = 2:1$

$$\text{Also, } Q = \left( \frac{2 \cdot 0 + 1 \cdot 4}{2+1}, \frac{2 \cdot 3 + 1 \cdot 0}{2+1} \right) = \left( \frac{4}{3}, 2 \right)$$

Now, equation of line OP passing through (0, 0) and  $\left(\frac{8}{3}, 1\right)$  is

$$y - 0 = \frac{1-0}{\frac{8}{3}-0}(x - 0) \Rightarrow y = \frac{3}{8}x$$

$$\Rightarrow 3x - 8y = 0$$

And equation of the line OQ passing through (0,0) and  $\left(\frac{4}{3}, 2\right)$  is

$$y - 0 = \frac{2-0}{\frac{4}{3}-0}(x - 0) \Rightarrow 2y = 3x \Rightarrow 3x - 2y = 0$$

15. Let ABCD be a rectangle whose two opposite vertices are A (1, 2) and C (5,5).

Let the coordinates of the other two vertices B and D of rectangle ABCD be B (3,  $y_1$ ) and D (3,  $y_2$ ). Since diagonals, AC and BD bisect each other. Therefore, the mid-points of AC and BD are the same.

$$\therefore \frac{y_1+y_2}{2} = \frac{2+5}{2} \Rightarrow y_1 + y_2 = 7 \dots(i)$$

Since ABCD is a rectangle.

$$\therefore AC = BD$$

$$\Rightarrow AC^2 = BD^2$$

$$\Rightarrow (1 - 5)^2 + (2 - 5)^2 = (3 - 3)^2 + (y_1 - y_2)^2$$

$$\Rightarrow 16 + 9 = (y_1 - y_2)^2$$

$$\Rightarrow y_1 - y_2 = \pm 5 \dots(ii)$$

Solving (i) and (ii), we get

$$y_1 = 6 \text{ and } y_2 = 1 \text{ or, } y_1 = 1 \text{ and } y_2 = 6$$

Thus, the coordinates of B and D are B (3,1) and D (3, 6).

The equation of side AB is

$$y - 2 = \frac{1-2}{3-1}(x - 1) \text{ or, } y - 2 = -\frac{1}{2}(x - 1) \text{ or, } x + 2y - 5 = 0$$

The equation of side BC is

$$y - 1 = \frac{5-1}{5-3}(x - 3) \text{ or, } y - 1 = 2(x - 3) \text{ or, } 2x - y - 5 = 0$$

The equation of side CD is

$$y - 5 = \frac{6-5}{3-5}(x - 5) \text{ or, } y - 5 = -\frac{1}{2}(x - 5) \text{ or, } x + 2y - 15 = 0$$

The equation of side AD is

$$y - 2 = \frac{6-2}{3-1}(x - 1) \text{ or, } y - 2 = 2(x - 1) \text{ or, } 2x - y = 0$$