

**CBSE Test Paper 01**  
**Chapter 4 Quadratic Equation**

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1.  $(x + 1)^2 - x^2 = 0$  has **(1)**
  - a. no real roots
  - b. 1 real root
  - c. 2 real roots
  - d. 4 real roots
2.  $9x^2 + 12x + 4 = 0$  have **(1)**
  - a. Real and Distinct roots
  - b. No real roots
  - c. Distinct roots
  - d. Real and Equal roots
3. If the equation  $(a^2 + b^2)x^2 - 2(ac + bd)x + c^2 + d^2 = 0$  has equal roots, then **(1)**
  - a.  $ad = bc$
  - b.  $ab = cd$
  - c.  $ad = \sqrt{bc}$
  - d.  $ab = \sqrt{cd}$
4. The ratio of sum and the product of the roots of  $7x^2 - 12x + 18 = 0$  is **(1)**
  - a. 2 : 3
  - b. 3 : 2
  - c. 7 : 18
  - d. 7 : 12
5. If  $y = 1$  is the common root of  $ly^2 + ly + 3 = 0$  and  $y^2 + y + m = 0$ , then the value of ' $lm$ ' is **(1)**
  - a. 3
  - b. -4
  - c. 4
  - d. -3
6. Solve the quadratic equations by factorization method:  $x^2 - 9 = 0$  **(1)**
7. Find the values of  $p$  for which the quadratic equation  $4x^2 + px + 3 = 0$  has equal roots. **(1)**

8. Form a quadratic equation whose roots are -3 and 4. **(1)**
9. If  $x = \frac{-1}{2}$  is a solution of the quadratic equation  $3x^2 + 2kx + 3 = 0$ , find the value of k. **(1)**
10. Write the discriminant of the given quadratic equation  $x^2 + x - 12 = 0$  **(1)**
11. Find the values of k for which the given equation has real and equal roots:  $(k + 1)x^2 - 2(k - 1)x + 1 = 0$  **(2)**
12. Check, whether the quadratic equation have real roots and if so, then find the roots of equation.  $6x^2 + x - 2 = 0$  **(2)**
13. Check whether the given equation is quadratic equation:  $(x-3)(2x + 1) = x(x + 5)$  **(2)**
14. In a class test, the sum of Shefali's marks in Mathematics and English is 30. Had she got 2 marks more in Mathematics and 3 marks less in English, the product of their marks would have been 210. Find her marks in the two subjects. **(3)**
15. If 2 is a root of the quadratic equation  $3x^2 + px - 8 = 0$  and the quadratic equation  $4x^2 - 2px + k = 0$  has equal roots, find k. **(3)**
16. If p, q, r and s are real numbers such that  $pr = 2(q + s)$ , then show that at least one of the equations  $x^2 + px + q = 0$  and  $x^2 + rx + s = 0$  has real roots. **(3)**
17. The speed of a boat in still water is 8 km/hr. It can go 15 km upstream and 22 km downstream in 5 hours. Find the speed of the stream. **(3)**
18. A train travelling at a uniform speed for 360 km, would have taken 48 minutes less to travel the same distance if its speed were 5 km/hour more. Find the original speed of the train. **(4)**
19. Solve for x:  $\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$  **(4)**
20. Solve for x:  $2\left(\frac{x+2}{2x-3}\right) - 9\left(\frac{2x-3}{x+2}\right) = 3$ ; given that  $x \neq -2$ ,  $x \neq \frac{3}{2}$  **(4)**

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**Solution**

1. b. 1 real root

**Explanation:** Given:  $(x + 1)^2 - x^2 = 0$

$$\Rightarrow x^2 + 1 + 2x - x^2 = 0$$

$$\Rightarrow 2x + 1 = 0$$

$$\Rightarrow x = \frac{-1}{2}$$

Therefore,  $(x^2 + 1)^2 - x^2 = 0$  is a linear polynomial and has one real root.

2. d. Real and Equal roots

**Explanation:** Comparing the given equation to the below equation

$$ax^2 + bx + c = 0$$

$$a = 9, b = 12, c = 4$$

$$D = b^2 - 4ac$$

$$D = 12^2 - 4 \times 9 \times 4$$

$$D = 144 - 144$$

$$D = 0$$

If  $b^2 - 4ac = 0$  then equation have equal and real roots.

3. a.  $ad = bc$

**Explanation** If the equation  $(a^2 + b^2)x^2 - 2(ac + bd)x + c^2 + d^2 = 0$  has equal roots, then

$$b^2 - 4ac = 0$$

$$\Rightarrow [-2(ac + bd)]^2 - 4 \times (a^2 + b^2) \times (c^2 + d^2) = 0$$

$$\Rightarrow 4[a^2c^2 + b^2d^2 + 2abcd] - 4[a^2c^2 + a^2d^2 + b^2c^2 + b^2d^2] = 0$$

$$\Rightarrow 4[a^2c^2 + b^2d^2 + 2abcd - a^2c^2 - a^2d^2 - b^2c^2 - b^2d^2] = 0$$

$$\Rightarrow a^2d^2 + b^2c^2 - 2abcd = 0$$

$$(ad - bc)^2 = 0$$

$$\Rightarrow (ad - bc)^2 = 0$$

$$\Rightarrow ad - bc = 0$$

$$\Rightarrow ad = bc$$

4. a. 2:3

**Explanation:** Ratio of sum and product of the roots of  $7x^2 - 12x + 18 = 0$  is

$$\frac{\alpha + \beta}{\alpha\beta}$$

$\Rightarrow$

$$\Rightarrow \frac{-b}{c}$$

$$\Rightarrow \frac{12}{18} = \frac{2}{3} = 2 : 3$$

5. a. 3

**Explanation:** In quadratic equation  $ly^2 + ly + 3 = 0$ ,

$$l(1)^2 + l(1) + 3 = 0$$

$$\Rightarrow l + l + 3 = 0$$

$$\Rightarrow 2l + 3 = 0$$

$$\Rightarrow l = \frac{-3}{2}$$

And  $(1)^2 + 1 + m = 0$

$$\Rightarrow 1 + 1 + m = 0$$

$$\Rightarrow 2 + m = 0$$

$$\Rightarrow m = -2$$

$$\therefore lm = \frac{-3}{2} \times (-2) = 3$$

6. We have,

$$x^2 - 9 = 0$$

$$\Rightarrow (x - 3)(x + 3) = 0$$

$$\Rightarrow x - 3 = 0 \text{ or, } x + 3 = 0$$

$$\Rightarrow x = 3 \text{ or, } x = -3 \Rightarrow x = \pm 3$$

Thus,  $x = 3$  and  $x = -3$  are roots of the given equation.

7.  $4x^2 + px + 3 = 0$

$$a = 4, b = p \text{ and } c = 3$$

As the equation has equal roots

$$\therefore D = 0$$

$$D = b^2 - 4ac = 0$$

$$\text{or, } p^2 - 4 \times 4 \times 3 = 0$$

$$\text{or, } p^2 - 48 = 0$$

$$\text{or, } p^2 = 48$$

$$\text{or, } p = \pm 4\sqrt{3}$$

8. We have,  $x = 4$  and  $x = -3$ .

Then,

$$x - 4 = 0 \text{ and } x + 3 = 0$$

$$\Rightarrow (x - 4)(x + 3) = 0$$

$$\Rightarrow x^2 + 3x - 4x - 12 = 0$$

$$\Rightarrow x^2 - x - 12 = 0$$

This is the required quadratic equation

9. we have,  $3x^2 + 2kx + 3 = 0$

put,  $x = \frac{-1}{2}$  (given)

$$\Rightarrow 3\left(\frac{-1}{2}\right)^2 + 2k\left(\frac{-1}{2}\right) + 3 = 0$$

$$\Rightarrow 3\left(\frac{1}{4}\right) - k + 3 = 0$$

$$\Rightarrow \frac{3}{4} - k + 3 = 0$$

$$\Rightarrow k = 3 + \frac{3}{4}$$

$$\therefore k = \frac{15}{4}$$

10. The given quadratic equation is  $x^2 + x - 12 = 0$ ,

here  $a=1, b=1, c=-12$

$$\therefore D = b^2 - 4ac = (1)^2 - 4((1)(-12)) = 1 + 48 = 49$$

Hence, the discriminant is 49.

11. We have,  $(k+1)x^2 - 2(k-1)x + 1 = 0$ .

$a = k + 1, b = -2(k - 1), c = 1$ .

$$D = b^2 - 4ac = 4(k-1)^2 - 4(k+1) = 4(k^2 - 3k)$$

The given equation will have real and equal roots, if

$$D = 0 \Rightarrow 4(k^2 - 3k) = 0 \Rightarrow k^2 - 3k = 0 \Rightarrow k(k - 3) = 0 \Rightarrow k = 0, 3$$

12. The given equation is  $6x^2 + x - 2 = 0$

Here,  $a = 6, b = 1$  and,  $c = -2$

$$\therefore D = b^2 - 4ac = 1 - 4 \times 6 \times -2 = 49 > 0$$

So, the given equation has real roots, given by

$$\alpha = \frac{-b + \sqrt{D}}{2a} = \frac{-1 + \sqrt{49}}{2 \times 6} = \frac{-1 + 7}{12} = \frac{6}{12} = \frac{1}{2}$$

$$\text{and, } \beta = \frac{-b - \sqrt{D}}{2a} = \frac{-1 - \sqrt{49}}{2 \times 6} = \frac{-1 - 7}{12} = \frac{-8}{12} = \frac{-2}{3}$$

13. The given equation is  $(x - 3)(2x + 1) = x(x + 5)$

$$\implies 2x^2 + x - 6x - 3 = x^2 + 5x$$

$$\implies 2x^2 - 5x - 3 = x^2 + 5x$$

$$\implies x^2 - 10x - 3 = 0$$

It is in the form of  $ax^2 + bx + c = 0$ ,  $a \neq 0$

$\therefore$  the given equation is a quadratic equation.

14. Let Shefali's marks in Mathematics =  $x$

Let Shefali's marks in English =  $30 - x$

If, she had got 2 marks more in Mathematics, her marks would be =  $x + 2$

If, she had got 3 marks less in English, her marks in English would be =  $30 - x - 3 = 27 - x$

According to given condition:

$$\implies (x + 2)(27 - x) = 210$$

$$\implies 27x - x^2 + 54 - 2x = 210$$

$$\implies x^2 - 25x + 156 = 0$$

Comparing quadratic equation  $x^2 - 25x + 156 = 0$  with general form  $ax^2 + bx + c = 0$ ,

We get  $a = 1$ ,  $b = -25$  and  $c = 156$

Applying Quadratic Formula  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$x = \frac{25 \pm \sqrt{(-25)^2 - 4(1)(156)}}{2 \times 1}$$

$$\implies \frac{25 \pm \sqrt{625 - 624}}{2}$$

$$\implies x = \frac{25 \pm \sqrt{1}}{2}$$

$$\implies x = \frac{25+1}{2}, \frac{25-1}{2}$$

$$\implies x = 13, 12$$

Therefore, Shefali's marks in Mathematics = 13 or 12

Shefali's marks in English =  $30 - x = 30 - 13 = 17$

Or Shefali's marks in English =  $30 - x = 30 - 12 = 18$

Therefore, her marks in Mathematics and English are (13, 17) or (12, 18).

15. Given, 2 is a root of the equation,  $3x^2 + px - 8 = 0$

Putting  $x = 2$  in  $3x^2 + px - 8 = 0$

$$12 + 2p - 8 = 0$$

$$\text{or, } p = -2$$

Given,  $4x^2 - 2px + k = 0$  has equal roots

$4x^2 + 4x + k = 0$  has equal roots

$$D = b^2 - 4ac = 0$$

$$\text{or, } (4)^2 - 4(4)(k) = 0$$

$$\text{or, } 16 - 16k = 0$$

$$\text{or, } 16k = 16$$

$$\therefore k = 1$$

16. Given quadratic equations are;

$$x^2 + px + q = 0 \text{ ---(i)}$$

$$\text{and, } x^2 + rx + s = 0 \text{ .....(ii)}$$

$$\text{Also given ; } pr = 2(q + s) \text{ .....(iii)}$$

Let  $D_1$  and  $D_2$  be the discriminant of quadratic equations (i) and (ii) respectively.

Then,

$$D_1 = p^2 - 4q \text{ and } D_2 = r^2 - 4s$$

$$\Rightarrow D_1 + D_2 = p^2 - 4q + r^2 - 4s = (p^2 + r^2) - 4(q + s)$$

$$\Rightarrow D_1 + D_2 = p^2 + r^2 - 4\left(\frac{pr}{2}\right) \text{ [from equation (iii)]}$$

$$\Rightarrow D_1 + D_2 = p^2 + r^2 - 2pr = (p - r)^2 \geq 0 \text{ [}\because (p - r)^2 \geq 0 \text{ for all real } p, r\text{]}$$

Now, Since sum of both  $D_2$  &  $D_1$  is greater than or equal to 0. Hence, both can't be negative.

$\Rightarrow$  At least one of  $D_1$  and  $D_2$  is greater than or equal to zero

**Case 1.** If  $D_1 \geq 0$ , equation (i) has real roots.

**Case 2.** If  $D_2 \geq 0$ , equation (ii) has real roots.

**Case 3.** If  $D_1$  &  $D_2$  both  $\geq 0$ , then equation (i) & (ii) both have equal roots.

Clearly, from case 1, 2 & 3 at least one given quadratic equations has equal roots.

17. Given, speed of boat in still water = 8 Km/hr. Let the speed of the stream be  $x$  km/hr.

Then,

Speed of boat in downstream =  $(8 + x)$  km/hr

Speed of boat in upstream =  $(8 - x)$  km/hr

We know that time taken to cover 'd' km with speed 's' km/hr is  $\frac{d}{s}$

So, Time taken by the boat to go 15 km upstream =  $\frac{15}{8-x}$  hours.

&, Time taken by the boat to 22 km downstream =  $\frac{22}{8+x}$  hours.

It is given that the total time taken by boat to go 15 km upstream & 22 km downstream is 5 hours.

$$\therefore \frac{15}{8-x} + \frac{22}{8+x} = 5$$

$$\Rightarrow \frac{15(8+x) + 22(8-x)}{(8-x)(8+x)} = 5$$

$$\Rightarrow \frac{120 + 15x + 176 - 22x}{8^2 - x^2} = 5$$

$$\Rightarrow \frac{-7x + 296}{64 - x^2} = 5$$

$$\Rightarrow -7x + 296 = 5(64 - x^2)$$

$$\Rightarrow -7x + 296 = 320 - 5x^2$$

$$\Rightarrow 5x^2 - 7x + 296 - 320 = 0$$

$$\Rightarrow 5x^2 - 7x - 24 = 0$$

$$\Rightarrow 5x^2 - 15x + 8x - 24 = 0$$

$$\Rightarrow 5x(x - 3) + 8(x - 3) = 0$$

$$\Rightarrow (5x + 8)(x - 3) = 0$$

$$\Rightarrow x - 3 = 0 \quad [\because \text{Speed can not be negative } \therefore 5x + 8 \neq 0]$$

$$\Rightarrow x = 3$$

Hence, the speed of the stream is 3 km/hr.

18. Given that a train travelling at a uniform speed for 360 km

Let the original speed of the train be x km/hr

$$\text{Time taken} = \frac{\text{Distance}}{\text{Speed}} = \frac{360}{x}$$

$$\text{Time taken at increased speed} = \frac{360}{x+5} \text{ hours.}$$

According to the question

$$\frac{360}{x} - \frac{360}{x+5} = \frac{48}{60}$$

$$360 \left[ \frac{1}{x} - \frac{1}{x+5} \right] = \frac{4}{5}$$

$$\text{or, } \frac{360(x+5-x)}{x^2+5x} = \frac{4}{5}$$

$$\text{or, } \frac{1800}{x^2+5x} = \frac{4}{5}$$

$$\Rightarrow x^2 + 5x - 2250 = 0$$



$$\Rightarrow x^2 + (50 - 45)x - 2250 = 0$$

$$\Rightarrow x^2 + 50x - 45x - 2250 = 0$$

$$\Rightarrow (x + 50)(x - 45) = 0$$

Either  $x = -50$  or  $x = 45$

As speed cannot be negative

$\therefore$  Original speed of train = 45 km/hr.

19. We have the following equation,

$$\sqrt{3}x^2 + 10x + 7\sqrt{3} = 0$$

Now factorise the equation,

$$\sqrt{3}x^2 + 3x + 7x + 7\sqrt{3} = 0$$

$$\Rightarrow \sqrt{3}x(x + \sqrt{3}) + 7(x + \sqrt{3}) = 0$$

$$\Rightarrow (x + \sqrt{3})(\sqrt{3}x + 7) = 0$$

$$\Rightarrow x = -\sqrt{3} \text{ or } x = \frac{-7}{\sqrt{3}}$$

If  $x = \frac{-7}{\sqrt{3}}$  we need to rationalise it.

$$\Rightarrow x = -\frac{7 \times \sqrt{3}}{\sqrt{3} \times \sqrt{3}} = -\frac{7\sqrt{3}}{3}$$

Therefore, Roots are  $-\sqrt{3}, -\frac{7\sqrt{3}}{3}$

20. Let  $\frac{x+2}{2x-3} = y$  ... (i)

$\therefore$  Given equation becomes,

$$2y - 9 \times \frac{1}{y} = 3$$

$$\Rightarrow 2y^2 - 3y - 9 = 0$$

$$\Rightarrow 2y^2 - 6y + 3y - 9 = 0$$

$$\Rightarrow 2y(y - 3) + 3(y - 3) = 0$$

$$\Rightarrow (2y + 3)(y - 3) = 0$$

$$\Rightarrow y = -\frac{3}{2} \text{ or } y = 3$$

Putting the value of  $y$  in equation (i), we get

$$\Rightarrow \frac{x+2}{2x-3} = -\frac{3}{2} \text{ or } \frac{x+2}{2x-3} = 3$$

$$\Rightarrow 2x + 4 = -6x + 9 \text{ or } x + 2 = 6x - 9$$

$$\Rightarrow 8x = 5 \text{ or } -5x = -11$$

$$\Rightarrow x = \frac{5}{8} \text{ or } x = \frac{11}{5}$$