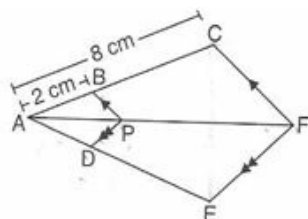


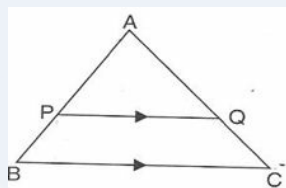
CBSE Test Paper 02

Chapter 6 Triangles

1. In the given figure if $BP \parallel CF$, $DP \parallel EF$, then AD: DE is equal to (1)



- a. 1 : 3.
b. 3 : 4.
c. 2 : 3.
d. 1 : 4.
2. In the given figure $PQ \parallel BC$. $\frac{AP}{PB} = 4$, then the value of $\frac{AQ}{AC}$ is (1)



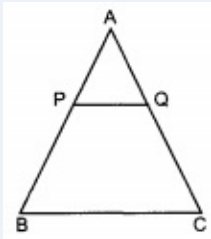
- a. 5
b. $\frac{4}{5}$
c. 4
d. $\frac{5}{4}$
3. If $\triangle ABC \sim \triangle PQR$ such that $AB = 9.1$ cm and $PQ = 6.5$ cm. If the perimeter of $\triangle PQR$ is 25 cm, then the perimeter of $\triangle ABC$ is (1)
- a. 34 cm
b. 35 cm
c. 36 cm
d. 30 cm
4. Out of the given statements (1)
- The areas of two similar triangles are in the ratio of the corresponding altitudes.
 - If the areas of two similar triangles are equal, then the triangles are congruent.
 - The ratio of areas of two similar triangles is equal to the ratio of their corresponding medians.
 - The ratio of the areas of two similar triangles is equal to the ratio of their

corresponding sides.

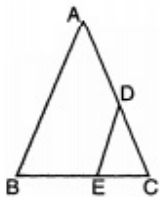
The correct statement is

- a. (iii)
 - b. (ii)
 - c. (i)
 - d. (iv)
5. If in two triangles ABC and DEF, $\frac{AB}{DE} = \frac{BC}{FE} = \frac{CA}{FD}$, then **(1)**
- a. $\triangle FDE \sim \triangle ABC$.
 - b. $\triangle BCA \sim \triangle FDE$.
 - c. $\triangle FDE \sim \triangle CAB$.
 - d. $\triangle CBA \sim \triangle FDE$.

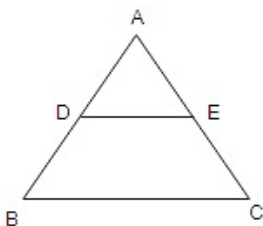
6. In the fig PQ \parallel BC and AP: PB = 1:2. Find $\frac{\text{ar}(\triangle APQ)}{\text{ar}(\triangle ABC)}$. **(1)**



7. If the altitude of two similar triangles are in the ratio 2 : 3, what is the ratio of their areas? **(1)**
8. In the figure of $\triangle ABC$, the points D and E are on the sides CA, CB respectively such that DE \parallel AB, AD = 2x, DC = x + 3, BE = 2x - 1 and CE = x. Then, find x. **(1)**

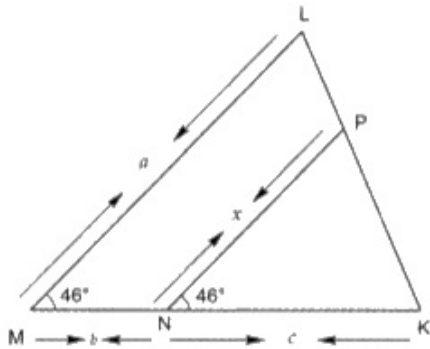


9. In $\triangle ABC$ shown below, DE \parallel BC
If BC = 8 cm, DE = 6 cm and area of $\triangle ADE = 45\text{cm}^2$, What is the area of $\triangle ABC$? **(1)**

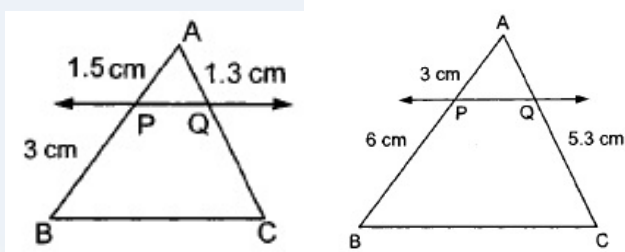


10. In $\triangle ABC$, if X and Y are points on AB and AC respectively such that $\frac{AX}{XB} = \frac{3}{4}$, $AY = 5$ and $YC = 9$, then state whether XY and BC are parallel or not. **(1)**

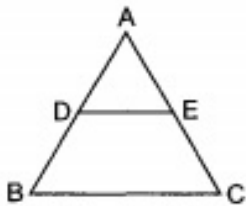
11. In Fig. $\angle M = \angle N = 46^\circ$. Express x in terms of a, b and c where a, b, c are lengths of LM, MN and NK respectively. **(2)**



12. In Fig. (i) and (ii), $PQ \parallel BC$. Find QC in (i) and AQ in (ii). **(2)**

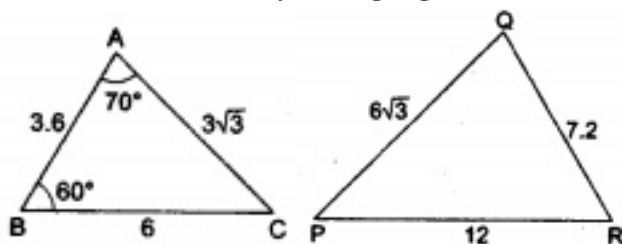


13. In figure, D and E are points on AB and AC respectively, such that $DE \parallel BC$. If $AD = \frac{1}{3} BD$, $AE = 4.5$ cm, find AC. **(2)**



14. In $\triangle ABC$, $DE \parallel BC$ If $AD = x + 2$, $DB = 3x + 16$, $AE = x$ and $EC = 3x + 5$, then find x. **(3)**

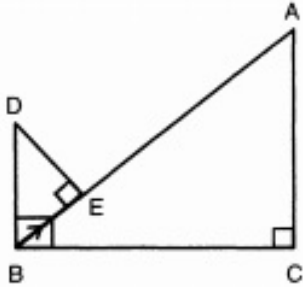
15. Find $\angle P$ in the adjoining figure. **(3)**



16. In three line segments OA, OB, and OC, points L, M, N respectively are so chosen that

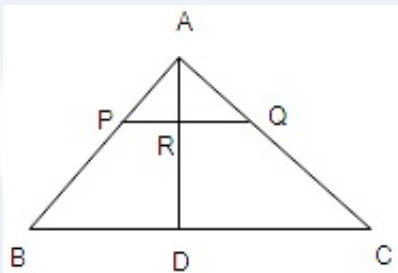
$LM \parallel AB$ and $MN \parallel BC$ but neither of L, M, N nor of A, B, C are collinear. Show that $LN \parallel AC$. (3)

17. In the given figure, $DB \perp BC$, $DE \perp AB$ and $AC \perp BC$. Prove that $\frac{BE}{DE} = \frac{AC}{BC}$ (3)

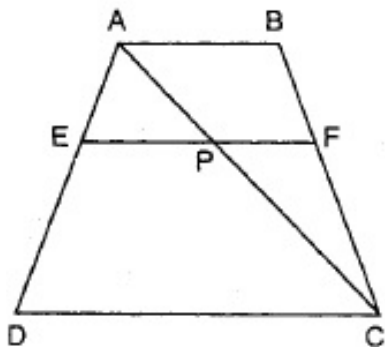


18. For going to a city B from city A, there is a route via city C such that $AC \perp CB$, $AC = 2x$ km and $CB = 2(x + 7)$ km. It is proposed to construct a 26 km highway which directly connects the two cities A and B. Find how much distance will be saved in reaching city B from city A after the construction of the highway. (4)

19. In the given figure, $AP = 3$ cm, $AR = 4.5$ cm, $AQ = 6$ cm, $AB = 5$ cm and $AC = 10$ cm, then find AD and the ratio of areas of $\triangle ARQ$ and $\triangle ADC$. (4)



20. In Fig. if $EF \parallel DC \parallel AB$. prove that $\frac{AE}{ED} = \frac{BF}{FC}$. (4)



CBSE Test Paper 02
Chapter 6 Triangles

Solution

1. a. 1 : 3.

Explanation: In $\triangle AFC$, $BP \parallel FC \Rightarrow \frac{AB}{BC} = \frac{AP}{PF} = \frac{1}{3}$

In $\triangle AFE$, $DP \parallel FE \Rightarrow \frac{AD}{DE} = \frac{AP}{PF} = \frac{1}{3}$

therefore AD:DE = 1:3

2. b. $\frac{4}{5}$

Explanation: Given: $\frac{AP}{PB} = \frac{4}{1}$

Let AP = 4x and PB = x, then AB = AP + PB = 4x + x = 5x

Since PQ \parallel BC, then

$\frac{AP}{AB} = \frac{AQ}{AC}$ [Using Thales theorem]

$\therefore \frac{AQ}{AC} = \frac{AP}{AB} = \frac{4x}{5x} = \frac{4}{5}$

3. b. 35 cm

Explanation:

$\frac{AB}{PQ} = \frac{7}{5}$ (cpst) Therefore $BC = a \implies QR = \frac{5}{7}a$, $AC = b \implies PR = \frac{5}{7}b$

$6.5 + \frac{5}{7}a + \frac{5}{7}b = 25 \implies a + b = 25.9$

Therefore perimeter of $\triangle ABC = 35$

4. b. (ii)

Explanation: If the areas of two similar triangles are equal, then the triangles are congruent

Option (i) is wrong since "The areas of two similar triangles are in the ratio of the square of the corresponding altitudes.

Like that options (iii) and (iv) are also wrong.

5. c. $\triangle FDE \sim \triangle CAB$.

Explanation: If in two triangles ABC and DEF, $\frac{AB}{DE} = \frac{BC}{FE} = \frac{CA}{FD}$, then

$\triangle FDE \sim \triangle CAB$

because for similarity, all the corresponding sides should be in proportion.

6. In ABC,

$PQ \parallel BC$

$$\therefore \frac{AP}{AB} = \frac{AQ}{AC}$$

Now in $\triangle APQ$ and $\triangle ABC$,

$$\frac{AP}{AB} = \frac{AQ}{AC} \text{ (As proved)}$$

$\angle A = \angle A$ (common angle)

$\triangle APQ \sim \triangle ABC$ (SAS similarity)

Since for similar triangles, the ratio of the areas is the square of the ratio of their corresponding sides. Therefore,

$$\frac{\text{ar}(\triangle APQ)}{\text{ar}(\triangle ABC)} = \frac{AP^2}{AB^2} = \frac{AP^2}{(AP+PB)^2} = \frac{1^2}{3^2} = \frac{1}{9}$$

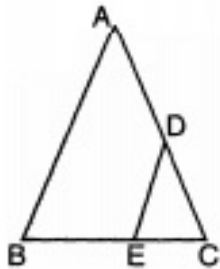
7. We know that the ratio of areas of two similar triangles is equal to the square of the ratio of corresponding altitude.

Ratio of their areas = (ratio of their altitudes)²

$$= \left(\frac{2}{3}\right)^2 = \frac{4}{9}$$

$$= 4 : 9$$

8. $DE \parallel AB$



$AD = 2x$, $DC = x + 3$, $BE = 2x - 1$ and $CE = x$

By Basic proportionality theorem

$$\frac{CD}{AD} = \frac{CE}{BE}$$
$$\frac{x+3}{2x} = \frac{x}{2x-1}$$

$$(x + 3)(2x - 1) = x(2x)$$

$$2x^2 - x + 6x - 3 = 2x^2$$

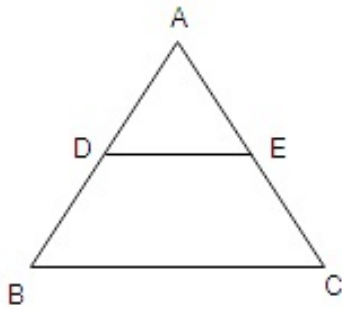
$$2x^2 + 5x - 3 = 2x^2$$

$$5x - 3 = 0$$

$$\text{or, } 5x = 3$$

$$x = \frac{3}{5}$$

9. $\triangle ADE \sim \triangle ABC$



$$\Rightarrow \frac{ar(\triangle ADE)}{ar(\triangle ABC)} = \left(\frac{DE}{BC}\right)^2$$

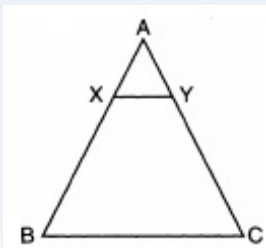
$$\Rightarrow \frac{45}{ar(\triangle ABC)} = \left(\frac{6}{8}\right)^2$$

$$\Rightarrow \frac{45}{ar(\triangle ABC)} = \frac{36}{64}$$

$$\Rightarrow ar(\triangle ABC) = \frac{64(45)}{36}$$

$$\Rightarrow ar(\triangle ABC) = 80\text{cm}^2$$

10.



$$\frac{AX}{XB} = \frac{3}{4} \dots (i)$$

$$\frac{AY}{CY} = \frac{5}{9} \dots (ii)$$

From eqn (i) and (ii)

$$\frac{AX}{XB} \neq \frac{AY}{YC}$$

So XY and BC are not parallel

11. In $\triangle KPN$ and $\triangle KLM$, we have

$$\angle KNP = \angle KML = 46^\circ \text{ [Given]}$$

$$\angle NKP = \angle MKL \text{ [Common]}$$

Thus, $\triangle KPN \sim \triangle KLM$ [by AA similarity criterion of triangles]

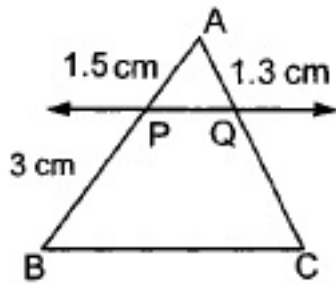
$\frac{KN}{KM} = \frac{NP}{ML}$ [because we know that corresponding sides of similar triangles are proportional]

$$\frac{c}{b+c} = \frac{x}{a} \text{ [KM = MN + NK]}$$

$$\Rightarrow x(b+c) = ca$$

Therefore, $x = \frac{ac}{b+c}$

12. According to question



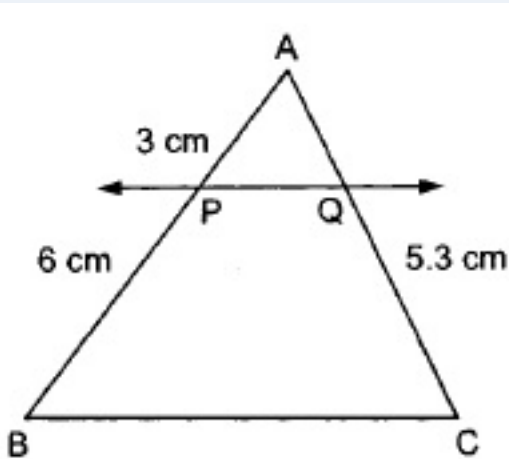
$$PQ \parallel BC$$

Therefore, by basic proportionality theorem, we have

$$\frac{AP}{PB} = \frac{AQ}{QC}$$
$$\Rightarrow \frac{1.5}{3} = \frac{1.3}{QC}$$
$$\Rightarrow \frac{1}{2} = \frac{1.3}{QC}$$

$$\Rightarrow QC = 2.6 \text{ cm}$$

In Fig. (ii)



it is given that $PQ \parallel BC$.

Therefore, by basic proportionality theorem, we have

$$\frac{AP}{PB} = \frac{AQ}{QC}$$
$$\Rightarrow \frac{3}{6} = \frac{AQ}{5.3}$$
$$\Rightarrow \frac{1}{2} = \frac{AQ}{5.3}$$
$$\Rightarrow AQ = \frac{5.3}{2} = 2.65 \text{ cm}$$

Hence $QC = 2.6 \text{ cm}$ and $AQ = 2.65 \text{ cm}$ respectively

13. According to question it is given that D and E are the points on sides AB and AC respectively

$$\text{Also } AD = \frac{1}{3} BD,$$

$$AE = 4.5 \text{ cm, } DE \parallel BC$$

$$\therefore \frac{AD}{BD} = \frac{AE}{EC}$$

$$\Rightarrow \frac{\frac{1}{3}BD}{BD} = \frac{4.5}{EC}$$

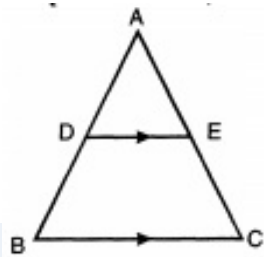
$$\Rightarrow \frac{1}{3} = \frac{4.5}{EC}$$

$$\Rightarrow EC = 4.5 \times 3 \text{ cm}$$

$$\Rightarrow EC = 13.5 \text{ cm}$$

$$\text{Now, } AC = AE + EC = 4.5 + 13.5 = 18 \text{ cm}$$

14.



$$\therefore DE \parallel BC$$

$$\frac{AD}{DB} = \frac{AE}{EC} \text{ (by BPT)}$$

$$\text{or, } \frac{x+2}{3x+16} = \frac{x}{3x+5}$$

On cross multiplication we get

$$(x+2)(3x+5) = x(3x+16)$$

$$3x^2 + 5x + 6x + 10 = 3x^2 + 16x$$

$$5x = 10$$

$$x = 2$$

15. In $\triangle ABC$ and $\triangle QRP$, we have

$$\frac{AB}{QR} = \frac{3.6}{7.2} = \frac{1}{2},$$

$$\frac{BC}{RP} = \frac{6}{12} = \frac{1}{2}$$

$$\text{and } \frac{CA}{PQ} = \frac{3\sqrt{3}}{6\sqrt{3}} = \frac{1}{2}$$

Thus, $\frac{AB}{QR} = \frac{BC}{RP} = \frac{CA}{PQ}$ and so

$\triangle ABC \sim \triangle QRP$ [by SSS-similarly].

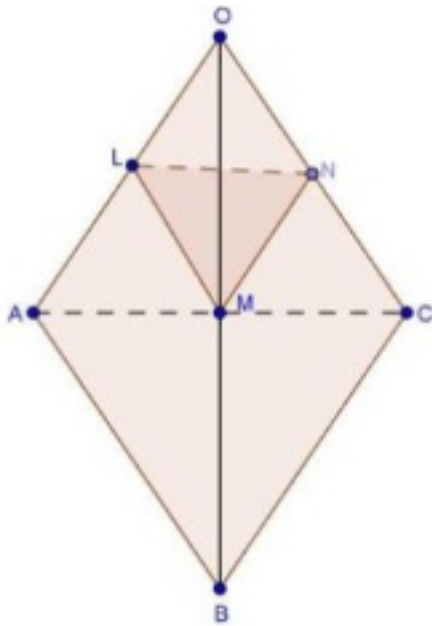
$\therefore \angle C = \angle P$ [corresponding angles of similar triangles].

$$\text{But, } \angle C = 180^\circ - (\angle A + \angle B)$$

$$= 180^\circ - (70^\circ + 60^\circ) = 50^\circ$$

$$\therefore \angle P = 50^\circ.$$

16. We have,



$LM \parallel AB$ and $MN \parallel BC$

Therefore, by basic proportionality theorem,

We have,

$$\frac{OL}{AL} = \frac{OM}{MB} \dots\dots(i)$$

And, $\frac{ON}{NC} = \frac{OM}{MB} \dots\dots(ii)$

Compare equation (i) and equation (ii), we get

$$\frac{OL}{AL} = \frac{ON}{NC}$$

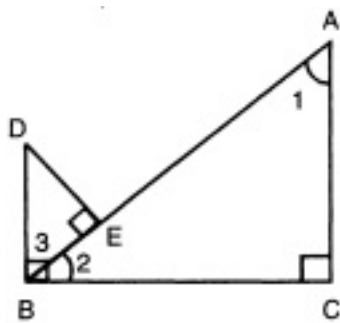
Thus, LN divides sides OA and OC $\triangle OAC$ in the same ratio.

Therefore, by the converse of basic proportionality theorem, we have,

$LN \parallel AC$.

17. Given:

$DB \perp BC$, $DE \perp AB$ and $AC \perp BC$



To prove:

$$\frac{BE}{DE} = \frac{AC}{BC}$$

Proof: As per the figure

$$\angle 1 + \angle 2 = 90^\circ$$

$$\angle 2 + \angle 3 = 90^\circ$$

$$\text{So } \angle 1 = \angle 3$$

$\triangle ABC$ and $\triangle BDE$

$$\angle ACB = \angle DEB = 90^\circ$$

$$\angle 1 = \angle 3$$

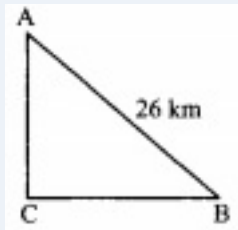
Hence $\triangle ACB \sim \triangle DEB$

$$\text{Hence } \frac{BE}{DE} = \frac{AC}{BC}$$

18. A.T.Q.

Let $AC = 2x$ km

$CB = 2(x + 7)$ km



In right-angled $\triangle ACB$, $AB^2 = AC^2 + CB^2$

Highway is $AB = 26$ km

$$(26)^2 = (2x)^2 + (2(x + 7))^2$$

$$\Rightarrow 676 = 4x^2 + 4(x + 7)^2$$

$$\Rightarrow \frac{676}{4} = x^2 + x^2 + 49 + 14x$$

$$\Rightarrow 169 = 2x^2 + 14x + 49$$

$$\Rightarrow 2x^2 + 14x + 49 - 169 = 0$$

$$\Rightarrow 2x^2 + 14x - 120 = 0$$

$$\Rightarrow x^2 + 7x - 60 = 0$$

$$\Rightarrow x^2 + 12x - 5x - 60 = 0$$

$$\Rightarrow x(x + 12) - 5(x + 12) = 0$$

$$\Rightarrow (x - 5)(x + 12) = 0$$

$$\Rightarrow x = -12, 5$$

So, $AC = 2x = 2(5) = 10$ km

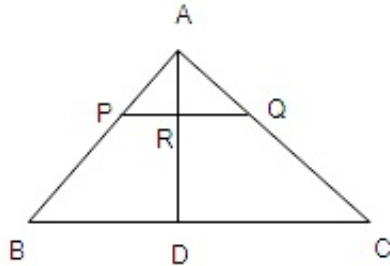
$BC = 2(x + 7) = 2(5 + 7) = 24$ km

Total distance for A to B via C = 10 + 24 = 34 km

A to B via highway = 26 km

Distance saved = 34 - 26 = 8 km.

19. Given , AP = 3cm, AR = 4.5 cm, AQ = 6 cm, AB = 5 cm and AC = 10 cm



$$\text{Here, } \frac{AP}{AB} = \frac{3}{5} \text{ and } \frac{AQ}{AC} = \frac{6}{10} = \frac{3}{5}$$

$$\Rightarrow \frac{AP}{AB} = \frac{AQ}{AC}$$

Thus, $PQ \parallel BC$ [by converse of basic proportionality theorem]

In $\triangle ARQ$ and $\triangle ADC$

$$\angle RAQ = \angle DAC \text{ [common angle]}$$

$$\angle ARQ = \angle ADC \text{ [corresponding angles]}$$

$$\angle RQA = \angle DCA \text{ [corresponding angles]}$$

So, $\triangle ARQ \sim \triangle ADC$ [By AAA similarity criterion]

$$\Rightarrow \frac{AR}{AD} = \frac{AQ}{AC} \text{ [Since, corresponding sides of similar triangles are proportional]}$$

$$\Rightarrow \frac{AR}{4.5} = \frac{6}{10}$$

$$\Rightarrow AD = \frac{45}{6}$$

$$\Rightarrow AD = \frac{15}{2} = 7.5 \text{ cm} \dots\dots (i)$$

$$\text{Now, } \frac{ar(\triangle ARQ)}{ar(\triangle ADC)} = \left(\frac{AQ}{AC}\right)^2 \text{ [By theorem of area of similar triangles]}$$

$$\frac{ar(\triangle ARQ)}{ar(\triangle ADC)} = \left(\frac{6}{10}\right)^2$$

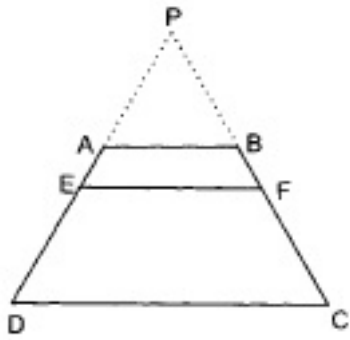
$$\frac{ar(\triangle ARQ)}{ar(\triangle ADC)} = \frac{36}{100}$$

$$\frac{ar(\triangle ARQ)}{ar(\triangle ADC)} = \frac{9}{25} \dots\dots (ii)$$

$$\text{So, } AD = 7.5 \text{ cm and } \frac{ar(\triangle ARQ)}{ar(\triangle ADC)} = \frac{9}{25}.$$

20. Given: According to the question, We have, $EF \parallel DC \parallel AB$ in the given figure.

$$\text{To prove: } \frac{AE}{ED} = \frac{BF}{FC}$$



Construction: Produce DA and CB to meet at P(say).

Proof: In $\triangle PEF$, we have

$$AB \parallel EF$$

$$\therefore \frac{PA}{AE} = \frac{PB}{BF} \text{ [By Basic proportionality theorem]}$$

$$\Rightarrow \frac{PA}{AE} + 1 = \frac{PB}{BF} + 1 \text{ [Adding 1 on both sides]}$$

$$\Rightarrow \frac{PA+AE}{AE} = \frac{PB+BF}{BF}$$

$$\Rightarrow \frac{PE}{AE} = \frac{PF}{BF} \dots(1)$$

In $\triangle PDC$, we have,

$$EF \parallel DC$$

$$\therefore \frac{PE}{ED} = \frac{PF}{FC} \text{ [By Basic Proportionality Theorem]} \dots(2)$$

Therefore, on dividing equation (i) by equation (ii), we get

$$\frac{\frac{PE}{AE}}{\frac{PE}{ED}} = \frac{\frac{PF}{BF}}{\frac{PF}{FC}}$$

$$\Rightarrow \frac{ED}{AE} = \frac{FC}{BF}$$

$$\Rightarrow \frac{AE}{ED} = \frac{BF}{FC}$$