

CBSE Test Paper 02
Chapter 1 Real Number

1. _____ is neither prime nor composite. **(1)**
 - a. 4
 - b. 1
 - c. 2
 - d. 3
2. All non-terminating and non-recurring decimal numbers are **(1)**
 - a. rational numbers
 - b. irrational numbers
 - c. integers
 - d. natural numbers
3. The HCF of two consecutive odd numbers is **(1)**
 - a. 2
 - b. 0
 - c. 1
 - d. 3
4. The decimal expansion of ' π ': **(1)**
 - a. is non-terminating and non-recurring
 - b. is terminating
 - c. does not exist
 - d. is non-terminating and recurring
5. If a is rational and \sqrt{b} is irrational, then $a + \sqrt{b}$ is: **(1)**
 - a. an irrational number
 - b. an integer
 - c. a natural number
 - d. a rational number
6. Find the simplest form of $\frac{69}{92}$. **(1)**
7. State whether the given rational number will have a terminating decimal expansion or a nonterminating repeating decimal expansion. **(1)**

8. What can you say about the prime factorisations of the denominators of 43.123456789 . **(1)**
9. Find the LCM and HCF of 24, 15 and 36 by applying the prime factorization method. **(1)**
10. For any integer a and 3, there exists unique integers q and r such that $a = 3q + r$. Find the possible values of r . **(1)**
11. If α and β are zeroes of $x^2 - (k - 6)x + 2(2k - 1)$, find the value of k : if $\alpha + \beta = \frac{1}{2}\alpha\beta$. **(2)**
12. Find the prime factorization of 1296. **(2)**
13. Without actual division, show that rational number $\frac{33}{50}$ is a terminating decimal. Express decimal form. **(2)**
14. Show that one and only one out of n , $(n + 2)$ or $(n + 4)$ is divisible by 3, where $n \in \mathbb{N}$. **(3)**
15. Write the HCF and LCM of smallest odd composite number and the smallest odd prime number. If an odd number p divides q^2 , then will it divide q^3 also? Explain. **(3)**
16. The HCF and LCM of two polynomials $P(x)$ and $Q(x)$ are $(2x-1)$ and $(6x^3 + 25x^2 - 24x + 5)$ respectively. If $P(x) = 2x^2 + 9x - 5$, determine $Q(x)$. **(3)**
17. The traffic lights at three different road crossings change after every 48 seconds, 72 seconds and 108 seconds respectively. If they all change simultaneously at 8 a.m. then at what time will they again change simultaneously? **(3)**
18. Show that the cube of any positive integer is of the form $4m$, $4m+1$ or $4m+3$, for some integer m . **(4)**
19. Find the HCF of 256 and 36 using Euclid's Division Algorithm. Also, find their LCM and verify that $\text{HCF} \times \text{LCM} = \text{Product of the two numbers}$. **(4)**
20. Use Euclid's division algorithm, to find the largest number, which divides 957 and 1280 leaving remainder 5 in each case. **(4)**

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Solution

1. b. 1

Explanation: 1 is neither prime nor composite.

A prime is a natural number greater than 1 that has no positive divisors other than 1 and itself

e.g. 5 is prime because 1 and 5 are its only positive integers factors but 6 is composite because it has divisors 2 and 3 in addition to 1 and 6.

2. b. irrational numbers

Explanation: All non-terminating and non-recurring decimal numbers are irrational numbers. A number is rational if and only if its decimal representation is repeating or terminating.

3. c. 1

Explanation: The HCF of two consecutive odd numbers is 1. (e.g. the HCF of 25, 27 is 1)

4. a. is non-terminating and non-recurring

Explanation: The decimal expansion of ' π ' is non-terminating and non-recurring.

The value of $\pi = 3.141592653589.....$

\therefore Value of π is not-repeating decimal, non-terminating and non-recurring number.

5. a. an irrational number

Explanation: Let a be rational and \sqrt{b} is irrational.

If possible let $a + \sqrt{b}$ be rational.

Then $a + \sqrt{b}$ is rational and a is rational.

$\Rightarrow [(a + \sqrt{b}) - a]$ is rational [Difference of two rationals is rational]

$\Rightarrow \sqrt{b}$ is rational.

This contradicts the fact that \sqrt{b} is irrational.

The contradiction arises by assuming that $a + \sqrt{b}$ is rational.

Therefore, $a + \sqrt{b}$ is irrational.

6. The prime factors of 69 and 92 are:

$$69 = 3 \times 23$$

$$92 = 4 \times 23 = 2^2 \times 23$$

$$\text{Hence } \frac{69}{92} = \frac{3 \times 23}{2 \times 2 \times 23} = \frac{3}{4}$$

7. $\frac{13}{3125} = \frac{13}{5^5}$ Here, $q = 5^5$,

which is of the form $2^n 5^m$ ($n = 0, m = 5$).

So the rational number $\frac{13}{3125}$ has a terminating decimal expansion.

$$\begin{aligned} 8. \quad 43.123456789 &= \frac{43123456789}{1000000000} = \frac{43123456789}{10^9} \\ &= \frac{43123456789}{(2 \times 5)^9} = \frac{43123456789}{2^9 \times 5^9} \end{aligned}$$

Prime factorization of the denominator of 43.123456789 are $2^9 \times 5^9$

and are of the form, $2^m \times 5^n$

where $m=9$ and $n=9$

9. 24, 15 and 36

Let us first find the factors of 24, 15 and 36

$$24 = 2^3 \times 3$$

$$15 = 3 \times 5$$

$$36 = 2 \times 2 \times 3 \times 3$$

$$\text{LCM of 24, 15 and 36} = 2 \times 2 \times 2 \times 3 \times 3 \times 5$$

$$\text{LCM of 24, 15 and 36} = 360$$

$$\text{HCF of 24, 15 and 36} = 3$$

10. According to Euclid's division lemma for two positive number a and b there exist integers q and r such that $a = b \times q + r$ where $0 \leq r < b$.

Here $b = 3$

Therefore, $0 \leq r < 3$

So, the possible values of r can be 0, 1, 2 because as per Euclid's division lemma r is greater then or equal to zero and smaller then b

11. we are given that α and β are zeroes of $x^2 - (k - 6)x + 2(2k - 1)$,

Given, α, β are the zeroes of polynomial

$$x^2 - (k - 6)x + 2(2k - 1)$$

$$\therefore \alpha + \beta = -[-(k - 6)] = k - 6$$

$$\alpha\beta = 2(2k - 1)$$

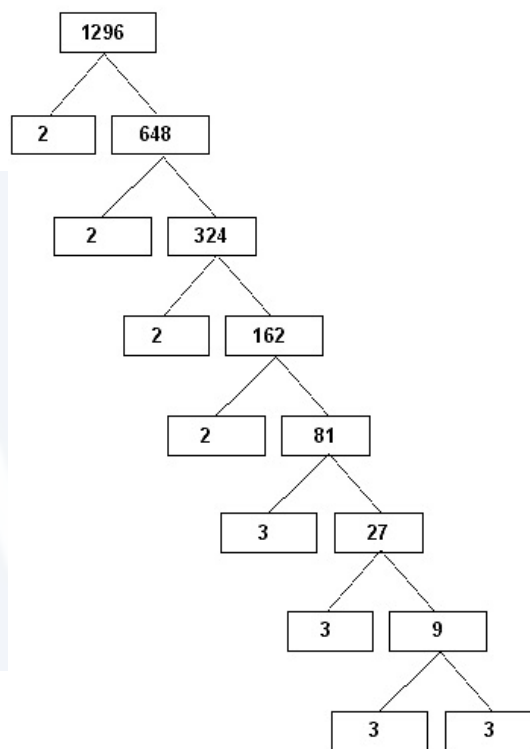
$$\alpha + \beta = \frac{1}{2}\alpha\beta$$

$$\text{or, } k + 6 = \frac{2(2k - 1)}{2}$$

$$\text{or, } k - 6 = 2k - 1$$

$$\text{or } k = -5$$

Hence the value of $k = -5$.



$$\text{So, } 1296 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 = 2^4 \times 3^4$$

Hence the prime factors of 1296 are 2, 2, 2, 2, 3, 3, 3, 3.

13. The given number is $\frac{33}{50}$.

$$\text{The denominator } 50 = 2 \times 25$$

$$= 2 \times 5^2 = 2^1 \times 5^2$$

So the denominator is in the form of $2^m \times 5^n$ where $m = 1$ and $n = 2$.

Hence the given number is a terminating decimal.

$$\begin{aligned} \text{Now, } \frac{33}{50} &= \frac{33}{(2 \times 5^2)} = \frac{33 \times 2}{(2^2 \times 5^2)} = \frac{66}{(2 \times 5)^2} \\ &= \frac{66}{(10)^2} = \frac{66}{100} = 0.66. \end{aligned}$$

14. Let the number be $(3q + r)$

$$n = 3q + r \quad 0 \leq r < 3$$

or $3q, 3q + 1, 3q + 2$

If $n = 3q$ then, numbers are $3q, (3q + 1), (3q + 2)$

$3q$ is divisible by 3.

If $n = 3q + 1$ then, numbers are $(3q + 1), (3q + 3), (3q + 4)$

$(3q + 3)$ is divisible by 3

If $n = 3q + 2$ then, numbers are $(3q + 2), (3q + 4), (3q + 6)$

$(3q + 6)$ is divisible by 3.

\therefore out of $n, (n + 2)$ and $(n + 4)$ only one is divisible by 3.

15. Smallest odd composite number = 9

and smallest odd prime number = 3

HCF of 9 and 3 = 3 and LCM of 9 and 3 = 9

Now, if an odd number p divides q^2 , then p is one of the factors of q^2 ,

i.e. $q^2 = pm$, for some integer m(i)

Now, $q^3 = q^2 \times q$

$$\Rightarrow q^3 = pm \times q$$

$$\Rightarrow q^3 = p(mq) \text{ [from Eq(i)]}$$

$\Rightarrow p$ is a factor of q^3 also $\Rightarrow p$ divides q^3 .

16. It is given that $P(x) = 2x^2 + 9x - 5$

$$= 2x^2 + 10x - x - 5 = (x + 5)(2x - 1)$$

HCF of $P(x)$ and $Q(x) = (2x - 1)$ and

$$\text{LCM of } p(x) \text{ and } Q(x) = 6x^3 + 25x^2 - 24x + 5$$

$$= (2x - 1)(3x^2 + 14x - 5) \text{ [Applying factor theorem]}$$

$$= (2x - 1)(3x^2 + 15x - x - 5)$$

$$= (2x - 1)(x + 5)(3x - 1)$$

Now, $P(x) \times Q(x) = [\text{HCF of } P(x) \text{ and } Q(x)] \times [\text{LCM of } P(x) \text{ and } Q(x)]$

$$\Rightarrow (x + 5)(2x - 1) \Rightarrow Q(x) = (2x - 1)(2x - 1)(x + 5)(3x - 1)$$

$$Q(x) = (2x - 1)(3x - 1) = 6x^2 - 5x + 1$$

17. We have to find Prime Factors of the following numbers

$$48 = 2^4 \times 3$$

$$72 = 2^3 \times 3^2$$

$$108 = 2^2 \times 3^3$$

so the LCM of 48, 72 and 108 is

$$LCM = 2^4 \times 3^3$$

$$LCM = 16 \times 27 = 432$$

$$432 \text{ seconds} = \frac{432}{60} \text{ mins}$$

$$432 \text{ seconds} = 7.2 \text{ mins}$$

So the time it will change together again is

$$8 \text{ am} + 7 \text{ mins } 12 \text{ seconds} = 8 : 07 : 12 \text{ am}$$

18. Let a be an arbitrary positive integer.

Then, by Euclid's division Lemma, corresponding to the positive integers a and 4, there exist non-negative integers q and r such that

$$a = 4q + r, \text{ where } 0 \leq r < 4$$

$$\Rightarrow a^3 = (4q+r)^3 = 64q^3 + r^3 + 12qr^2 + 48q^2r \quad [(A+B)^3 = A^3 + B^3 + 3AB^2 + 3A^2B]$$

$$\Rightarrow a^3 = 64q^3 + 48q^2r + 12qr^2 + r^3 \text{ where } 0 \leq r < 4 \dots\dots(i)$$

The possible values of r are 0,1,2,3.

Case I: If $r=0$ then from Eq.(i) we get

$$a^3 = 64q^3 + 48q^2(0) + 12q(0)^2 + (0)^3$$

$$a^3 = 64q^3 = 4(16q^3)$$

$$\Rightarrow a^3 = 4m$$

where, $m = 16q^3$ is an integer.

Case II: If $r = 1$, then from Eq.(i), we get

$$a^3 = 64q^3 + 48q^2r + 12qr + 1$$

$$a^3 = 64q^3 + 48q^2(1) + 12q(1)^2 + (1)^3$$

$$= 4(16q^3 + 12q^2 + 3q) + 1 = 4m + 1$$

where, $m = (16q^3 + 12q^2 + 3q)$ is an integer.

Case III: If $r = 2$, then from Eq.(i), we get

$$a^3 = 64q^3 + 48q^2(2) + 12q(2)^2 + (2)^3$$

$$a^3 = 64q^3 + 96q^2 + 48q + 8$$

$$= 4(16q^3 + 24q^2 + 12q + 2) = 4m$$

where, $m = (16q^3 + 24q^2 + 12q + 2)$ is an integer.

Case IV: If $r = 3$, then from Eq.(i), we get

$$a^3 = 64q^3 + 48q^2(3) + 12q(3)^2 + (3)^3$$

$$a^3 = 64q^3 + 144q^2 + 108q + 27$$

$$= 64q^3 + 144q^2 + 108q + 24 + 3$$

$$= 4(16q^3 + 36q^2 + 27q + 6) + 3 = 4m + 3$$

where, $m = (16q^3 + 36q^2 + 27q + 6)$ is an integer.

Hence, the cube for any positive integer is of the form $4m$, $4m + 1$ or $4m + 3$ for some integer m .

19. Since $256 > 36$, we apply the division lemma to 256 and 36, to get

$$256 = 36 \times 7 + 4$$

Again on applying the division lemma to 36 and 4, to get

$$36 = 4 \times 9 + 0$$

Hence, the HCF of 256 and 36 is 4

$$256 = 16 \times 16 = 2^4 \times 2^4 = 2^8$$

$$36 = 4 \times 9 = 2^2 \times 3^2$$

$$\text{So LCM}(36, 256) = 2^8 \times 3^2 = 256 \times 9 = 2304$$

$$\text{HCF} \times \text{LCM} = 4 \times 2304 = 9216$$

$$\text{and } 36 \times 256 = 9216$$

$$\text{So HCF} \times \text{LCM} = 36 \times 256$$

Hence $\text{HCF} \times \text{LCM} = \text{Product of two numbers}$

20. Given numbers are 957 and 1280 and remainder is 5 in each case. Then, new numbers after subtracting remainders are

$$957 - 5 = 952 \text{ and } 1280 - 5 = 1275$$

Now, by using Euclid's Division lemma, we get

$$1275 = (952 \times 1) + 323$$

Here remainder = 323

So, on taking 952 as dividend and 323 as new divisor and then apply Euclid's Division

lemma, we get

$$952 = (323 \times 2) + 306$$

Again, remainder = 306.

So, on taking 323 as dividend and 306 as new divisor and then apply Euclid's Division lemma, we get

$$323 = (306 \times 1) + 17$$

Again, remainder = 17.

So, on taking 306 as dividend and 17 as new divisor and then apply Euclid's Division lemma, we get

$$306 = (17 \times 18) + 0$$

Here, remainder = 0.

Since, remainder has now become zero and the last divisor is 17.

Therefore, HCF of 952 and 1275 is 17.



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