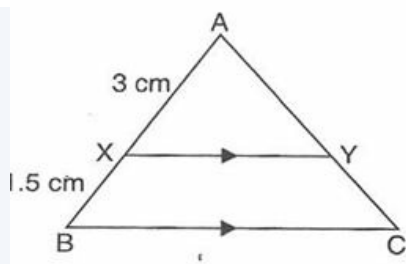


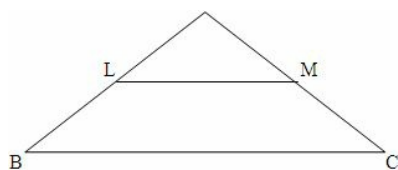
CBSE Test Paper 01

Chapter 6 Triangles

- In an isosceles triangle ABC if  $AC = BC$  and  $AB^2 = 2AC^2$  then the measure of  $\angle C$  is **(1)**
  - $90^\circ$
  - $45^\circ$
  - $60^\circ$
  - $30^\circ$
- In the given figure  $XY \parallel BC$ . If  $AX = 3\text{cm}$ ,  $XB = 1.5\text{cm}$  and  $BC = 6\text{cm}$ , then  $XY$  is equal to **(1)**



- 6 cm.
  - 4.5 cm
  - 3 cm.
  - 4 cm.
- What will be the length of the hypotenuse of an isosceles right triangle whose one side is  $4\sqrt{2}\text{ cm}$  **(1)**
    - $12\sqrt{2}\text{ cm}$ .
    - 12 cm.
    - 8 cm.
    - $8\sqrt{2}\text{ cm}$ .
  - In the given figure, if  $\frac{\text{ar}(\triangle ALM)}{\text{ar}(\text{trapezium } LMCB)} = \frac{9}{16}$ , and  $LM \parallel BC$ , Then  $AL:LB$  is equal to **(1)**



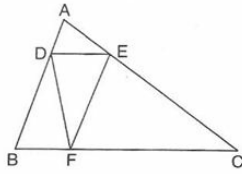
- 3 : 5

b. 4 : 1

c. 3 : 4

d. 2 : 3

5. In the following figure  $AD : DB = 1 : 3$ ,  $AE : EC = 1 : 3$  and  $BF : FC = 1 : 4$ , then **(1)**



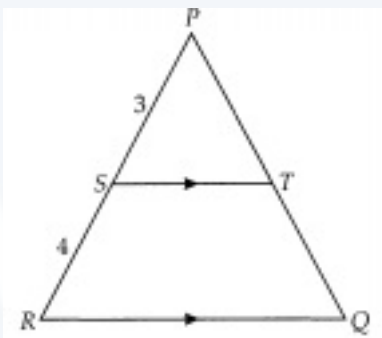
a.  $AD \parallel FC$ .

b.  $AD \parallel FE$ .

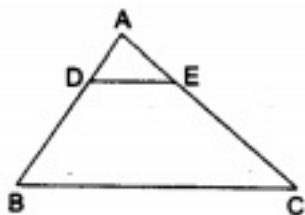
c.  $DE \parallel BC$ .

d.  $AE \parallel DF$ .

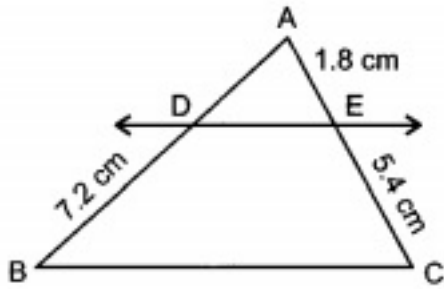
6. In the given figure,  $ST \parallel RQ$ ,  $PS = 3$  cm and  $SR = 4$  cm. Find the ratio of the area of  $\triangle PST$  to the area of  $\triangle PRQ$ . **(1)**



7. If D and E are points on the sides AB and AC respectively of  $\triangle ABC$  such that  $AB = 5.6$  cm,  $AD = 1.4$  cm,  $AC = 7.2$  cm and  $AE = 1.8$  cm, show that  $DE \parallel BC$ . **(1)**

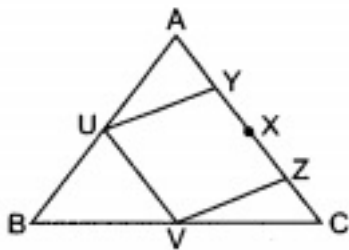


8. A ladder is placed in such a way that its foot is at a distance of 5 m from a wall and its tip reaches a window 12 m above the ground. Determine the length of the ladder. **(1)**
9. Triangles ABC and DEF are similar. If  $AC = 19$  cm and  $DF = 8$  cm, find the ratio of the area of two triangles. **(1)**
10. In the given figure,  $DE \parallel BC$ .

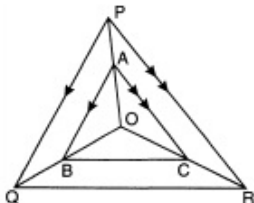


Find AD. **(1)**

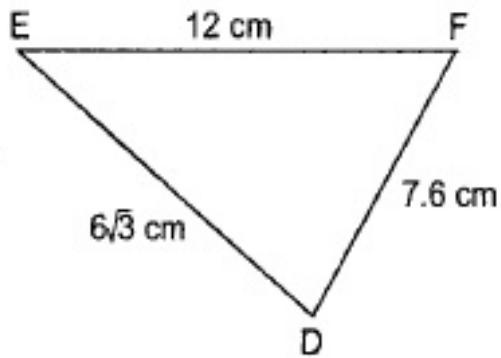
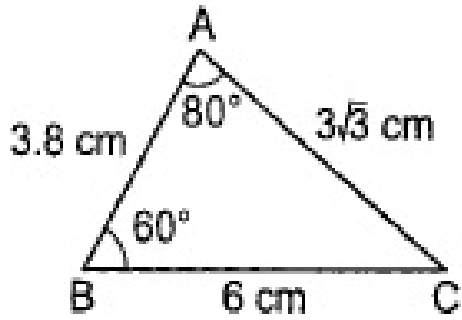
11. In  $\triangle ABC$ , X is any point on AC. If Y, Z, U and V are the middle points on AX, XC, AB and BC respectively, then prove that  $UY \parallel VZ$  and  $UV \parallel YZ$ .



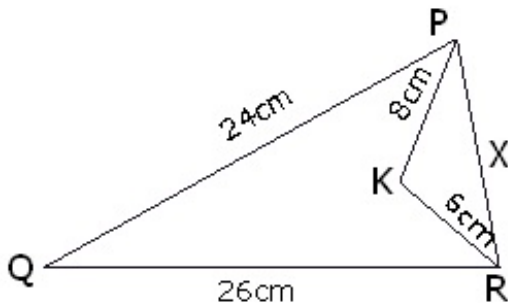
12. If the angles of one triangle are respectively equal to the angles of another triangle, Prove that the ratio of their corresponding sides is the same as the ratio of their corresponding angle bisectors. **(2)**
13. In a  $\triangle ABC$ , D and E are points on the sides AB and AC respectively such that  $DE \parallel BC$ . If  $AD = x$ ,  $DB = x-2$ ,  $AE = x + 2$  and  $EC = x - 1$ , find the value of x. **(2)**
14. A man goes 10m due south and then 24m due west. How far is he from the starting point? **(3)**
15. In the given figure A, B and C are points on OP, OQ and OR respectively such that  $AB \parallel PQ$  and  $AC \parallel PR$ . Prove that  $BC \parallel QR$ .



16. In a  $\triangle ABC$ , D and E are points on the sides AB and AC respectively such that  $DE \parallel BC$ . If  $AD = 8x - 7$ ,  $DB = 5x - 3$ ,  $AE = 4x - 3$  and  $EC = (3x - 1)$ , find the value of x. **(3)**
17. In Fig. find  $\angle F$ . **(3)**



18. Prove that ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides. **(4)**
19. In a trapezium ABCD,  $AB \parallel DC$  and  $DC = 2AB$ .  $EF \parallel AB$ , where E and F lie on BC and AD respectively such that  $\frac{BE}{EC} = \frac{4}{3}$ . Diagonal DB intersects EF at G. Prove that,  $7EF = 11AB$ . **(4)**
20. In a triangle, if the square of one side is equal to the sum of the squares on the other two sides. Prove that the angle opposite to the first side is a right angle. Use the above theorem to find the measure of  $\angle PKR$  in the figure given below. **(4)**



**CBSE Test Paper 01**  
**Chapter 6 Triangles**

**Solution**

1. a.  $90^\circ$

**Explanation:** Given:  $AB^2 = 2AC^2$

$$\Rightarrow AB^2 = AC^2 + AC^2$$

$\Rightarrow AB^2 = AC^2 + BC^2$  [Given:  $AC = BC$ ]  $\therefore \Delta ABC$  is a right angled triangle, by converse of Pythagoras theorem

Now, since  $\Delta ABC$  is an isosceles triangle also.

Therefore, its two sides are equal i.e.,  $AC = BC$  Therefore,  $AB$  is hypotenuse.

$\therefore \angle C$  is a right angle i.e.,  $90^\circ$

2. d. 4 cm.

**Explanation:** Since  $XY \parallel BC$ , then using Thales theorem,

$$\Rightarrow \frac{AX}{AB} = \frac{XY}{BC}$$

$$\Rightarrow \frac{3}{4.5} = \frac{XY}{6}$$

$$\Rightarrow XY = 4 \text{ cm}$$

3. c. 8 cm.

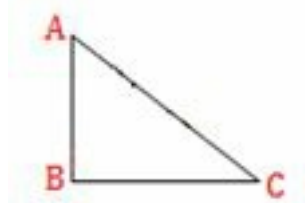
**Explanation:** Let  $AC$  be hypotenuse. Its equal sides are  $AB$  and  $BC$  and  $AB = BC = 4\sqrt{2}$  cm.

Using Pythagoras Theorem,

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow AC^2 = (4\sqrt{2})^2 + (4\sqrt{2})^2 = 32 + 32 = 64 \text{ cm}^2$$

$$\Rightarrow AC = 8 \text{ cm}$$



4. b. 4 : 1

**Explanation:** In  $\Delta ALM$  and  $\Delta ABC$ ,  $\angle A = \angle A$  [Common]

$\angle ALM = \angle ABC$  [Corresponding angles as  $LM \parallel BC$ ]

$$\begin{aligned}
&\therefore \Delta ALM \sim \Delta ABC \text{ [AA similarity]} \\
&\therefore \frac{\text{ar}(\Delta ALM)}{\text{ar}(\Delta ABC)} = \frac{AL^2}{AB^2} \text{ Now, } \frac{\text{ar}(\text{trap.LMCB})}{\text{ar}(\Delta ALM)} = \frac{9}{16} \\
&\Rightarrow \frac{\text{ar}(\Delta ABC) - \text{ar}(\Delta ALM)}{\text{ar}(\Delta ALM)} = \frac{9}{16} \\
&\Rightarrow \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta ALM)} - 1 = \frac{9}{16} \\
&\Rightarrow \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta ALM)} = \frac{9}{16} + 1 \\
&\Rightarrow \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta ALM)} = \frac{25}{16} \\
&\Rightarrow \frac{AB^2}{AL^2} = \frac{25}{16} \\
&\Rightarrow \frac{AB}{AL} = \frac{5}{4}
\end{aligned}$$

Let  $AB = 5x$  and  $AL = 4x$  then  $LB = AB - AL = 5x - 4x = 1x$

$$\begin{aligned}
&\therefore \frac{AL}{LB} = \frac{4x}{1x} = \frac{4}{1} \\
&\Rightarrow AL : LB = 4 : 1
\end{aligned}$$

5. c.  $DE \parallel BC$ .

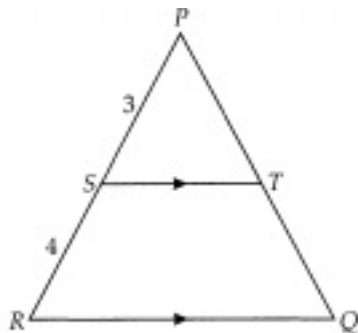
**Explanation:** Given:  $\frac{AD}{DB} = \frac{1}{3}$  and  $\frac{AE}{EC} = \frac{1}{3}$

Therefore, in  $\Delta ABC$ ,  $\frac{AD}{DB} = \frac{AE}{EC}$

$\therefore DE \parallel BC$  [Using Thales Theorem]

Here we are not considering  $BF : FC = 1 : 4$ .

6.  $PS = 3$  cm,  $SR = 4$  cm and  $ST \parallel RQ$ .



$$\begin{aligned}
PR &= PS + SR \\
&= 3 + 4 = 7 \text{ cm}
\end{aligned}$$

In  $\Delta PST$  and  $\Delta PRQ$

$\angle SPT \cong \angle RPQ$  (common angle)

$\angle PST \cong \angle PRQ$  (Alternate angle)

$\Delta PST \sim \Delta PRQ$  (AA configuration)

$$\frac{\text{ar } \triangle PST}{\text{ar } \triangle PQR} = \frac{PS^2}{PR^2} = \frac{3^2}{7^2} = \frac{9}{49}$$

Hence required ratio = 9 : 49.

7. Given:  $AB = 5.6$  cm,  $AD = 1.4$  cm,  $AC = 7.2$  cm and  $AE = 1.8$  cm

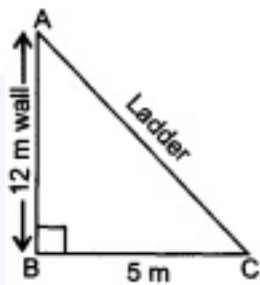
$$\therefore \frac{AD}{AB} = \frac{1.4}{5.6} = \frac{1}{4} \text{ and } \frac{AE}{AC} = \frac{1.8}{7.2} = \frac{1}{4}$$

$$\Rightarrow \frac{AD}{AB} = \frac{AE}{AC}$$

Hence, by the converse of Thales' theorem,  $DE \parallel BC$ .

8. Let  $AC$  be the ladder,  $AB$  be the wall and  $BC$  be the distance of ladder from the foot of the wall.

In right  $\triangle ABC$ ,



$$AC^2 = AB^2 + BC^2 \{ \text{using Pythagoras theorem for right-angled triangle} \}$$

$$\Rightarrow AC^2 = (12)^2 + 5^2$$

$$\Rightarrow AC^2 = 144 + 25$$

$$\Rightarrow AC = 13 \text{ m}$$

9. We have,

$$\triangle ABC \sim \triangle DEF$$

$$AC = 19 \text{ cm and } DF = 8 \text{ cm}$$

By area of similar triangle theorem

$$\frac{\text{Area}(\triangle ABC)}{\text{Area}(\triangle DEF)} = \frac{AC^2}{DF^2} = \frac{(19)^2}{8^2} = \frac{361}{64}$$

10.  $\therefore DE \parallel BC$

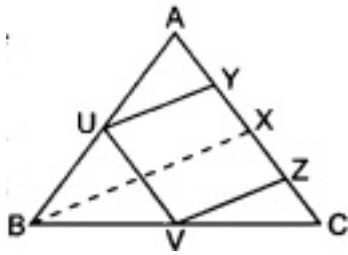
$$\therefore \frac{AD}{BD} = \frac{AE}{CE} \text{ (from BPT)}$$

$$\Rightarrow \frac{AD}{7.2} = \frac{1.8}{5.4} \Rightarrow AD = 2.4 \text{ cm}$$

11. Join  $BX$

In  $ABX$ ,  $U$  is midpoint of  $AB$  and  $Y$  is mid-point  $AX$  (given)

$\therefore UY \parallel BX$  (using mid-point theorem) .....(i)



In BCX, v is mid-point of BC and z is mid-point of XC

$VZ \parallel BX$  ..(ii)

from (i) and (ii)

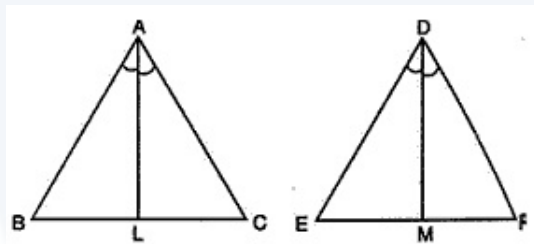
$UY \parallel VZ$

In ABC, U is mid-point of AB and V is mid-point of BE.

$\therefore UV \parallel AC$

$\Rightarrow UV \parallel YZ$  Hence proved.

12.



Given: Two triangles ABC and DEF in which  $\angle A = \angle D$ ,  $\angle B = \angle E$  and  $\angle C = \angle F$ , AL and DM are angle bisectors of  $\angle A$

and  $\angle D$  respectively

To prove:  $\frac{BC}{EF} = \frac{AL}{DM}$

Proof: Triangle ABC and DEF are Similar.

$\Rightarrow \frac{AB}{DE} = \frac{BC}{EF}$  .....(i)

In  $\triangle ABL$  and  $\triangle DEM$ , we have

$\angle B = \angle E$  [Given]

$\angle BAL = \angle EDM$  [ $\because \angle A = \angle D \Rightarrow \frac{1}{2}\angle A = \frac{1}{2}\angle D$ ]

$\Rightarrow \triangle ABL \sim \triangle DEM$  [AA similarity]

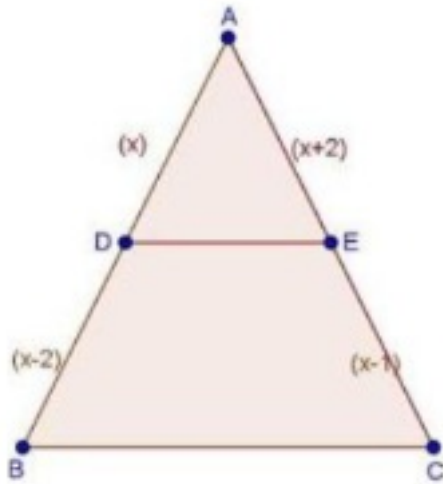
$\Rightarrow \frac{AB}{DE} = \frac{AL}{DM}$  .....(ii)

From (i) and (ii) we have

$\frac{BC}{EF} = \frac{AL}{DM}$

13. We have,





$DE \parallel BC$

Therefore, by basic proportionality theorem,

We have,

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{x}{x-2} = \frac{x+2}{x-1}$$

$$\Rightarrow x(x-1) = (x+2)(x-2)$$

$$\Rightarrow x^2 - x = x^2 - (2)^2 \quad [\because (a-b)(a+b) = a^2 - b^2]$$

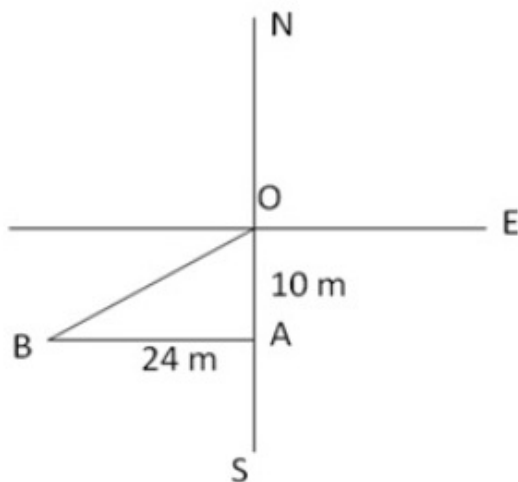
$$\Rightarrow -x = -4$$

$$\Rightarrow x = 4 \text{ cm.}$$

14. Starting from O, let the man goes from O to A and then A to B as shown in the figure.

Then,

$OA = 10\text{m}$ ,  $AB = 24\text{m}$  and  $\angle OAB = 90^\circ$



Using Pythagoras theorem:

$$OB^2 = OA^2 + AB^2$$

$$\Rightarrow OB^2 = 10^2 + 24^2$$

$$\Rightarrow OB^2 = 100 + 576$$

$$\Rightarrow OB^2 = 676$$

$$\Rightarrow OB = \sqrt{676} = 26\text{m}$$

Hence, the man is 26m south-west from the starting position.

15. Proof : In  $\triangle POQ$ ,  $AB \parallel PQ$ , (Given)

$$\frac{AO}{AP} = \frac{OB}{BQ} \dots\dots (i) \text{ (BPT)}$$

In  $\triangle OPR$   $AC \parallel PR$

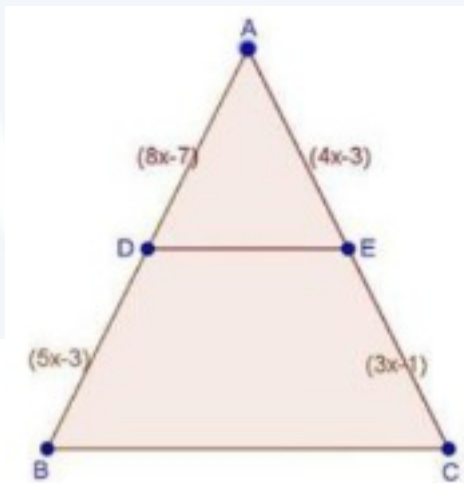
$$\frac{OA}{AP} = \frac{OC}{CR} \dots\dots (ii)$$

From eqn (I) and (ii)

$$\frac{OB}{BQ} = \frac{OC}{CR}$$

Hence  $BC \parallel QR$  ( By converse of BPT)

16. We have,



We are given that,  $DE \parallel BC$

Therefore, by thales theorem,

We have,

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{8x-7}{5x-3} = \frac{4x-3}{3x-1}$$

$$\Rightarrow (8x - 7)(3x - 1) = (4x - 3)(5x - 3)$$

$$\Rightarrow 24x^2 - 8x - 21x + 7 = 20x^2 - 12x - 15x + 9$$

$$\Rightarrow 24x^2 - 20x^2 - 29x + 27x + 7 - 9 = 0$$

$$\Rightarrow 4x^2 - 2x - 2 = 0$$

$$\begin{aligned} &\Rightarrow 2[2x^2 - x - 1] = 0 \\ &\Rightarrow 2x^2 - x - 1 = 0 \\ &\Rightarrow 2x^2 - 2x + 1x - 1 = 0 \\ &\Rightarrow 2x(x - 1) + 1(x - 1) = 0 \\ &\Rightarrow (2x + 1)(x - 1) = 0 \\ &\Rightarrow 2x + 1 = 0 \text{ or } x - 1 = 0 \\ &\Rightarrow x = -\frac{1}{2} \text{ or } x = 1 \\ &x = -\frac{1}{2} \text{ is not possible.} \\ &\therefore x = 1. \end{aligned}$$

17. In triangles ABC and DEF, we have

$$\frac{AB}{DF} = \frac{BC}{FE} = \frac{CA}{ED} = \frac{1}{2}$$

Therefore, by SSS-criterion of similarity, we have

$$\Delta ABC \sim \Delta DFE$$

$$\Rightarrow \angle A = \angle D, \angle B = \angle F \text{ and } \angle C = \angle E$$

$$\Rightarrow \angle D = 80^\circ, \angle F = 60^\circ$$

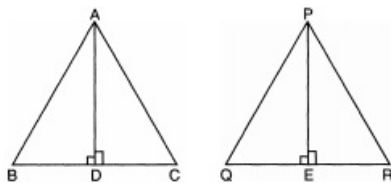
Hence,  $\angle E = 60^\circ$ .

18. Given :  $\Delta ABC \sim \Delta PQR$

$$\text{To Prove : } \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta PQR)} = \left(\frac{AB}{PQ}\right)^2 = \left(\frac{BC}{QR}\right)^2 = \left(\frac{AC}{PR}\right)^2$$

Construction: Draw  $AD \perp BC$  and  $PE \perp QR$

Proof :



$$\Delta ABC \sim \Delta PQR$$

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} \text{ (Ratio of corresponding sides of similar triangles are equal) ... (i)}$$

$$\angle B = \angle Q \text{ (Corresponding angles of similar triangles)..... (ii)}$$

In  $\Delta ADB$  and  $\Delta PEQ$

$$\angle B = \angle Q \text{ (From (ii))}$$

$$\angle ADB = \angle PEQ \text{ [ each } 90^\circ \text{]}$$

$$\therefore \Delta ADB \sim \Delta PEQ \text{ [ By AA criteria]}$$

$$\Rightarrow \frac{AD}{PE} = \frac{AB}{PQ} \text{ (Corresponding sides of similar triangles) ... (iii)}$$

From equation (i) and equation (iii)

$$\frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR} = \frac{AD}{PE} \text{ ... (iv)}$$

$$\frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta PQR)} = \frac{\frac{1}{2} \times BC \times AD}{\frac{1}{2} \times QR \times PE}$$

$$= \left( \frac{BC}{QR} \right) \times \left( \frac{AD}{PE} \right)$$

$$\left( \frac{AD}{PE} = \frac{BC}{QR} \right)$$

$$= \frac{BC}{QR} \times \frac{BC}{QR}$$

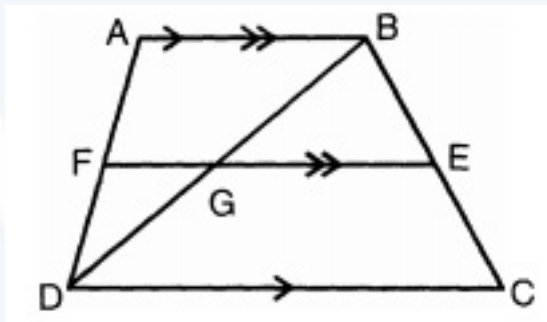
$$\Rightarrow \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta PQR)} = \frac{BC^2}{QR^2} \text{ ... (v) [from eq. (iv)]}$$

From equation (iv) and equation (v),

$$\therefore \frac{\text{ar}(\Delta ABC)}{\text{ar}(\Delta PQR)} = \left( \frac{AB}{PQ} \right)^2 = \left( \frac{BC}{QR} \right)^2 = \left( \frac{AC}{PR} \right)^2$$

$\therefore$  Ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.

19.



In a trapezium ABCD,  $AB \parallel DC$ ,  $EF \parallel AB$  and  $CD = 2AB$

$$\text{and also } \frac{BE}{EC} = \frac{4}{3} \text{ ----- (1)}$$

$AB \parallel DC$  and  $AB \parallel EF$

$$\therefore \frac{AF}{FD} = \frac{BE}{EC} = \frac{4}{3}$$

In  $\Delta BGE$  and  $\Delta BDC$

$$\angle BEG = \angle BCD \text{ (}\because \text{ corresponding angles)}$$

$$\angle GBE = \angle DBC \text{ (Common)}$$

$$\therefore \Delta BGE \sim \Delta BDC \text{ [ By AA similarity]}$$

$$\Rightarrow \frac{EG}{CD} = \frac{BE}{BC} \text{ ..... (2)}$$

$$\text{Now, from (1) } \frac{BE}{EC} = \frac{4}{3}$$

$$\Rightarrow \frac{EC}{BE} = \frac{3}{4}$$

$$\Rightarrow \frac{EC}{BE} + 1 = \frac{3}{4} + 1$$

$$\Rightarrow \frac{EC+BE}{BE} = \frac{7}{4}$$

$$\Rightarrow \frac{BC}{BE} = \frac{7}{4} \text{ or } \frac{BE}{BC} = \frac{4}{7}$$

from equation (2),  $\frac{EG}{CD} = \frac{4}{7}$

$$\text{So } EG = \frac{4}{7}CD \dots\dots(3)$$

Similarly,  $\triangle DGF \sim \triangle DBA$  (by AA similarity)

$$\Rightarrow \frac{DF}{DA} = \frac{FG}{AB}$$

$$\Rightarrow \frac{FG}{AB} = \frac{3}{7}$$

$$\Rightarrow FG = \frac{3}{7}AB \dots(4)$$

$$\left[ \begin{array}{l} \because \frac{AF}{AD} = \frac{4}{7} = \frac{BE}{BC} \\ \Rightarrow \frac{EC}{BC} = \frac{3}{7} = \frac{DE}{DA} \end{array} \right]$$

Adding equations (3) and (4), we get,

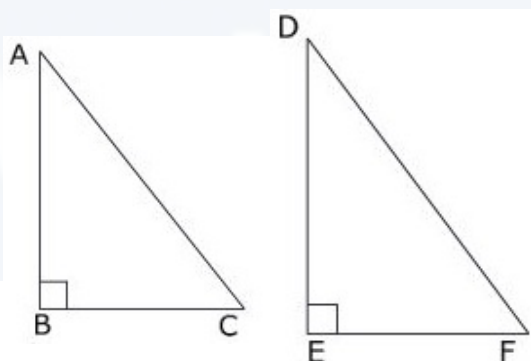
$$EG + FG = \frac{4}{7}CD + \frac{3}{7}AB$$

$$\Rightarrow EF = \frac{4}{7} \times (2AB) + \frac{3}{7}AB$$

$$= \frac{8}{7}AB + \frac{3}{7}AB = \frac{11}{7}AB$$

$$\therefore 7EF = 11AB$$

20.



i. Given: In  $\triangle ABC$  such that

$$AC^2 = AB^2 + BC^2$$

To prove: Triangle ABC is right angled at B

Construction: Construct a triangle DEF such that

$$DE = AB, EF = BC \text{ and } \angle E = 90^\circ$$

Proof:  $\because \triangle DEF$  is a right angled triangle right angled at E [construction]

$\therefore$  By Pythagoras theorem, we have

$$DF^2 = DE^2 + EF^2$$

$$\Rightarrow DF^2 = AB^2 + BC^2 \text{ [ } \because DE = AB \text{ and } EF = BC \text{]}$$

$$\Rightarrow DF^2 = AC^2 [\because AB^2 + BC^2 = AC^2]$$

$$\Rightarrow DF = AC$$

Thus, in  $\triangle ABC$  and  $\triangle DEF$ , we have

$$AB = DE$$

$$BC = EF$$

and  $AC = DF$  [By Construction and (i)]

$$\therefore \triangle ABC \cong \triangle DEF \text{ (SSS)}$$

$$\Rightarrow \angle B = \angle E = 90^\circ$$

Hence,  $\triangle ABC$  is a right triangle.

ii. In  $\triangle QPR$ ,  $\angle QPR = 90^\circ$

$$\Rightarrow 24^2 + x^2 = 26^2$$

$$\Rightarrow x = 10$$

$$\Rightarrow PR = 10 \text{ cm}$$

Now in  $\triangle PKR$ ,  $PR^2 = PK^2 + KR^2$  [as  $10^2 = 8^2 + 6^2$ ]

$\therefore$   $\triangle PKR$  is right angled at  $K$

$$\Rightarrow \angle PKR = 90^\circ$$

Vidya Champ